# POLLUTEv7 Examples



# Example Summary

All the examples in this appendix have been stored in the Examples project, shown below. When reviewing these examples, you can either use the models in the Examples project or create a new project and create the models using the New Model button. In the examples below, it is assumed that the models in the Examples project are being used.

Model #	Title	~
1	Case 1: Subtitle D Landfill with constant source concentration	
2	Case 2: Pure diffusion - specified surface and base concentrations	
3	Case 3: Advective diffusive transport, Constant source, Base aquifer	
4	Case 4: Finite mass, leachate collection, base aquifer	
5	Case 5: Hydraulic trap, Finite mass, leachate collection, base aquifer	
6	Case 6: 1m thick liner, 3m fractured till, finite mass, sorption	
7	Case 7: Lateral migration in fractured rock	
8	Case 8: Analysis of a Labratory Diffusion test with background	
9	Case 9: Freundlich Non-linear sorption in a lab diffusion test	
10	Case 10: Time-varying velocity; termination of leachate collection	
11	Case 11: Variable source concentration history	1
12	Case 12: POLLUTE vs Analytical solutionsingle fracture	
13	Case 13: Comparison with an analytical method.	
14	Case 14: Landfill with Primary and Secondary Leachate Collection	
15	Case 15: Landfill with Primary and Secondary Leachate Collection with Failure.	1
16	Case 16: Monte Carlo Simulation	1
17	Case 17. Landfill with composite primary and clay secondary liners.	
18	Case 18: Phase Change in Secondary Leachate Collection System	
19	Case 19: Multiphase Diffusion Test by Buss et al.	
20	Case 20: Sensitivity Analysis	
		~

Shows how to create a **Subtitle D** landfill with a composite liner and constant concentration source. The flow through the composite liner is calculated using a leakage rate calculation as proposed by Giroud et. al. (1992).

### Case 2

Shows the case of **pure diffusion** with constant source and base concentrations.

### Case 3

Edits the previously entered data in Case 2 to include **advective transport and fixed outflow** in the base stratum.

### Case 4

Shows how to add a **finite mass source with leachate collection** to Case 3. Also shows how to calculate the **Reference Height of Leachate** and the **Volume of Leachate Collected**. Uses the **automatic search** for the peak concentration.

### Case 5

Illustrates use of the program to model a hydraulic trap, using essentially the same data as in Case 4.

### Case 6

This case has a 1 m thick compacted clay liner underlain by a 3 m thick **fractured till layer**. The source is **finite mass** with a **leachate collection system**, and the base is an **aquifer with fixed outflow**. Different sorption in the liner and the fractured till is also considered.

### Case 7

The lateral migration of a **radioactive contaminant** is modelled, in a **fractured porous rock** with a single set of parallel fractures. The base of the porous rock is assumed to extend to a considerable distance from the source and is represented by an **infinite thickness boundary condition**. This example illustrates the case where the default integration is not adequate. The **maximum sublayer thickness** feature is also used in this example.

Uses an **Initial Concentration Profile** in analyzing a laboratory **diffusion test for Potassium.** The specimen consists of a 4.5 cm thick clay sample with a background concentration of Potassium of 10 mg/L. In this example the Reference Height of Leachate is equal to the actual height of leachate above the sample.

### Case 9

**Freundlich non-linear sorption** is considered in analyzing a laboratory **diffusion test for Phenol.** The sample is a 7 cm thick undisturbed clay, with a 6.5 cm leachate column above for a source.

### Case 10

The Variable Properties option is used to examine time-varying advective-dispersive transport from a landfill. A landfill with a finite mass and a leachate collection system with an inward Darcy Velocity (i.e., a hydraulic trap) is considered. The leachate collection system is assumed to begin to fail after 19 years. After failure of the leachate collection system the leachate mound builds over a 10 year period, causing a reversal in the hydraulic gradient and a loss of the hydraulic trap.

### Case 11

This example demonstrates the use of a **time-varying source concentration** and **an initial concentration profile.** A landfill cell is initially filled with fresh water, and no waste is deposited for 7 years. The landfill is situated in a clay with a pore water chloride concentration, during the initial 7 years the chloride from the clay diffuses into the cell water. Between 7 and 10 years the cell is filled with waste and the chloride concentration increases linearly to 2100 mg/L. The source concentration then remains constant between 10 and 13 years. Between 13 and 15 years the source concentration decreases linearly to 1180 mg/L. The source concentration then remains constant between 15 and 19 years.

### Case 12

In this example the **results of the program are compared with an analytical solution** developed by Tang et al. (1981). The analysis is for a **single fracture system.** It is shown that the program gives exactly the same results as the analytical solution.

The results of the program are compared to the results obtained by an analytical solution given by TDAST. The TDAST program was developed by Javandel et al. (1984), and is for a 2-dimensional plane dispersion problems in an infinitely deep porous media. Concentrations obtained by both methods are in close agreement for a dispersion coefficient of  $0.01 \text{ m}^2/a$ . However, at higher dispersion coefficients, for example 5 or  $10 \text{ m}^2/a$ , the methods are not in agreement. This is because for the geometry and time frame considered in this problem, a 2-dimensional solution is required and POLLUTEv7 considers only 1-dimensional migration in the layer below the source.

### Case 14

In this example a landfill with **primary and secondary leachate collection systems** is modelled using the **Passive Sink** option. The secondary leachate collection system is simulated using a passive sink to model outflow from the collection system. The landfill contains a finite mass of a conservative species, and is underlain by an aquifer with fixed outflow.

### Case 15

The model of Case 14 is extended to incorporate **failure of the primary leachate collection system** after 20 years. This failure is modelled using the Variable Properties special feature. The use of the **Variable Properties and Passive Sink** features together is illustrated in this example.

### Case 16

This example illustrates the use of the **Monte Carlo simulation** feature, in conjunction with the **Variable Properties and Passive Sink** features. The landfill model used in Case 15 is modified to **simulate uncer-tainty in the time of failure** of the primary leachate collection system. In this example the failure time is given a triangular distribution, with a minimum of 15 years, a mode of 25 years, and a maximum of 50 years.

### Case 17

This example demonstrates how to create a landfill with a composite primary liner, primary and secondary leachate collection systems, and a compacted clay secondary liner.

A **phase change** in the secondary leachate collection system is modelled using the **Phase Change** special feature. The phase change occurs in the secondary leachate collection system at the interface between the unsaturated and saturated zones, assumed to be .2 and .1 metres thick respectively. The landfill contains a constant concentration of DCM, which experiences biological decay in the landfill, primary and secondary liners, and the aquifer.

### Case 19

In this example a **multiphase diffusion test** performed by Buss et al. (1995) is modelled. This test involved the migration of toluene from a 'constant' source through a 0.1 cm thick HDPE geomembrane, a 18.2 cm thick airspace and into a 12.3 cm water reservoir (assumed to be well mixed).

### Case 20

This example uses the same date as Case 16 for Monte Carlo simulation, except a **Sensitivity Analysis** is performed. In this example the failure time has a minimum of 15 years and a maximum of 50 years.

# Case 1: Subtitle D Landfill

### Description

This example illustrates the use of the program to model a U.S. RCRA Subtitle D landfill. The landfill consists of a composite liner and a primary leachate collection system. The composite liner is composed of a 60 mil (1.5 mm) geomembrane in good contact with a 0.9 m thick compacted clay liner. Small holes with an area of 0.1 cm<sup>2</sup> and a frequency of 1 per acre (2.5 per hectare) are assumed for the geomembrane. The method proposed by Giroud et al (1992) is used to calculate the flow (leakage) through the composite liner, these calculations are performed automatically by the program.

The landfill has a length (L) of 200 m in the direction parallel to groundwater flow in the underlying aquifer. Consideration is being given to a volatile organic contaminant with an initial source concentration of 1500  $\mu$ g/L, which is assumed to remain constant with time over the time period being examined in this example. The leachate head on the composite liner is assumed to be constant at 0.3 m. The flow in the aquifer must be established based on hydrogeologic data and is represented in terms of the horizontal Darcy velocity (the "Base Outflow Velocity") in the aquifer at the down-gradient edge of the landfill.

The parameters used for this example are listed below:

<b><u>Property</u></b>		<u>Value</u>	<u>Units</u>
Geomembrane Contact		Good	-
Geomembrane Holes		Circles	-
Hole Area		0.1	cm <sup>2</sup>
Hole Frequency		1	/acre
Source Concentration	co	1500	μg/L
Source Type		Constant	-
Landfill Length	L	200	m
Leachate Head on Liner		0.3	m
Geomembrane Thickness		60	mil
Geomembrane Diffusion Coef.		3.0x10 <sup>-5</sup>	$m^{2/a}$
Clay Thickness	H <sub>s</sub>	0.9	m
Clay Diffusion Coef.	D	0.02	m <sup>2</sup> /a
Distribution Coefficient	К <sub>d</sub>	0.5	mL/g
Soil Porosity	n	0.35	-
Dry Density		1.9	g/cm <sup>3</sup>
Aquifer Thickness	h	3.0	m
Aquifer Porosity	n <sub>b</sub>	0.3	-
Base Outflow Velocity	v <sub>b</sub>	10	m/a

For more information regarding:

- Leakage through composite liners see Giroud et al (1992).
- Diffusion through geomembranes see Hughes and Monteleone, (1987); Lord et al (1988).
- Diffusion, sorption, and effective porosity in clays (D, K<sub>d</sub>, n) see Rowe et al (1988)
- Modelling, hydrogeology, and engineering interaction see Rowe (1992), Rowe et al, 1994.
- Theory used see Rowe and Booker (1985, 1991), Rowe et al (1994).

### **Data Entry**

l

Start the POLLUTEv7 program and open the Examples project. Select Case 1 and open the model by double clicking on it in the model list. After the model is displayed, click on any layer to display the Primary Liner Landfill form below.

### **Model Parameters**

On the General tab, the title and layers present in the model are specified as shown above. In this example there is a geomembrane, clay liner and aquifer.

Primary Liner L	.andfill	_		- 14
General Source	Hydraulic Heads Geo	omembrane   Leakage	Clay Liner Aq	uifer Outflow
Title Case 1: Su	btitle D Landfill with con	stant source concentra	tion	
Coll	Waste lection System eomembrane Clay Liner	R	Geomembrane C No Clay Liner C No Aquitard	
	Aquitard		No     Aquifer     No     Units     Metric	© Yes © Yes
	🗸 ОК	🗙 Cancel	? Help	

On the Source tab shown on the next page, the Source Type, Source Concentration and Landfill Length are specified. In this example, the source type is constant concentration. If the source type was finite mass additional information for the source would need to be entered as discussed in Case 4.

#### Case 1: Subtitle D Landfill with Constant Concentration

Primary Liner Landfill
General Source Hydraulic Heads Geomembrane Leakage Clay Liner Aquifer Outflow
Concentration 1500 µg/L
Landfill Length 200 m
Source Type
Constant Concentration
V OK X Cancel ? Help

The Hydraulic Heads tab, shown below, is used to specify the leachate head on the primary liner and the groundwater level relative to the top of the aquifer. These heads are used to calculate the Darcy velocity through the liner.

Pri	imary Liner Landfill	
Ge	eneral Source Hydraulic Heads Geomembrane Leakage Clay Liner Aquifer Outflow	
	Leachate Head on Primary Liner 0.3 m	
	Groundwater level relative to top of Aquifer 0 m	
	V OK X Cancel ? Help	

#### Case 1: Subtitle D Landfill with Constant Concentration

On the Geomembrane tab shown below, the Name, Thickness, Diffusion Coefficient, Phase Parameter, and method to calculate the leakage through the geomembrane is specified. If the method is Rowe et. al. 2004 or Giroud & Bonaparte 1992, an additional tab will be displayed to enter the hole parameters. If the method is equivalent K, then the Hydraulic Conductivity of the geomembrane can be entered on this tab. In this example the leakage method used is Giroud & Bonaparte 1992.

Primary Liner Landfill	
General Source Hydraulic Heads Geomembrane Leakag	ge   Clay Liner   Aquifer   Outflow
Name: Geomembrane	Leakage Method
Change Symbol	C LEAK, Rowe et al 2004
Thickness 60 mil 💌	Giroud & Bonaparte 1992
Diffusion Coef 3E-5 m2/a	C Equivalent K
Phase Parameter 1	
ØK K Cancel	? Help

The parameters for the holes in the geomembrane are specified on the Leakage tab shown on the next page. These parameters include the Type of Contact, Hole Type, Use of Permeation, and Hole Frequency. If the type of holes is Circles then the Hole Area can be specified, if the type is Long then the Hole Length and Width can be specified.

At the bottom of the tab, the Calculate Leakage button can be used to calculate and display the Darcy velocity (leakage) through the primary liner .In this example the calculated Darcy velocity is  $3.929 \times 10^{-5}$  m/a

Primary Liner Landfill	6
General Source Hydraulic Heads	Geomembrane Leakage Clay Liner Aquifer Outflow
	Giroud & Bonaparte, 1992
Contact Good C Poor	Hole Frequency 1 acre
-Hole Tupe	Hole Area 0.1 v
Circle C Long	
Permeation C Yes ⓒ No	
Calculate Le	akage Darcy Velocity 3.929E-5 m/a
O	K Cancel ? Help

The Clay Liner tab below is used to specify the properties of the clay liner below the geomembrane. These properties include the Name, Symbol, Thickness, Density, Hydraulic Conductivity, Diffusion Coefficient, Distribution Coefficient, and Porosity.

Primary Liner Landfill		
General Source Hydraulic Heads Geomembrane Leakage Clay Liner Aquifer Outflow		
Name: Clay Linet Change Symbol		
Thickness 0.9		
Density 1.9 g/cm3 -		
Conductivity K 1E-7 cm/s		
Diffusion Coef 0.02 m2/a		
Distr. Coef 0.5 mL/g 💌		
Porosity 0.35		
V OK X Cancel ? Help		

#### Case 1: Subtitle D Landfill with Constant Concentration

Primary Liner Landfill	
General   Source   Hydraulic Heads   Geomembrane   Leakage   Clay Liner Aquife	Outflow
Name: Aquifer Change:	Symbol
Thickness 🖻 🦷 💌	
Porosity 0.3	
V DK X Cancel ? Help	

The Aquifer tab, shown below, is used to specify the Name, Symbol, Thickness and Porosity of the Aquifer.

The last tab is used to specify the Outflow Rate in the Aquifer. This rate should be at greater than or equal to the minimum calculated by the program. In this example, the minimum is 0.00262 m/a.

Primary Liner Landfill
General Source Hydraulic Heads Geomembrane Leakage Clay Liner Aquifer Outflow
Outflow in Aquifer The minimum outflow velocity in the Aquifer that will fulfill the conditions of continuity of flow is: 0.00262 m/a
Outflow Velocity
Calculated Results
Darcy Velocity 3.929E-5 m/a
Leachate Head on Primary Liner 0.3 m
Cancel ? Help

### **Run Parameters**

To set the times and depths to calculate the concentrations, select the Run Parameters menu item from the Data Entry menu. The Run Parameters form below will be displayed. The Type tab is used to specify the Type of Output and the units for the output. The concentrations can either be calculated at specified times or the time of the maximum concentration can be found.

Run Pa	arameters
Туре	Concentrations at Specified Times
	Type of Output Concentrations at Specified Times Maximum Concentrations
	Time Units: yr
	Depth Units: M
	Concentration Units: µg/L
[	Cancel ? Help

The Concentrations at Specified Times tab is used to specify the times and depths to calculate the concentrations.

Run Parameters
Type Concentrations at Specified Times
Times
Number of Times: 3
Number: 1 (
Time: 10 yr
All Depths
Yes
C No
Cancel ? Help

### **Model Execution**

To run the model and calculate the concentrations either select the Run menu item from the Execute menu or press the Run button on the toolbar.

### **Model Output**

After the model has been executed, the output for the model will be displayed. The initial display will depend on your settings in the program's preferences.

### **Concentration vs Depth**

The Concentration vs. Depth chart below can be displayed by pressing the Concentration vs Depth button on the Output toolbar or selecting the Concentration vs Depth menu item from the Output menu.



### **Output Listing**

To display the output as a text listing that will show the calculated concentrations as numbers, select the List Output menu item from the Output menu or press the Output Listing button on the Output toolbar.

#### Case 1: Subtitle D Landfill with constant source concentration

#### THE DARCY VELOCITY (Flux) THROUGH THE LAYERS Va = 3.929E-5 m/a

#### Layer Properties

Layer	Thickness	Number of Sublayers	Coefficient of Hydrodynamic Dispersion	Matrix Porosity	Distributon Coefficient	Dry Density
Geomembrane Clay Liner	60 mil 0.9 m T	1 10	3E-5 m2/a 0.02 m2/a	- 1 0.35	. 0 cm3/g 0.5 mL/g	950 kg/m3 1 1.9 g/cm3

#### **Boundary Conditions**

#### Contant Concentration

Source Concentration = 1500 µg/L

#### Fixed Outflow Bottom Boundary Landfill Length = 200 m Landfill Width = 1 m Base Thickness = 3 m Base Porosity = 0.3 Base Outflow Velocity = 10 m/a

#### Laplace Transform Parameters

**TAU** = 7 **N** = 20 **SIG** = 0 **RNU** = 2

#### Calculated Concentrations at Selected Times and Depths

Time	Depth	Concentration	
yr	m	μg/L	
10	0.000E+00	1.500E+03	

	1.524E-03 9.152E-02 1.815E-01 2.715E-01 3.615E-01 4.515E-01 6.315E-01 6.315E-01 7.215E-01 8.115E-01 9.015E-01	6.823E+02 4.917E+02 3.370E+02 2.190E+02 1.345E+02 7.798E+01 4.254E+01 2.176E+01 1.028E+01 4.107E+00 3.970E-01
20	0.000E+00 1.524E-03 9.152E-02 1.815E-01 2.715E-01 3.615E-01 4.515E-01 5.415E-01 6.315E-01 6.315E-01 8.115E-01 9.015E-01	1.500E+03 8.259E+02 6.636E+02 3.966E+02 2.942E+02 2.117E+02 1.471E+02 9.768E+01 6.006E+01 3.082E+01 6.430E+00
30	0.000E+00 1.524E-03 9.152E-02 1.815E-01 2.715E-01 3.615E-01 4.515E-01 5.415E-01 6.315E-01 7.215E-01 8.115E-01 9.015E-01	1.500E+03 9.082E+02 7.636E+02 6.309E+02 5.115E+02 4.062E+02 3.148E+02 2.365E+02 1.698E+02 1.698E+02 1.126E+02 6.246E+01 1.675E+01

#### NOTICE

Although this program has been tested and experience would indicate that it is accurate within the limits given by the assumptions of the theory used, we make no warranty as to workability of this software or any other

÷

# Case 2: Pure Diffusion

### Description

This example illustrates the use of the program for the simple case of pure diffusion of a conservative species (i.e., no sorption). The hydrogeology is comprised of a 4 m thick layer with a constant contaminant concentration source at the top, and an underlying aquifer at the base. There is a sufficiently high flushing velocity in the aquifer that the concentration at the bottom of the layer can be assumed to be zero and the aquifer is not explicitly modelled. The following parameters are assumed for the example:

<b>Property</b>		<u>Value</u>	<u>Units</u>
Darcy Velocity	va	0.0	m/a
Diffusion Coefficient	D	0.01	m <sup>2</sup> /a
Distribution Coefficient	К <sub>d</sub>	0.0	$cm^{3/g}$
Soil Porosity	n	0.4	-
Dry Density		1.5	g/cm <sup>3</sup>
Soil Layer Thickness	Н	4.0	m
Number of Sub-layers		4	-
Source Concentration	c <sub>o</sub>	1.0	g/L
Base Concentration	с <sub>b</sub>	0.0	g/L
Times of Interest	t	10, 50, 100	а
		150, 200	а

### **Data Entry**

Start the POLLUTEv7 program and open the Examples project. Select Case 2 and open the model by double clicking on it in the model list. After the model is displayed, the data for the model can be displayed and edited using the Data Entry menu or by clicking on that part of the model.

### **General Data**

To edit the general model data either click on the title or select the General Data menu item from the Data Entry menu. On the General Data form on the next page the Title, Number of Layers, Maximum Depth, Darcy velocity, and Laplace Transform parameters can be specified. In this example there will only be one layer and since it is for diffusion only the Darcy velocity is zero.

1



### Layer Data

The data for the layer can be specified by either clicking on the layer or by selecting the Layer Data menu item from the Data Entry menu. On the Layer Data form shown below, the data and symbol for the layer can be specified. In this example, the diffusion coefficient of 0.01 is specified for the layer.

Layer Data 🦒			
La	ayer Number 1		
Layer Data Layer Symbol			
Name: Aquitard			
Number of Sub Layers 4		Fractures	
Thickness 4	m 💌	None	
Dry Density 1.5	g/cm3 💌	C 1 Dimensional	
Porosity 0.4		C 2 Dimensional	
Coef of Hydro Disp 0.01	cm3/g 💌	C 3 Dimensional	
Distribution Coef	m2/a 💌		
🗸 ОК	🗙 Cancel	? <u>H</u> elp	

### **Boundary Conditions**

The boundary conditions for the model can be specified by either clicking on the top or bottom boundary or selecting the Boundary Conditions menu item from the Data Entry menu. On the Boundary Conditions form below the top and bottom boundary conditions can be specified. In this example, the top boundary has a constant concentration of 1 and the bottom boundary has a constant concentration of 0.

Boundary Conditions		
Boundary Conditions   Top - Constant (	Conc. Bottom - Constant Conc.	
Top Boygdary	Zero Flux     Constant Concentration     Finite Mass	
Bottom Boundary	<ul> <li>Zero Flux</li> <li>Constant Conc</li> <li>Fixed Outflow Velocity</li> <li>Infinite Thickness</li> </ul>	
<u> </u>	X Cancel ? Help	

#### **Run Parameters**

To set the times and depths to calculate the concentrations, select the Run Parameters menu item from the Data Entry menu. The Run Parameters form is the same as shown in Case 1. In this example, the concentrations will be calculated at 5 times: 10, 50, 100, 150, and 200 years.

### **Model Execution**

To run the model and calculate the concentrations either select the Run menu item from the Execute menu or press the Run button on the toolbar.

### **Model Output**

After the model has been executed, the output for the model will be displayed. The initial display will depend on your settings in the program's preferences.

### **Concentration vs Depth**

The Concentration vs. Depth chart below can be displayed by pressing the Concentration vs Depth button on the Output toolbar or selecting the Concentration vs Depth menu item from the Output menu.



### **Output Listing**

To display the output as a text listing that will show the calculated concentrations as numbers, select the List Output menu item from the Output menu or press the Output Listing button on the Output toolbar.

#### Case 2: Pure diffusion - specified surface and base concentrations

THE DARCY VELOCITY (Flux) THROUGH THE LAYERS Va = 0 m/year

#### Layer Properties

Layer	Thickness	Number of Sublayers	Coefficient of Hydrodynamic Dispersion	Matrix Porosity	Distributon Coefficient	Dry Density
Aquitard	4 m	4	0.01 cm3/g	0.4	0 m2/a	- 1.5 g/cm3 =

#### **Boundary Conditions**

#### **Contant Concentration**

Source Concentration = 1 mg/L

#### **Contant Concentration Bottom Boundary**

Base Concentration = 0 mg/L

#### Laplace Transform Parameters

**TAU =** 7 **N =** 20 **SIG =** 0 **RNU =** 2

#### Calculated Concentrations at Selected Times and Depths

Time	Depth	Concentration
yr	, m	_ mg/L
10	. 0.000E+00	1.000E+00
	1.000E+00	2.535E-02
	. 2.000E+00	7.744E-06
	. 3.000E+00	2.011E-11
	4.000E+00	0.000E+00

50	0.000E+00 1.000E+00 2.000E+00 3.000E+00 4.000E+00	1.000E+00 3.173E-01 4.550E-02 2.699E-03 0.000E+00
100	0.000E+00 1.000E+00 2.000E+00 3.000E+00 4.000E+00	1.000E+00 4.795E-01 1.573E-01 3.349E-02 0.000E+00
150 ◀	0.000E+00 1.000E+00 2.000E+00 3.000E+00 4.000E+00	1.000E+00 5.636E-01 2.477E-01 7.937E-02 0.000E+00
200	0.000E+00 1.000E+00 2.000E+00 3.000E+00 4.000E+00	1.000E+00 6.166E-01 3.146E-01 1.212E-01 0.000E+00

#### NOTICE

Although this program has been tested and experience would indicate that it is accurate within the limits given by the assumptions of the theory used, we make no warranty as to workability of this software or any other licensed material. No warranties either expressed or implied (including warranties of fitness) shall apply. No responsibility is assumed for any errors, mistakes or misrepresentations that may occur from the use of this computer program. The user accepts full responsibility for assessing the validity and applicability of the results obtained with this program for any specific case.

# **Case 3: Advective Diffusive Transport**

### Description

In this example the input data file from Case 2 will be edited to include advective transport and a permeable base stratum (aquifer) with a fixed outflow. The hydrogeology is comprised of a 4 m thick aquitard layer with a constant contaminant concentration in the landfill source at the top, and a 20 m thick underlying aquifer at the base.

Although the aquifer is 20 m thick it is generally unrealistic to model dilution (mixing) of contaminant through the full thickness. The actual thickness that should be modelled depends on the hydrogeologic conditions, the length of monitoring screens, and the local regulations. In this example dilution (mixing) of the contaminant will only be considered in the upper 3m of the aquifer, and hence the aquifer thickness used is h = 3 m.

Since the aquifer (i.e., the contaminant receptor) is being modelled as a boundary condition the actual deposit thickness that is explicitly modelled is the 4 m thick aquitard, and the concentration given in the output at the 4 m depth is the concentration in the upper 3 m of the aquifer. It is assumed that this is uniformly distributed in the 3 m and that no contaminant moved lower than 3 m into the aquifer (if the aquifer thickness, h, were to be increased, the concentration in the aquifer would drop).

In the underlying aquifer the inflow of water beneath the up gradient edge of the landfill is given by a Darcy velocity of 20 m/a.

The "base velocity" is the outflow velocity beneath the down-gradient edge of the landfill and corresponds to the inflow velocity (20 m/a) at the up gradient edge plus the inflow from the landfill.

Based on continuity of flow the initial flow in the aquifer,  $q_{in}$ , is given by the inflow velocity ( $v_{in} = 20$  m/a in this example) multiplied by the thickness of the aquifer being considered (h = 3 m in this example) and the width of the landfill (the landfill dimension perpendicular to the direction of groundwater flow, W = 300 m in this example), thus:

$$q_{in} = v_{in} * h * W = 20 * 3 * 300 = 18000 \text{ m}^2/\text{a}$$

The flow into the aquifer from the landfill,  $q_a$ , is the downward Darcy velocity ( $v_a = 0.1$  m/a in this case) multiplied by the length (L = 200 m) and width (W = 300 m) of the landfill, thus:

$$q_a = v_a * L * W = 0.1 * 200 * 300 = 6000 \text{ m}^3/\text{a}$$

Hence the outflow at the down-gradient edge of the landfill is:

$$q_{out} = q_{in} + q_a = 18000 + 6000 = 24000 \text{ m}^3/a$$

And the "Base Outflow Velocity",  $v_b$ , is the outflow divided by the width of the landfill (W = 300 m) and the thickness of the aquifer being considered (h = 3 m), therefore:

 $v_{h} = q_{out} / (W * h) = 24000 / (3 * 300) = 26.67 m/a$ 

The following parameter are assumed for the example:

<u>Property</u>		<u>Value</u>	<u>Units</u>
Darcy Velocity	va	0.1	m/a
Diffusion Coefficient	D	0.01	m <sup>2</sup> /a
Distribution CoefficientK <sub>d</sub>		0.0	$cm^3/g$
Soil Porosity	n	0.4	-
Dry Density		1.5	g/cm <sup>3</sup>
Soil Layer Thickness	Н	4.0	m
Number of Sub-layers		4	-
Source Concentration	co	1.0	g/L
Landfill Length	L	200.0	m
Landfill Width	W	300.0	m
Thickness of Aquifer	h	3.0	m
Porosity of Aquifer	nb	0.3	-
Base Outflow Velocity	v <sub>b</sub>	26.67	m/a
Times of Interest	t	10, 50, 100	а
		150, 200	а

The landfill length (L) is measured in the direction parallel to groundwater flow. And the landfill width (W) is the direction perpendicular to groundwater flow, since this is not a 3D analysis this parameter has no effect on the results.

Warning: The evaluation of the base flow velocity,  $v_b$ , requires consideration of the local hydrogeology and the potential effect of the proposed landfill on flow conditions. For some situations, the aquitard has sufficiently low hydraulic conductivity and the aquifer has sufficiently high transmissivity that simple hand continuity calculations as indicated above are appropriate. In other cases some more sophisticated flow models may be required. The parameters used in any modelling should be selected by a hydrogeologist/engineer with sufficient knowledge and experience to understand the existing flow system and the flow system that is likely to exist after the landfill construction.

#### **Case 3: Advective Diffusive Transport**

Note: The concentration at 4 m is the concentration at the bottom of the aquitard and in the 3 m thick aquifer part of the aquifer beneath the landfill. This example was selected to have a downward flow ( $v_a = 0.1 \text{ m/a}$ ) so large that advection controls and in fact for the constant source boundary condition it is possible to calculate the peak impact in the aquifer from a simple hand calculation, viz.

 $c_{max} = q_a * c_o / q_{out} = 6000 * 1 / 24000 = 0.25 g/L$ 

[As an exercise the user may wish to repeat the calculation for  $v_a = 0.005$  m/a,  $v_b = 20.34$  m/a. Based on the simple hand calculation above, this would give  $c_{max} = 0.0164$  g/L = 16.4 mg/L.]

### Data Entry

Start the POLLUTEv7 program and open the Examples project. Select Case 3 and open the model by double clicking on it in the model list. After the model is displayed, the data for the model can be displayed and edited using the Data Entry menu or by clicking on that part of the model.

### **General Data**

To edit the Darcy velocity either click on the title or select the General Data menu item from the Data Entry menu. On the General Data form below the Darcy velocity of 0.1 m/a can be specified.

General Data
Title: Case 3: Advective diffusive transport, Constant source, Base aquifer
Number of Layers: 1 Maximum Depth: 7 m 💌
Darcy Velocity: 0.1
Laplace Transform Parameters
TAU: 7 N: 20 SIG: 0 RNU: 2
✓ OK X Cancel ? Help

### Layer Data

The layer data for this model is the same as that in Case 2.

L

### **Boundary Conditions**

The boundary conditions for the model can be specified by either clicking on the top or bottom boundary or selecting the Boundary Conditions menu item from the Data Entry menu. In this example, the top boundary has a constant concentration of 1 and the bottom boundary is represented as an aquifer with a fixed outflow velocity as shown on the Boundary Condition form below.

Boundary Conditions	
Boundary Conditions	Top - Constant Conc.
Bottom - Fixed Outflow	Fixed Outflow Symbol
Landfill Length: 201	m 💌
Landfill Width: 300	m
Base Thickness: 3	m
Base Porosity: 0.3	_
Base Outflow Velocity: 26.67	m/a 💌
	Cancel ? Help

### **Run Parameters**

The run parameters for this model is the same as that in Case 2.

### **Model Execution**

To run the model and calculate the concentrations either select the Run menu item from the Execute menu or press the Run button on the toolbar.

### **Model Output**

After the model has been executed, the output for the model will be displayed. The initial display will depend on your settings in the program's preferences.

### **Concentration vs Time**

The Concentration vs. Time chart below can be displayed by pressing the Concentration vs Time button on the Output toolbar or selecting the Concentration vs Time menu item from the Output menu.



### **Output Listing**

To display the output as a text listing that will show the calculated concentrations as numbers, select the List Output menu item from the Output menu or press the Output Listing button on the Output toolbar.

#### Case 3: Advective diffusive transport, Constant source, Base aquifer

#### THE DARCY VELOCITY (Flux) THROUGH THE LAYERS Va = 0.1 m/year

#### Layer Properties

Layer	Thickness	Number of Sublayers	Coefficient of Hydrodynamic Dispersion	Matrix Porosity	Distributon Coefficient	Dry Density
Aquitard	4 m	4	0.01 cm3/g	0.4	0 m2/a	; 1.5 g/cm3

#### **Boundary Conditions**

#### Contant Concentration

Source Concentration = 1 mg/L

#### Fixed Outflow Bottom Boundary

Landfill Length = 200 m Landfill Width = 300 m Base Thickness = 3 m Base Porosity = 0.3 Base Outflow Velocity = 26.67 m/a

#### Laplace Transform Parameters

**TAU =** 7 **N =** 20 **SIG =** 0 **RNU =** 2

#### Calculated Concentrations at Selected Times and Depths

Time	Depth	Concentration	
yr	m	mg/L	
5	0.000E+00	1.000E+00	
	1.000E+00	8.257E-01	

	2.000E+00 3.000E+00 4.000E+00	1.116E-02 2.255E-08 6.655E-11
10 I	0.000E+00 1.000E+00 2.000E+00 3.000E+00 4.000E+00	1.000E+00 1 9.998E-01 8.892E-01 1.490E-01 2.805E-05
15	1 0.000E+00 1.000E+00 2.000E+00 3.000E+00 4.000E+00	1.000E+00 1.000E+00 9.996E-01 9.271E-01 4.101E-02
20	0.000E+00 1.000E+00 2.000E+00 3.000E+00 4.000E+00	1.000E+00 1.000E+00 1.000E+00 9.994E-01 1.930E-01
25	0.000E+00 1.000E+00 2.000E+00 3.000E+00 4.000E+00	1.000E+00 1.000E+00 1.000E+00 1.000E+00 2.426E-01
30	0.000E+00 1.000E+00 2.000E+00 3.000E+00 4.000E+00	1.000E+00 1.000E+00 1.000E+00 1.000E+00 2.491E-01
50	0.000E+00 1.000E+00 2.000E+00 3.000E+00 4.000E+00	1.000E+00 1.000E+00 1.000E+00 1.000E+00 2.500E-01
100	0.000E+00 1.000E+00 2.000E+00 3.000E+00 4.000E+00	1.000E+00 1.000E+00 1.000E+00 1.000E+00 2.500E-01

## Case 4: Finite Mass Source

### Description

In this example the input data file from Case 3 will be edited to include a source with a finite mass of waste and a leachate collection system. The hydrogeology is comprised of a 4 m thick layer with a finite mass source at the top, and an underlying aquifer at the base with fixed outflow as discussed in Case 3. All of the parameters are the same as in Case 3, except the vertical Darcy velocity will be 0.03 m/a, the horizontal inflow velocity will be 4 m/a and there will be a finite mass top boundary condition. The finite mass top boundary condition requires the input of the Reference Height of Leachate ( $H_r$ ), Rate of Increase in Concentration ( $C_r$ ), and the Volume of Leachate Collected ( $Q_c$ ).

It is assumed in this example that the waste has an average thickness of 6.25 m and a density of 600 kg/m<sup>3</sup>, and that chloride represents 0.2% of the total mass of the waste. Thus, the total mass of chloride per unit area of the landfill ( $m_{tc}$ ) is calculated by multiplying the proportion of chloride by the density of the waste and the thickness of the waste.

i.e. 
$$m_{tc} = 0.002 * 600 * 6.25 \text{ kg/m}^2$$

A peak concentration ( $c_0$ ) for chloride of 1000 mg/L (i..e., 1 kg/m<sup>3</sup>) is assumed. The Reference Height of Leachate is then:

$$H_r = m_{tc} / c_0 = 0.002 * 600 * 6.25 / 1 = 7.5 m$$

If the peak concentration is reached relatively early in the life of the landfill and the analysis starts at this time, then there will be no increase in concentration with time. The Rate of Increase in Concentration  $(C_r)$  would then be zero.

The Volume of Leachate ( $Q_c$ ) collected is equal to the difference between the infiltration through the cover ( $q_0 = 0.3 \text{ m/a here}$ ) and the exfiltration through the base ( $v_a = 0.03 \text{ m/a here}$ ), and is given by:

$$Q_r = q_0 - v_a = 0.3 - 0.3 = 0.27 \text{ m/a}$$

In this example the inflow in the aquifer at the up gradient edge of the landfill will be 4 m/a and the outflow at the down gradient edge  $(v_b)$  is then:

$$v_{h} = (v_{h}(in)*h*W + v_{a}*L*W)/(h*W) = v_{a}(in) + v_{a}*L/h = 4 + 0.03*200/3 = 6 m/a$$

The following parameters	are assumed	for the example:
--------------------------	-------------	------------------

<b><u>Property</u></b>		<u>Value</u>	<u>Units</u>
Darcy Velocity	va	0.03	m/a
Diffusion Coefficient	D	0.01	m <sup>2</sup> /a
Distribution CoefficientKd		0.0	$cm^{3}/g$
Soil Porosity	n	0.4	-
Dry Density		1.5	g/cm <sup>3</sup>
Soil Layer Thickness	Н	4.0	m
Number of Sub-layers		4	-
Source Concentration	c <sub>o</sub>	1000.0	mg/L
Rate of Increase in c <sub>o</sub>	c <sub>r</sub>	0.0	mg/L/a
Ref. Height of Leachate H <sub>r</sub>		7.5	m
Volume Collected	Q <sub>c</sub>	0.27	m/a
Landfill Length	L	200.0	m
Landfill Width	W	300.0	m
Thickness of Aquifer	h	3.0	m
Porosity of Aquifer	nb	0.3	-
Base Outflow Velocity	v <sub>b</sub>	6.0	m/a
Upper and Lower Time Limit	ts	25, 400	а

The landfill length is measured in the direction parallel to groundwater flow. And the landfill width is the direction perpendicular to groundwater flow, since this is not a 3D analysis this parameter has no effect on the results.

### **Data Entry**

Start the POLLUTEv7 program and open the Examples project. Select Case 4 and open the model by double clicking on it in the model list. After the model is displayed, the data for the model can be displayed and edited using the Data Entry menu or by clicking on that part of the model.

### **General Data**

The general data for this example is the same as in Case 3, except for the Darcy velocity. To edit the Darcy velocity either click on the title or select the General Data menu item from the Data Entry menu. On the General Data form below the Darcy velocity of 0.03 m/a can be specified.

1

General Data
Title: Case 4: Finite mass, leachate collection, base aquifer
Number of Layers: 1 Maximum Depth: 7 m
Darcy Velocity: 0.03 m/year 💌
Laplace Transform Parameters
TAU: 7 N: 20 SIG: 0 RNU: 2
✓ OK Cancel ? Help

### Layer Data

The layer data for this model is the same as that in Case 3.

### **Boundary Conditions**

The boundary conditions for the model are the can be specified by either clicking on the top or bottom boundary or selecting the Boundary Conditions menu item from the Data Entry menu. In this example, the top boundary has a finite mass and the bottom boundary is represented as an aquifer with a fixed outflow velocity as shown on the Boundary Condition forms below.

Boundary Conditions								
Boundary Conditions	Top - Finite Mass	Bottom - Fixed O	utflow Fixed Outflow Symbol					
Specify								
Initial	Source Concentratior	r: 1000	mg/L 💌					
Rat	e of Increase in Conc	: 0	mg/L/yr 👻					
Volume (	of Leachate Collected	t 0.27	m/a 🔻					
and either								
	Thickness of Wase	x 0	m 💌					
	Waste Density	e  0	kg/m3 👻					
	Proportion of Mass	: 0						
Volu	imetric Water Conten	: 0						
Con	version Rate Half Life	x 0	year 💌					
or Bi	ef Height of Leachate	x 7.5	m					
	<u>o</u> k >	Cancel	? <u>H</u> elp					

Boundary Conditions
Boundary Conditions   Top - Finite Mass Bottom - Fixed Outflow   Fixed Outflow Symbol
Landfill Length: 200 m
Landfill Width: 300 m 💌
Base Thickness: 3 m
Base Porosity: 0.3
Base Outflow Velocity: 6 m/a 💌
✓ <u>D</u> K X Cancel ? Help

### **Run Parameters**

The run parameters for this model can be specified by selecting the Run menu item from the Execute menu or pressing the Run button on the toolbar. In this example the automatic search for the peak base concentration option is going to be used. The search depth will be 4 m (the bottom of the layer) and the lower and upper time limits will be 25 and 400 years.

Run Parameters 🗼
Type Maximum Concentrations
Search Depth: 4 m Accuracy (%): 0.1 Number of Iterations: 25
Lower Time Limit: 25 yr 💽 Upper Time Limit: 400 yr 💽
All Depths Yes No
Cancel ? Help

Provided the initial estimate for these time limits are reasonable the program will find the maximum even if it lies outside these limits. The default values for the Accuracy and Maximum number of Search Attempts should prove sufficient for this *example and most other problems*.

### **Model Execution**

To run the model and calculate the concentrations either select the Run menu item from the Execute menu or press the Run button on the toolbar.

### **Model Output**

After the model has been executed, the output for the model will be displayed. The initial display will depend on your settings in the program's preferences.



### **Concentration vs Depth**

The Concentration vs. Depth chart on the previous page can be displayed by pressing the Concentration vs Depth button on the Output toolbar or selecting the Concentration vs Depth menu item from the Output menu.

### **Output Listing**

To display the output as a text listing that will show the calculated concentrations as numbers, select the List Output menu item from the Output menu or press the Output Listing button on the Output toolbar. *The maximum concentration in the aquifer in this example is 136 mg/L. This peak occurs at 70 years.* 

#### Case 4: Finite mass, leachate collection, base aquifer

THE DARCY VELOCITY (Flux) THROUGH THE LAYERS Va = 0.03 m/year

#### Layer Properties

Layer	Thickness	Number of Sublayers	Coefficient of Hydrodynamic Dispersion	Matrix Porosity	Distributon Coefficient	Dry Density
Aquitard	4 m	4	0.01 cm3/g	0.4	0 m2/a	1.5 g/cm3

#### **Boundary Conditions**

#### Finite Mass Top Boundary

Initial Concentration = 1000 mg/L Rate of Increase = 0 mg/L/yr Volume of Leachate Collected = 0.27 m/a Thickness of Waste = 0 m Waste Density = 0 kg/m3 Proportion of Mass = 0 Volumetric Water Content = 0 Conversion Rate Half Life = 0 year Reference Height of Leachate = 7.5 m

#### Fixed Outflow Bottom Boundary

Landfill Length = 200 m Landfill Width = 300 m Base Thickness = 3 m Base Porosity = 0.3 Base Outflow Velocity = 6 m/a

#### Laplace Transform Parameters

#### Maximum Base Concentration Parameters

Depth to Search = 4 m Lower Time Limit = 25 yr Upper Time Limit = 400 yr Base Concentration Accuracy = 0.1 Maximum Search Attempts = 25

Ι

Maximum Base Concentration and Time of Occurrence

Time	Depth	Concentration	Preceeding	Preceeding	Exceeding	Exceeding
yr	m	mg/L	Time	Concentration	Time	Concentration
7.0233E+01	0.0000E+00	6.1040E+01				
	1.0000E+00	1.0820E+02				
	2.0000E+00	1.8998E+02				
	3.0000E+00	3.1335E+02				
	4.0000E+00	1.3589E+02	6.8517E+01	1.3550E+02	7.1949E+01	1.3548E+02

Number of Search Attempts = 5

#### NOTICE

Although this program has been tested and experience would indicate that it is accurate within the limits given by the assumptions of the theory used, we make no warranty as to workability of this software or any other licensed material. No warranties either expressed or implied (including warranties of fitness) shall apply. No responsibility is assumed for any errors, mistakes or misrepresentations that may occur from the use of this computer program. The user accepts full responsibility for assessing the validity and applicability of the results obtained with this program for any specific case.
# Case 5: Hydraulic Trap - Finite Mass Source

# Description

This illustrates the use of the program for the case where there is a hydraulic trap (i.e., flow is into the land-fill). The parameters are essentially the same as in Case 4, (where there was a finite mass source with a leachate collection system and a fixed outflow base) except that the Darcy velocity has been changed and the base aquifer is now assumed to be only 1 m thick with a porosity of 0.35 and is underlain by a low permeability layer. We also now choose to ignore the width of the landfill and take W = 1 m. This is the same as modelling a 1 m strip through the landfill. This width, W, has no effect on the results.

The calculation and values for the Reference Height of Leachate is the same as in Case 4. Again it is assumed that the average infiltration through the cover,  $(q_0)$  is 0.3 m/a. For this example the Darcy velocity  $(v_a)$  into the base of the landfill is assumed to be -0.001 m/a. The negative value for the Darcy velocity implies that the flow is upward. Neglecting the small volume of groundwater collected the average Volume of Leachate Collected  $(Q_c)$  is:

$$Q_{c} = q_{0} = 0.3 \text{ m/a}$$

In this example the inflow in the aquifer at the up gradient edge of the landfill will be 4 m/a and the outflow at the down gradient edge  $(v_h)$  is then:

 $v_{b} = v_{b}(in) + v_{a}*L/h = 4 - 200*0.001 = 3.8 m/a$ 

The following parameters are assumed for the example:

<b>Property</b>		<u>Value</u>	<u>Units</u>
Darcy Velocity	va	-0.001	m/a
Diffusion Coefficient	D	0.01	m <sup>2</sup> /a
Distribution CoefficientK		0.0	cm <sup>3</sup> /g
Soil Porosity	n	0.4	-
Dry Density		1.5	g/cm <sup>3</sup>
Soil Layer Thickness	Η	4.0	m
Number of Sub-layers		4	-
Source Concentration	c <sub>o</sub>	1000.0	mg/L
Rate of Increase in co	c <sub>r</sub>	0.0	mg/L/a
Ref. Height of Leachate	H <sub>r</sub>	7.5	m
Volume Collected	Qc	0.3	m/a
Landfill Length	L	200.0	m

## Case 5: Hydraulic Trap - Finite Mass Source

Landfill Width	W	1.0	m
Thickness of Aquifer	h	1.0	m
Porosity of Aquifer	n <sub>b</sub>	0.35	-

# **Data Entry**

Start the POLLUTEv7 program and open the Examples project. Select Case 5 and open the model by double clicking on it in the model list. After the model is displayed, the data for the model can be displayed and edited using the Data Entry menu or by clicking on that part of the model.

## **General Data**

The general data for this example is the same as in Case 4, except for the Darcy velocity. To edit the Darcy velocity either click on the title or select the General Data menu item from the Data Entry menu. On the General Data form below the Darcy velocity of -0.001 m/a can be specified.

General Data
Title Case E. Lindentie tran Einite mars langhate collection have an iter
Title: Toase 3. Hydraulic trap, Finite mass, leachate collection, base aquiler
Number of Layers: 1 Maximum Depth: 5 m 💌
Darcy Velocity: 0.001 m/year
Laplace Transform Parameters
TAU: 7 N: 20 SIG: 0 RNU: 2
✓ OK X Cancel ? Help

# Layer Data

The layer data for this model is the same as that in Case 4.

1

## **Boundary Conditions**

The boundary conditions for the model can be specified by either clicking on the top or bottom boundary or selecting the Boundary Conditions menu item from the Data Entry menu. In this example, the top boundary has a finite mass and the bottom boundary is represented as an aquifer with a fixed outflow velocity as shown on the Boundary Condition forms below.

Boundary Conditi			
Boundary Conditions	Top - Finite Mass B	ottom - Fixed O	utflow Fixed Outflow Symbol
Specify			
Initial	Source Concentration:	1000	mg/L 👻
Rat	e of Increase in Conc:	0	mg/L/yr ▼
Volume o	of Leachate Collected:	0.3	m/a 🔻
and either			
	Thickness of Wase:	0	m 💌
	Waste Density:	0	kg/m3 ▼
	Proportion of Mass:	0	
Volu	metric Water Content:	0	
Con	version Rate Half Life:	0	year 💌
B	ef Height of Leachate:	7.5	m
	<u>o</u> k 🗙	Cancel	? <u>H</u> elp

Boundary Conditions
Boundary Conditions   Top - Finite Mass   Bottom - Fixed Outflow   Fixed Outflow Symbol
Landfill Length: 200 m
Landfill Width: 1 m
Base Thickness: 1
Base Porosity: 0.35
Base Dutflow Velocity: 3.8 m/a
✓ OK K Cancel ? Help

## **Run Parameters**

The run parameters for this model are the same as in Case 4.

# **Model Execution**

To run the model and calculate the concentrations either select the Run menu item from the Execute menu or press the Run button on the toolbar.

# **Model Output**

After the model has been executed, the output for the model will be displayed. The initial display will depend on your settings in the program's preferences.



## **Concentration vs Depth**

The Concentration vs. Depth chart on the previous can be displayed by pressing the Concentration vs Depth button on the Output toolbar or selecting the Concentration vs Depth menu item from the Output menu.

## **Output Listing**

To display the output as a text listing that will show the calculated concentrations as numbers, select the List Output menu item from the Output menu or press the Output Listing button on the Output toolbar. The peak at 2008 years was found, even though the upper time limit specified by the user was 400 years.

## Case 5: Hydraulic trap, Finite mass, leachate collection, base aquifer

### THE DARCY VELOCITY (Flux) THROUGH THE LAYERS Va = -0.001 m/year

## Layer Properties

	Layer	Thickness	Number of Sublayers	Coefficient of Hydrodynamic Dispersion	Matrix Porosity	Distributon Coefficient	Dry Density
	Aquitard	4 m	4	0.01 cm3/g	0.4	0 m2/a	1.5 g/cm3

### Finite Mass Top Boundary

Initial Concentration = 1000 mg/L Rate of Increase = 0 mg/L/yr Volume of Leachate Collected = 0.3 m/a Thickness of Waste = 0 m Waste Density = 0 kg/m3 Proportion of Mass = 0 Volumetric Water Content = 0 Conversion Rate Half Life = 0 year Reference Height of Leachate = 7.5 m

#### **Fixed Outflow Bottom Boundary**

Landfill Length = 200 m Landfill Width = 1 m Base Thickness = 1 m Base Porosity = 0.35 Base Outflow Velocity = 3.8 m/a

### Laplace Transform Parameters

**TAU =** 7 **N =** 20 **SIG =** 0 **RNU =** 2

### Maximum Base Concentration Parameters

Depth to Search = 4 m Lower Time Limit = 25 year Upper Time Limit = 400 year Base Concentration Accuracy = 0.01 Maximum Search Attempts = 25

Ι

#### Maximum Base Concentration and Time of Occurrence

Time	Depth	Concentration	Preceeding	Preceeding	Exceeding	Exceeding
yr	m	mg/L	Time	Concentration	Time	Concentration
2.0828E+02	0.0000E+00	7.7427E-01				
	1.0000E+00	2.2363E+01				
	2.0000E+00	2.4529E+01				
	3.0000E+00	1.4300E+01				
	4.0000E+00	2.2199E+00	2.0800E+02	2.2199E+00	2.0857E+02	2.2198E+00

Number of Search Attempts = 8

### NOTICE

Although this program has been tested and experience would indicate that it is accurate within the limits given by the assumptions of the theory used, we make no warranty as to workability of this software or any other licensed material. No warranties either expressed or implied (including warranties of fitness) shall apply. No responsibility is assumed for any errors, mistakes or misrepresentations that may occur from the use of this computer program. The user accepts full responsibility for assessing the validity and applicability of the results obtained with this program for any specific case.

The peak concentration in the aquifer at the down gradient edge of the landfill is only about 2 mg/L, compared to the initial source concentration of 1000 mg/L. This peak is reached after 208 years. Thus with a working hydraulic trap some contaminant reaches the base aquifer despite the inward gradient, however for this diffusion coefficient and combination of parameters the impact is negligible.

# Case 6: Fractured Layer and Sorption

# Description

This example illustrates the use of the program for the case where one of the layers are fractured and there is and sorption of the contaminant species. The "barrier" consists of a 1 m thick compacted clay layer overlying a 3 m thick fractured till. A reactive species (i.e., one that will sorb on to the clay) is modelled in this case. The same finite mass source and leachate collection system is used as in the previous examples.

A Darcy velocity  $(v_a)$  of 0.02 m/a through the deposit and an infiltration through the cover  $(q_0)$  of 0.3 m/a are assumed. The Volume of Leachate Collected  $(Q_c)$  is then given by:

$$Q_c = q_0 - v_a = 0.3 - 0.02 = 0.28 \text{ m/a}$$

As in the previous examples the inflow in the aquifer at the up gradient edge of the landfill is 4 m/a. The outflow (v<sub>b</sub>) at the down gradient edge of the landfill is then:

$$v_{b} = 4 + 200 * 0.02 = 8 \text{ m/a}$$

The following parameters are defined for this example:

<b>Property</b>		<u>Value</u>	<u>Units</u>
Darcy Velocity	v <sub>a</sub>	0.02	m/a
Diffusion Coefficient	D	0.01	$m^{2/a}$
Distribution Coefficient	К <sub>d</sub>	1.5	$cm^{3/g}$
Soil Porosity	n	0.4	-
Dry Density		2.0	g/cm <sup>3</sup>
Soil Liner Thickness	$H_{L}$	1.0	m
Number of Sub-layers		1	-
Fractured Till Thickness	Н <sub>Т</sub>	3.0	m
Number of Sub-layers		1	-
Fracture spacing in x direction	2H <sub>1</sub>	1.0	m
Fracture opening in x "	2h1	10	μm
Fracture spacing in y direction	2H <sub>2</sub>	1.0	m
Fracture opening in y "	2h <sub>2</sub>	10	μm
Dispersion along fractures	$D_{\mathrm{f}}$	0.06	$m^{2/a}$
Fracture Distribution Coefficient K <sub>f</sub>	0.0	$cm^3/g$	

<b><u>Property</u></b>		<u>Value</u>	<u>Units</u>
Matrix Diffusion Coefficient	D <sub>m</sub>	0.01	m <sup>2</sup> /a
Matrix Distribution Coefficient	К <sub>m</sub>	1.5	$cm^{3/g}$
Matrix Porosity	n <sub>m</sub>	0.4	-
Dry Density of Matrix Source Concentration	c <sub>o</sub>	2.0 1000	g/cm <sup>3</sup> mg/L
Rate of Increase in Conc.	c <sub>r</sub>	0.0	mg/L/a
Reference Height of Leachate	H <sub>r</sub>	7.5	m
Volume of Leachate Collected	Q <sub>c</sub>	0.28	m/a
Landfill Length	L	200.0	m
Landfill Width	W	1.0	m
Aquifer Thickness	h	1.0	m
Aquifer Porosity	nb	0.35	-
Base Outflow Velocity	v <sub>b</sub>	8.0	m/a
Lower and Upper Time Limits		20, 300	a

# **Data Entry**

Start the POLLUTEv7 program and open the Examples project. Select Case 6 and open the model by double clicking on it in the model list. After the model is displayed, the data for the model can be displayed and edited using the Data Entry menu or by clicking on that part of the model.

# **General Data**

The general data for this example can be specified by either clicking on the title or selecting the General Data menu item from the Data Entry menu. On the General Data form the Darcy velocity of 0.02 m/a and the number of layers of 2 can be specified

General Data
The Case C. for Web Ener On Graduat III Gale and a service
Title: Lase 6. Im thick liner, 3m tractured till, innite mass, sorption
Number of Layers: 2 Maximum Depth: 5 m 💌
Darcy Velocity: 0.02 m/year 💌
Laplace Transform Parameters
TAU:  7 N:  20 SIG:  0 RNU:  2
✓ OK Cancel ? Help

1

### **Case 6: Fractured Layer and Sorption**

## Layer Data

The layer data for the two layers can be specified by either clicking on the layers or selecting the Layer Data menu item from the Data Entry menu. On this form the current layer number can be selected using the arrows at the top of the form. The first layer in this model is a compacted clay with no fractures.

Layer Data	
Layer I	Number 1  4 4 🕨 🕅
Layer Data Layer Symbol	13
Name: Compacted Clay	
Number of Sub Layers 1	Fractures
Thickness 1	m 💌 🕞 None
Dry Density 2	g/cm3  C 1 Dimensional
Porosity 0.4	C 2 Dimensional
Coef of Hydro Disp 0.01	cm3/g 💌 C 3 Dimensional
Distribution Coef 1.5	m3/kg 💌
🗸 ОК	X Cancel ? Help

To enter the data for the second layer, click on the Next button at the top of the form. The second layer is a fractured till with 2 dimensional fractures.

Layer Data	
Layer Number 2	
Layer Data Layer Symbol 2 Dimensional Fructures	
Name: Fractured Till	
Number of Sub Layers 1	Fractures
Thickness 3 m	C None
Dry Density 2 g/cm3 🗸	C 1 Dimensional
Porosity 0.4	2 Dimensional
Coef of Hydro Disp 0.01 cm3/g 💌	C 3 Dimensional
Distribution Coef 1.5 m3/kg 💌	
✓ OK X Cancel	<b>?</b> <u>H</u> elp

### **Case 6: Fractured Layer and Sorption**

On the Fracture tab, the parameters for the two sets of fractures can be specified. The x and y directions for a 2-dimensional fracture system refer to two sets of vertical fractures which are approximately perpendicular to each other. Fracture opening size is the gap between the walls of the fractures in m for metric units.

Layer Data	
	Layer Number 2   ( ( ))
Layer Data Layer Symbol 2 Dimensio	onal Fructures
	Dimension 1 2
Spacing	1 1 m 💌
Opening size	1E-5 m 💌
Number to Sum	10 10
Dispersion Coefficient	0.06 m2/a 💌
Distribution Coefficient	0 m2/a 💌
🗸 ОК	Cancel ? Help

# **Boundary Conditions**

The boundary conditions for the model are the can be specified by either clicking on the top or bottom boundary or selecting the Boundary Conditions menu item from the Data Entry menu. In this example, the top boundary has a finite mass and the bottom boundary is represented as an aquifer with a fixed outflow velocity as shown on the Boundary Condition forms below.

Boundary Conditi	ions			
Boundary Conditions	Top - Finite Mass	lottom - Fixed Ou	utflow   Fix	ed Outflow Symbol
Specify				
Initial	Source Concentration:	1000	mg/L	•
Ral	te of Increase in Conc	0	mg/L/yr	•
Volume	of Leachate Collected	0.28	m/a	•
and either				_
	Thickness of Wase	0	m	•
	Waste Density	0	kg/m3	-7
	Proportion of Mass	0		
Volu	umetric Water Content	0		
Con	version Rate Half Life	0	year	•
or R	ef Height of Leachate	7.5	m	•
	' <u>о</u> к 🗙	Cancel	?	<u>H</u> elp

Boundary Conditi	ons			-
Boundary Conditions	Top - Finite Mass	Bottom - Fixed (	Dutflow   Fi	xed Outflow Symbol
	Landfill Length: 20		•	
	Landfill Width: 1	m	•	
В	ase Thickness: 1	m	•	
	Base Porosity: 0.3	15		
Base O	utflow Velocity: 8	m/a	•	
	<u>0</u> K	X <u>C</u> ancel	?	<u>H</u> elp

## **Run Parameters**

The run parameters for this model can be specified by selecting the Run Parameters menu item from the Data Entry menu. On the Run Parameters form below, the parameters for searching for the maximum concentration can be specified.

Run Pa	arameters	4	
Туре	Maximum Concentrati	ons	
	Search Depth: Accuracy (%): Number of Iterations:	4	Search 👤
	Lower Time Limit: Upper Time Limit:	20	Lower 💌
All ©	Depths Yes No		
	🗸 ОК	🗙 Cancel	? <u>H</u> elp

# **Model Execution**

To run the model and calculate the concentrations either select the Run menu item from the Execute menu or press the Run button on the toolbar.

# **Model Output**

After the model has been executed, the output for the model will be displayed. The initial display will depend on your settings in the program's preferences.

# **Concentration vs Depth**

The Concentration vs. Depth chart below can be displayed by pressing the Concentration vs Depth button on the Output toolbar or selecting the Concentration vs Depth menu item from the Output menu.



# **Output Listing**

To display the output as a text listing that will show the calculated concentrations as numbers, select the List Output menu item from the Output menu or press the Output Listing button on the Output toolbar. The peak concentration occurred at 618 years, which is outside the lower and upper time limits specified. In this example the program was able to find the peak since the bounds were reasonably close to the peak time of occurrence.

## Case 6: 1m thick liner, 3m fractured till, finite mass, sorption

### THE DARCY VELOCITY (Flux) THROUGH THE LAYERS Va = 0.02 m/year

### Layer Properties

Layer	Thickness	Number of Sublayers	Coefficient of Hydrodynamic Dispersion	Matrix Porosity	Distributon Coefficient	Dry Density
Compacted Clay	1 m	1	0.01 cm3/g	0.4	1.5 m3/kg	2 g/cm3
Fractured Till	3 m	1	0.01 cm3/g	0.4	1.5 m3/kg	2 g/cm3

Layer	Fracture Spacing	Opening Size	Number	Fracture Spacing	Opening Size	Number	Fracture Spacing	Opening Size	Number
	1	1	1	2	2	2	3	3	3
Fractured Till	1 m	1E-5 m	10	1 m	1E-5 m	10	[		[

Layer	Dispersion Coefficient in Fractures	Distribution Coefficient in Fractures	Fracture Porosity	Retardation Coefficient in Matrix
Fractured Till	0.06 m2/a	0 m2/a	2.0000E-05	8.5000E+00

### **Boundary Conditions**

#### Finite Mass Top Boundary

Initial Concentration = 1000 mg/L Rate of Increase = 0 mg/L/yr Volume of Leachate Collected = 0.28 m/a Thickness of Waste = 0 m Waste Density = 0 kg/m3 Proportion of Mass = 0 Volumetric Water Content = 0 Conversion Rate Half Life = 0 year Reference Height of Leachate = 7.5 m

#### Fixed Outflow Bottom Boundary

Landfill Length = 200 m Landfill Width = 1 m Base Thickness = 1 m Base Porosity = 0.35 Base Outflow Velocity = 8 m/a

Τ

### Laplace Transform Parameters

**TAU** = 7 **N** = 20 **SIG** = 0 **RNU** = 2

### Maximum Base Concentration Parameters

Depth to Search = 4 Search Lower Time Limit = 20 Lower Upper Time Limit = 300 Upper Base Concentration Accuracy = 0.01 Maximum Search Attempts = 25

#### Maximum Base Concentration and Time of Occurrence

Time	Depth	Concentration	Preceeding	Preceeding	Exceeding	Exceeding
yr	m	mg/L	Time	Concentration	Time	Concentration
6.1816E+02	0.0000E+00 1.0000E+00 4.0000E+00	1.7644E-03 2.9323E-01 2.6868E+01	6.1770E+02	2.6868E+01	6.1861E+02	2.6869E+01

Number of Search Attempts = 10

#### NOTICE

Although this program has been tested and experience would indicate that it is accurate within the limits given by the assumptions of the theory used, we make no warranty as to workability of this software or any other licensed material. No warranties either expressed or implied (including warranties of fitness) shall apply. No

# Case 7: Fractured Rock and Radioactive Decay

# Description

This example illustrates the use of the program for lateral migration of a radioactive contaminant in a fractured porous rock with a single set of parallel fractures. It considers advective-dispersive transport along the fractures and diffusion into the rock matrix. The deposit is assumed to extend a considerable distance from the source (effectively an infinite distance) but we are only interested here in what happens over the first 50 m after 30 years..

It is assumed that the source concentration,  $c_0$ , is 1 unit and that the half life of the radioactive species is

100 years. The source is considered to have a sufficiently large supply that there is no significant change in source concentration due to mass movement into the rock. However the source does experience radioactive decay.

This example is also being used to illustrate the **Maximum Sublayer Thickness Special Feature**, for specifying sublayer thicknesses that are greater than 5 units.

The following parameters are defined for this example:

<b>Property</b>		<u>Value</u>	<u>Units</u>
Darcy Velocity	v <sub>a</sub>	0.08	m/a
Matrix Diffusion Coefficient	D <sub>m</sub>	0.0018	m <sup>2</sup> /a
Matrix Distribution Coefficient	К <sub>m</sub>	0.0	$cm^{3/g}$
Matrix Porosity	n <sub>m</sub>	0.05	-
Matrix Dry Density		2.0	g/cm <sup>3</sup>
Fractured Rock Thickness	Н <sub>Т</sub>	50	m
Number of Sub-layers		5	-
Fracture spacing	2H <sub>1</sub>	0.05	m
Fracture opening	2h1	10	μm
Dispersion along fractures	$D_{\mathrm{f}}$	6.0	$m^{2/a}$
Fracture Distribution Coefficient	К <sub>f</sub>	0.0	$cm^{3/g}$
Source Concentration	c <sub>0</sub>	1.0	unit
Half life of contaminant		100	a
Time period of interest		30	a

# **Data Entry**

Start the POLLUTEv7 program and open the Examples project. Select Case 7 and open the model by double clicking on it in the model list. After the model is displayed, the data for the model can be displayed and edited using the Data Entry menu or by clicking on that part of the model.

## **General Data**

The general data for this example can be specified by either clicking on the title or selecting the General Data menu item from the Data Entry menu. On the General Data form below, the integration parameters for the Laplace Transform have been increased for this example. These parameters will need to be adjusted if the output shows that the default parameters are insufficient.

General Data
Title: Case 7: Lateral migration in fractured vock
Number of Layers: 1 Maximum Depth: 50 m
Darcy Velocity: 0.08 m/year 💌
Laplace Transform Parameters
TAU: 7 N: 40 SIG: 0 RNU: 4
✓ OK Cancel ? Help

l

## Layer Data

The layer data for the layer can be specified by either clicking on the layer or selecting the Layer Data menu item from the Data Entry menu. On this form the data for the layer and fracture can be added as below.

Layer Data	
Layer Number 1	
Layer Data Layer Symbol 1 Dimensional Fractures	
Name: Fractured Rock	Ĩ
Number of Sub Layers 5	Fractures
Thickness 50 m 🖵	C None
Dry Density 2 g/cm3 🗸	• 1 Dimensional
Porosity 0.05	C 2 Dimensional
Coef of Hydro Disp 0.0018 m2/a 💌	C 3 Dimensional
Distribution Coef 0 m3/kg 💌	
V OK Cancel	? Help

Layer Data
Layer Number 1 🛛 🖌 🖌 🕨
Layer Data Layer Symbol 1 Dimensional Fractures
Dimension
Spacing  0.05 m _
Opening Size 1E-5 m 💌
Number to Sum 10
Dispersion coefficient 6 m2/a 💌
Distirubition Coefficient 0 m3/kg 🗨
✓ OK X Cancel ? Help

## **Boundary Conditions**

The boundary conditions for the model can be specified by either clicking on the top or bottom boundary or selecting the Boundary Conditions menu item from the Data Entry menu. In this example, the top boundary has a constant concentration and the bottom boundary is represented as a layer with infinite thickness, as shown on the Boundary Condition forms below. For the Infinite Thickness boundary condition, the properties of the last layer in the Layer Data are assumed to extend infinitely.

Boundary Conditions				
Boundary Conditions Top - Constant C	Conc.			
Top Boundary	Zero Flux     Constant Concentration     Finite Mass			
Bottom Boundary	<ul> <li>Zero Flux</li> <li>Constant Conc</li> <li>Fixed Outflow Velocity</li> <li>Infinite Thickness</li> </ul>			
<u>√</u> <u>□</u> K	X Cancel ? Help			

## **Run Parameters**

To set the times and depths to calculate the concentrations, select the Run Parameters menu item from the Data Entry menu. The concentrations can either be calculated at specified times or the time of the maximum concentration can be found. In this example the concentrations will be calculated at a time of 30 years and at 4 depths: 10, 30, 40, and 50 m.

# **Special Features**

The radioactive decay and maximum sublayer thickness for this example are specified using the Special Features menu.

## **Radioactive Decay**

To specify the radioactive decay, select the Radioactive/Biological Decay menu item from the Special Features form. The Decay tab on the Radioactive/Biological Decay form shown on the next page can be used to specify the source and base decay.

Radioa	ctive/Bi	ological Decay
Decay	Ranges	
		Number of Depth Rangers: 1
Sou	urce Decaj (● Yes	, Source Half-Life
	C No	100 yr 💌
Bas	e Decay	Page Half I ife
	Yes	
	C No	100  yr <u> </u>
[	🗸 01	K Cancel ? Help

The data for the depth ranges is entered on the Ranges tab, shown below. In this example there is one depth range, corresponding to the entire thickness of the layer, with a half-life of 100 years.

Radioa	ctive/Bi	ological De	cay		
Decay	Ranges				
	Rang	ge Number	1	4 4	▶ ▶
		Top Depth		m	•
	В	ottom Depth	50	m	•
		Half Life	100	yr	•
[	🗸 0ł		🗙 Cancel	?	'Help

## **Maximum Sublayer Thickness**

The Maximum Sublayer Thickness special feature allows the user to override the default maximum sublayer thickness of 5 units. This maximum is set to avoid problems with exponential overflow which can sometimes occur if the sublayers are too large. When overriding the default you take the risk that the program will crash or give false results - <u>caveat emptor!</u>.

To change the maximum sublayer thickness, select the Maximum Sublayer Thickness menu item from the Special Features menu, the Maximum Sublayer Thickness form below will then be displayed. In this example a value of 10.01 is used, each sublayer may be up to 10.01 m thick in this example. The reason for changing this parameter is to allow the calculation of depth at 10 m intervals in the 50 m layer.

Maximum Sublayer Thickness				
Information				
Maximum Sublayer Thickness - When overriding the default the program may crash or give false results				
Maximum Layer Thickness 10.01				
V OK Cancel ? Help				

# **Model Execution**

To run the model and calculate the concentrations either select the Run menu item from the Execute menu or press the Run button on the toolbar.

# **Model Output**

After the model has been executed, the output for the model will be displayed. The initial display will depend on your settings in the program's preferences.

## **Concentration vs Depth**

The Concentration vs. Depth chart on the next page can be displayed by pressing the Concentration vs Depth button on the Output toolbar or selecting the Concentration vs Depth menu item from the Output menu.

## **Case 7: Fractured Rock and Radioactive Decay**



Ι

## **Output Listing**

To display the output as a text listing that will show the calculated concentrations as numbers, select the List Output menu item from the Output menu or press the Output Listing button on the Output toolbar.

## Case 7: Lateral migration in fractured rock

### THE DARCY VELOCITY (Flux) THROUGH THE LAYERS Va = 0.08 m/year

Layer Properties

Layer	Thickness	Number of Sublayers	Coefficient of Hydrodynamic Dispersion	Matrix Porosity	Distributon Coefficient	Dry Density
Fractured Rock	50 m	5	0.0018 m2/a	0.05 9	0 m3/kg	2 g/cm3

Layer	Fracture Spacing 1	Opening Size 1	Number 1	Fracture Spacing 2	Opening Size 2	Number 2	Fracture Spacing 3	Opening Size 3	Number 3
Fractured Rock	0.05 m	1E-5 m	10			1	-		

Layer	Dispersion Coefficient in Fractures	Distribution Coefficient in Fractures	Fracture Porosity	Retardation Coefficient in Matrix
Fractured Rock	6 m2/a	i O m3/kg	2.0000E-04	1.0000E+00

### **Boundary Conditions**

Contant Concentration

Source Concentration = 1 mg/L

Infinite Thickness Bottom Boundary

### RADIOACTIVE OR BIOLOGICAL DECAY

#### First Order Radioactive or Biological Decay Depth Ranges

Minimum Depth	Maximum Depth	Half Life	
0 m	50 m	100 yr	

Radioactive or Biological Decay Source Half Life = 100 yr

Radioactive or Biological Decay Base Half Life = 100 yr

### Laplace Transform Parameters

#### TAU = 7 N = 40 SIG = 0 RNU = 4

### Calculated Concentrations at Selected Times and Depths

Time	Depth	Concentration
year	m –	mg/L
30	0.000E+00	8.123E-01
	1.000E+01	8.123E-01
	3.000E+01	8.123E-01
	4.000E+01	7.881E-01
	5.000E+01	2.588E-01

#### NOTICE

Although this program has been tested and experience would indicate that it is accurate within the limits given by the assumptions of the theory used, we make no warranty as to workability of this software or any other licensed material. No warranties either expressed or implied (including warranties of fitness) shall apply. No responsibility is assumed for any errors, mistakes or misrepresentations that may occur from the use of this computer program. The user accepts full responsibility for assessing the validity and applicability of the results obtained with this program for any specific case.

### **Case 7: Fractured Rock and Radioactive Decay**

Below is the results using the default Laplace Transform parameters. These results are clearly wrong! The other values are correct. We can get the correct value at 50 m by increasing the amount of integration as indicated in the previous output listing.

### First Order Radioactive or Biological Decay Depth Ranges

Minimum Depth	Maximum Depth	Half Life
0 m	50 m	100 yr

Radioactive or Biological Decay Source Half Life = 100 yr

Radioactive or Biological Decay Base Half Life = 100 yr

### Laplace Transform Parameters

TAU = 7 N = 20 SIG = 0 RNU = 2

Ι

### Calculated Concentrations at Selected Times and Depths

Time	Depth	Concentration
year	m	mg/L
30	0.000E+00	8.123E-01
	1.000E+01	8.123E-01
	3.000E+01	8.123E-01
	4.000E+01	7.883E-01
	5.000E+01	-1.384E+02

#### NOTICE

Although this program has been tested and experience would indicate that it is accurate within the limits given by the assumptions of the theory used, we make no warranty as to workability of this software or any other licensed material. No warranties either expressed or implied (including warranties of fitness) shall apply. No responsibility is assumed for any errors, mistakes or misrepresentations that may occur from the use of this computer program. The user accepts full responsibility for assessing the validity and applicability of the results obtained with this program for any specific case.

# **Case 8: Diffusion with Initial Concentration Profile**

# Description

The results of a laboratory diffusion test are analyzed in this example [see Rowe, Caers & Barone, 1988; Barone, Yanful, Quigley & Rowe, 1989]. In this example the diffusion of Potassium in a clay is examined. The clay has an initial background concentration of Potassium of 10 mg/L.

The leachate source has an initial concentration  $(c_0)$  of 400 mg/L, and the physical height of the leachate in the reservoir above the soil was 6 cm. At the base of the specimen there was an impermeable barrier (i.e., zero flux).

Following are the parameters used in this example:

<b>Property</b>		<u>Value</u>	<u>Units</u>
Darcy Velocity	va	0.0	m/d
Diffusion Coefficient	D	0.648	$cm^2/d$
Distribution Coefficient	К <sub>d</sub>	2.68	$cm^3/g$
Soil Porosity	n	0.39	-
Dry Density		1.68	g/cm <sup>3</sup>
Soil Layer Thickness	Н	4.5	cm
Number of Sub-layers		10 -	
Source Concentration	co	400.0	mg/L
Ref. Height of Leachate	H <sub>r</sub>	6.0	cm
Background Concentration		10.0	mg/L
Times of Interest	t	3, 6, 9	d
		12, 15	d

When using an initial concentration profile (eg. background 10 mg/L in this example) the user should have at least three layers, with the top and bottom layer being very thin. In this example layers 1 and 3 are taken to be 0.1 cm thick and layer 2 (the main layer) is taken to be 4.5 - 0.2 = 4.3 cm thick.

# **Data Entry**

Start the POLLUTEv7 program and open the Examples project. Select Case 8 and open the model by double clicking on it in the model list. After the model is displayed, the data for the model can be displayed and edited using the Data Entry menu or by clicking on that part of the model.

1

## **General Data**

The general data for this example can be specified by either clicking on the title or selecting the General Data menu item from the Data Entry menu. On the General Data form below, the Darcy velocity is set to zero for pure diffusion.

General Data
Title: Case 8: Analysis of a Labratory-Piffusion test with background
Number of Layers: 3 Maximum Depth: 4.5 m
Darcy Velocity: 0 m/year 💌
Laplace Transform Parameters
TAU:  7 N:  20 SIG:  0 RNU:  2
✓ OK Cancel ? Help

# Layer Data

The layer data for the layers can be specified by either clicking on a layer or selecting the Layer Data menu item from the Data Entry menu. On this form the data for the layers can be added as shown below.

Layer Data	4	
	Layer Number 1	
Layer Data Layer Symbol		
Name: Clay		
Number of Sub Layers	1	Fractures
Thickness	0.1 m 💌	None
Dry Density	1.68 g/cm3 💌	C 1 Dimensional
Porosity	0.39	C 2 Dimensional
Coef of Hydro Disp	0.648 cm3/g 💌	C 3 Dimensional
Distribution Coef	2.68 m3/kg 💌	
<b>V</b>	OK 🗙 Cancel	<b>?</b> <u>H</u> elp

## **Case 8: Diffusion with Initial Concentration Profile**

There are no fractures in these layers. For pure diffusion even if there were fractures it should be modelled as if the soil was unfractured, since there would be no flow in the fractures for pure diffusion.

Layer Data	
Layer Number 2	
Layer Data Layer Symbol	
Name: Clay	<u>l</u>
Number of Sub Layers 10	Fractures
Thickness 4.3 m 💌	None
Dry Density 1.68 g/cm3 💌	C 1 Dimensional
Porosity 0.39	C 2 Dimensional
Coef of Hydro Disp 0.648 cm3/g 💌	C 3 Dimensional
Distribution Coef 2.68 m3/kg 💌	
V OK K Cancel	? Help

Layer Data		
	Layer Number 3	
Layer Data Layer Symbol	·	
Name: Clay		
Number of Sub Layers	1	Fractures
Thickness	0.1 m 💌	None
Dry Density	1.68 g/cm3 💌	C 1 Dimensional
Porosity	0.39	C 2 Dimensional
Coef of Hydro Disp	0.648 cm3/g 💌	C 3 Dimensional
Distribution Coef	2.68 m3/kg 💌	
<b>~</b> 0	DK 🗙 Cancel	<u>? Н</u> еlp

# **Boundary Conditions**

The boundary conditions for the model can be specified by either clicking on the top or bottom boundary or selecting the Boundary Conditions menu item from the Data Entry menu. In this example, the top boundary has a finite mass and the bottom boundary is represented as a zero flux layer, as shown on the Boundary Condition forms on the next page.

## **Case 8: Diffusion with Initial Concentration Profile**

Boundary Conditions	
Boundary Conditions   Top - Finite Mas	s
Top Boundary	Zero Flux     Constant Concentration     Finite Mass
Bottom Boundary	<ul> <li>Zero Flux</li> <li>Constant Conc</li> <li>Fixed Outflow Velocity</li> <li>Infinite Thickness</li> </ul>
<u>✓ </u> <u>□</u> K	X Cancel ? Help

Boundary Conditions 🛛 👌		
Boundary Conditions Top - Finite Mass		
Specify		
Initial Source Concentration:	400	mg/L 💌
Rate of Increase in Conc:	0	mg/L/yr 👻
Volume of Leachate Collected:	0	m/a 🔻
and either		
Thickness of Wase:	0	m 🔹
Waste Density:	0	kg/m3 👻
Proportion of Mass:	0	
Volumetric Water Content:	0	
Conversion Rate Half Life:	0	year 💌
or Ref Height of Leachate:	6	m
<u> </u>	Cancel	? Help

## **Run Parameters**

To set the times and depths to calculate the concentrations, select the Run Parameters menu item from the Data Entry menu. The concentrations can either be calculated at specified times or the time of the maximum concentration can be found. In this example the concentrations will be calculated at 5 times: 3, 6, 9, 12, and 15 years.

# **Special Features**

The initial concentration profile for this example is specified using the Special Features menu.

# **Initial Concentration Profile**

To specify the initial concentration profile, select the Initial Concentration Profile menu item from the Special Features form. The Concentration Profile tab on the form shown below can be used to specify the type of profile as either Depth Intervals or Sublayers.

Initial Concentratio	Initial Concentration Profile				
Concentration Prof	Depth Intervals				
Start Tim	e 🛛	yr •	-		
Flux into So	pil 0	m2/a	-		
Flux into Bas	e 0	m2/a	-		
Type of Profile		, _			
Oepth Inte	ervals	C Sublayers			
Number of Depth Ir	ntervals 1				
🗸 ок	🗙 Cancel	?⊦	lelp		
Initial Concentratio	n Profile	_			
Initial Concentratio	n Profile )epth Intervals	-			
Initial Concentratio	n Profile )epth Intervals	-			
Initial Concentratio Concentration Profile	n Profile Depth Intervals    1 ]	I	M		
Initial Concentratio Concentration Profile C Depth Interval	n Profile Depth Intervals	4 ↓ ▶	M		
Initial Concentratio Concentration Profile Depth Interval Top Depth	n Profile Depth Intervals    1	<b>∢ ∢ →</b>	×.		
Initial Concentratio Concentration Profile C Depth Interval Top Depth	n Profile Depth Intervals   1 1	<b>I</b> ◀ ▶	•		
Initial Concentratio	n Profile Depth Intervals	<b>∢</b> ↓ ↓  m	► •		
Initial Concentratio	n Profile Depth Intervals 1 1 0 4.5	▲ ▲ →  m  m	► - -		
Initial Concentratio Concentration Profile C Depth Interval Top Depth Bottom Depth Concentration	n Profile Depth Intervals 1 1 4.5 10	M ← M	► • •		
Initial Concentratio Concentration Profile C Depth Interval Top Depth Bottom Depth Concentration	n Profile Depth Intervals 1 1 4.5 10	I	► <b>F</b> <b>F</b>		
Initial Concentratio	n Profile Depth Intervals	I ↓ ↓ m m mg/L	•		

# **Model Execution**

To run the model and calculate the concentrations either select the Run menu item from the Execute menu or press the Run button on the toolbar.

# **Model Output**

After the model has been executed, the output for the model will be displayed. The initial display will depend on your settings in the program's preferences.

## **Concentration vs Depth**

The Concentration vs. Depth chart below can be displayed by pressing the Concentration vs Depth button on the Output toolbar or selecting the Concentration vs Depth menu item from the Output menu.



## **Output Listing**

To display the output as a text listing that will show the calculated concentrations as numbers, select the List Output menu item from the Output menu or press the Output Listing button on the Output toolbar.

### Case 8: Analysis of a Labratory Diffusion test with background

### THE DARCY VELOCITY (Flux) THROUGH THE LAYERS Va = 0 m/year

I

### Layer Properties

Layer	Thickness	Number of Sublayers	Coefficient of Hydrodynamic Dispersion	Matrix Porosity	Distributon Coefficient	Dry Density
Clay	0.1 m	1	0.648 cm3/g	0.39	2.68 m3/kg	1.68 g/cm3
Clay	4.3 m	10	0.648 cm3/g	0.39	⁼ 2.68 m3/kg	1.68 g/cm3

### Layer Properties

Layer	Thickness	Number of Sublayers	Coefficient of Hydrodynamic Dispersion	Matrix Porosity	Distributon Coefficient	Dry Density
Clay	0.1 m	1	0.648 cm3/g	0.39	2.68 m3/kg	1.68 g/cm3
Clay	4.3 m	10	0.648 cm3/g	0.39	2.68 m3/kg	1.68 g/cm3
Clay	0.1 m	1	0.648 cm3/g	0.39	2.68 m3/kg	1.68 g/cm3

### **Boundary Conditions**

#### Finite Mass Top Boundary

Initial Concentration = 400 mg/L Rate of Increase = 0 mg/L/yr Volume of Leachate Collected = 0 m/a Thickness of Waste = 0 m Waste Density = 0 kg/m3 Proportion of Mass = 0 Volumetric Water Content = 0 Conversion Rate Half Life = 0 year Reference Height of Leachate = 6 m

Flux into Base = 0 m2/a

Time	Depth	Concentration
year	m	mg/L
I	I 0.000E+00 1.000E-01 5.300E-01 9.600E-01 1.390E+00 1.820E+00 2.250E+00 2.680E+00 3.110E+00 3.540E+00 4.400E+00 4.500E+00	2.910E+02 2.569E+02 1.164E+02 3.779E+01 1.426E+01 1.038E+01 1.002E+01 1.000E+01 1.000E+01 1.000E+01 1.000E+01 1.000E+01 1.000E+01 1.000E+01 1.000E+01
ь	0.000E+00 1.000E+01 5.300E-01 9.600E-01 1.390E+00 2.250E+00 2.680E+00 3.110E+00 3.540E+00 3.970E+00 4.400E+00 4.500E+00	2.596E+02 2.398E+02 1.491E+02 7.573E+01 3.391E+01 1.664E+01 1.140E+01 1.022E+01 1.003E+01 1.000E+01 1.000E+01 1.000E+01 1.000E+01
9	0.000E+00 1.000E-01 5.300E-01 9.600E+00 1.390E+00 1.820E+00 2.250E+00 2.680E+00 3.110E+00 3.540E+00 3.970E+00 4.400E+00	2.394E+02 2.253E+02 1.586E+02 9.690E+01 5.273E+01 2.758E+01 1.602E+01 1.02E+01 1.040E+01 1.008E+01 1.001E+01 1.000E+01

## Calculated Concentrations at Selected Times and Depths

	4.500E+00	\$ 1.000E+01
12	0.000E+00     1.000E-01     1.000E-01     9.600E-01     1.390E+00     1.820E+00     2.250E+00     2.680E+00     3.110E+00     3.540E+00     3.970E+00     4.400E+00     4.500E+00	2.243E+02 2.135E+02 1.610E+02 1.088E+02 6.682E+01 3.859E+01 2.266E+01 1.480E+01 1.160E+01 1.046E+01 1.012E+01 1.004E+01 1.003E+01
15	0.000E+00 1.000E-01 5.300E-01 9.600E-01 1.390E+00 1.820E+00 2.250E+00 2.680E+00 3.110E+00 3.540E+00 3.970E+00 4.400E+00	2.124E+02 2.036E+02 1.605E+02 1.158E+02 7.699E+01 4.814E+01 2.948E+01 1.891E+01 1.365E+01 1.134E+01 1.045E+01 1.020E+01 1.019E+01

### NOTICE

Although this program has been tested and experience would indicate that it is accurate within the limits given by the assumptions of the theory used, we make no warranty as to workability of this software or any other licensed material. No warranties either expressed or implied (including warranties of fitness) shall apply. No responsibility is assumed for any errors, mistakes or misrepresentations that may occur from the use of this computer program. The user accepts full responsibility for assessing the validity and applicability of the results obtained with this program for any specific case.

# **Case 9: Freundlich Non-linear Sorption**

# Description

In this example a laboratory test is simulated using diffusion and Freundlich non-linear sorption. The sample is a 7 cm thick clay with an impermeable base and a finite mass source of Phenol. The leachate source has an initial concentration ( $c_0$ ) of 50 mg/L, and the physical height of the leachate in the reservoir above the soil was 6.5 cm. Parameters for the Freundlich isotherm were obtained experimentally from batch tests, these are K<sub>f</sub>=2 and =0.628 (see the section on Freundlich Non-linear Sorption in Chapter 4 for a discussion on these parameters).

Following are the parameters used in this example:

<b>Property</b>		<u>Value</u>	<u>Units</u>
Darcy Velocity	va	0.0	cm/hr
Diffusion Coefficient	D	0.019	cm <sup>2</sup> /hr
Sorption Coefficient	К <sub>f</sub>	2.0	$cm^{3/g}$
Sorption Exponent		0.628	-
Soil Porosity	n	0.46	-
Dry Density		1.47	g/cm <sup>3</sup>
Soil Layer Thickness	Н	7.0	cm
Number of Sub-layers		14	-
Source Concentration	c <sub>o</sub>	50.0	mg/L
Ref. Height of Leachate	H <sub>r</sub>	6.5	cm
Times of Interest	t	200, 400	hr
		600, 800	hr

When using non-linear sorption the accuracy of the solution is dependent on the number of sub-layers used.

# **Data Entry**

Start the POLLUTEv7 program and open the Examples project. Select Case 9 and open the model by double clicking on it in the model list. After the model is displayed, the data for the model can be displayed and edited using the Data Entry menu or by clicking on that part of the model.

1

## **General Data**

The general data for this example can be specified by either clicking on the title or selecting the General Data menu item from the Data Entry menu. On the General Data form below, the Darcy velocity is set to zero for pure diffusion.

General Data
Title: Case 9: Freundlich Non-linear sorption in a lab diffusion test
Number of Layers: 1 Maximum Depth: 7 cm 💌
Darcy Velocity: 0 m/hr 🗨
Laplace Transform Parameters
TAU: 7 N: 20 SIG: 0 RNU: 2
✓ OK X Cancel ? Help

# Layer Data

The layer data for the layer can be specified by either clicking on a layer or selecting the Layer Data menu item from the Data Entry menu. On this form the data for the layer can be added as shown below. When using non-linear sorption the Distribution Coefficient is automatically calculated. The value entered below is ignored by the program.

Layer Data		
	Layer Number 1	
Layer Data Layer Symbol	R	
Name: Clay		
Number of Sub Layers	14	Fractures
Thickness	7 cm 💌	None
Dry Density	1.47 g/cm3 💌	C 1 Dimensional
Porosity	0.46	C 2 Dimensional
Coef of Hydro Disp	0.019 cm2/hr 💌	C 3 Dimensional
Distribution Coef	0 cm3/g 👻	
<b>V</b> 0	K 🛛 🗶 Cancel	? Help

There are no fractures in the layer. For pure diffusion even if there were fractures it should be modelled as if the soil was unfractured, since there would be no flow in the fractures for pure diffusion through the matrix.

# **Boundary Conditions**

The boundary conditions for the model can be specified by either clicking on the top or bottom boundary or selecting the Boundary Conditions menu item from the Data Entry menu. In this example, the top boundary has a finite mass and the bottom boundary is represented as a zero flux layer, as shown on the Boundary Condition form below.

Boundary Conditions				
Boundary Conditions	Top - Finite Mass			
Specify				
Initial Source Concentration:		50	mg/L 💌	
Rate of Increase in Conc:		0	mg/L/yr ▼	
Volume o	of Leachate Collected:	0	m/a 🕹 🔻	
and either				
	Thickness of Wase:	0	m 💌	
	Waste Density:	0	kg/m3 👻	
	Proportion of Mass:	0		
Volu	metric Water Content:	0		
Con	version Rate Half Life:	0	year 💌	
Be	ef Height of Leachate:	6.5	cm 💌	
	ок 🗴	<u>C</u> ancel	? <u>H</u> elp	

# **Run Parameters**

To set the times and depths to calculate the concentrations, select the Run Parameters menu item from the Data Entry menu. The concentrations can either be calculated at specified times or the time of the maximum concentration can be found. In this example the concentrations will be calculated at 4 times: 200, 400, 600, and 800 years.

# **Special Features**

The non-linear sorption for this example is specified using the Special Features menu.
### **Non-linear Sorption**

To specify the Freundlich non-linear sorption, select the Non-linear Sorption menu item from the Special Features form. The Sorption Data tab on the Non-linear Sorption form shown on the next page can be used to specify the type of sorption as either Freundlich or Langmuir.

Non-Linear Sorption
Sorption Data Layer Data
Non-linear Sorption Type
⊂ None
Maximum Number of Iterations 10
Minimium Reference Concentration 0.1 mg/L 🗨
V OK Cancel ? Help

The Freundlich non-linear sorption parameters are entered on the Layer Data tab shown below. These *para-meters are determined experimentally*. The iterative procedure used to determine the distribution coefficient is repeated until either the maximum change in concentrations between iterations is less than 0.1% or the maximum number of iterations is reached. Minimum reference concentration is the minimum value that will be used in calculating the distribution coefficient. If the average concentration in a sub-layer is less than this minimum reference value, then the reference value is used in the calculation of the distribution coefficient (see the section on Freundlich Non-linear Sorption in Chapter 4 for more information).

Non-Linear Sorption Sorption Data
Layer Number 1 (4 4 ) )
S = Kf * c ** E
Coefficient Kf
Exponent E 0.628
✓ OK X Cancel ? Help

# **Model Execution**

To run the model and calculate the concentrations either select the Run menu item from the Execute menu or press the Run button on the toolbar.

# **Model Output**

After the model has been executed, the output for the model will be displayed. The initial display will depend on your settings in the program's preferences.

### **Concentration vs Depth**

The Concentration vs. Depth chart below can be displayed by pressing the Concentration vs Depth button on the Output toolbar or selecting the Concentration vs Depth menu item from the Output menu.



### **Output Listing**

To display the output as a text listing that will show the calculated concentrations as numbers, select the List Output menu item from the Output menu or press the Output Listing button on the Output toolbar.

### Case 9: Freundlich Non-linear sorption in a lab diffusion test

### THE DARCY VELOCITY (Flux) THROUGH THE LAYERS Va = 0 m/hr

### Layer Properties

Layer	Thickness	Number of Sublayers	Coefficient of Hydrodynamic Dispersion	Matrix Porosity	Distributon Coefficient	Dry Density
Clay	7 cm	14	0.019 cm2/hr	0.46	0 cm3/g	1.47 g/cm3
Clay	7 cm	14	Dispersion 0.019 cm2/hr	0.46	0 cm3/g	1.47 g/cm3

### Non-Linear Sorption

Maximum Number of Iterations = 10 Minimum Reference Concentration = 0.1 mg/L Freundlich Sorption Isotherm S = K \* c^E

Layer	K	E
1	2	. 0.628

### **Boundary Conditions**

#### Finite Mass Top Boundary

Initial Concentration = 50 mg/L Rate of Increase = 0 mg/L/yr Volume of Leachate Collected = 0 m/a Thickness of Waste = 0 m Waste Density = 0 kg/m3 Proportion of Mass = 0 Volumetric Water Content = 0 Conversion Rate Half Life = 0 year

### Laplace Transform Parameters

**TAU** = 7 **N** = 20 **SIG** = 0 **RNU** = 2

# Calculated Concentrations at Selected Times and Depths

Time	Depth	Concentration
hr	cm	mg/L
200	0.000E+00	3.915E+01
	5.000E-01	3.022E+01
	1.000E+00	2.143E+01
	1.500E+00	1.367E+01
	2.000E+00	7.618E+00
	2.500E+00	3.521E+00
	3.000E+00	1.233E+00
	3.500E+00	2.728E-01
	4.000E+00	3.002E-02
	4.500E+00	1.801E-03
	5.000E+00	6.511E-05
	5.500E+00	1.412E-06
	6.000E+00	1.834E-08
	6.500E+00	1.499E-10
	, 7.000E+00	5.539E-12
	ſ	

Convergence Check for Non-linear Sorption O Iterations. Maximum Change: 0%

400	0.000E+00	3.562E+01
	5.000E-01	3.009E+01
	1.000E+00	2.439E+01
	1.500E+00	1.884E+01
	2.000E+00	1.376E+01
	2.500E+00	9.404E+00
	3.000E+00	5.917E+00
	3.500E+00	3.349E+00
	4.000E+00	1.645E+00
	4.500E+00	6.591E-01
	5.000E+00	1.935E-01
	5.500E+00	3.828E-02
	6.000E+00	5.748E-03
	6.500E+00	6.747E-04
	7.000E+00	1.213E-04
		1

1.500E+00	2.057E+01
2.000E+00	1.643E+01
2.500E+00	1.261E+01
3.000E+00	9.239E+00
3.500E+00	6.408E+00
4.000E+00	4.156E+00
4.500E+00	2.478E+00
5.000E+00	1.324E+00
5.500E+00	6.085E-01
6.000E+00	2.267E-01
6.500E+00	6.795E-02
7.000E+00	3.012E-02

Convergence Check for Non-linear Sorption O Iterations. Maximum Change: G%

	0.0005.00	
800	U.UUUE+UU	3.136E+U1
	5.000E-01	2.812E+01
	1.000E+00	2.469E+01
	1.500E+00	2.119E+01
	2.000E+00	1.772E+01
	2.500E+00	1.441E+01
	3.000E+00	1.135E+01
	3.500E+00	8.617E+00
	4.000E+00	6.273E+00
	4.500E+00	4.347E+00
	5.000E+00	2.841E+00
	5.500E+00	1.736E+00
	6.000E+00	9.974E-01
	6.500E+00	5.794E-01
	7.000E+00	4.451E-01

Convergence Check for Non-linear Sorption 0 Iterations. Maximum Change: 0%

#### NOTICE

Although this program has been tested and experience would indicate that it is accurate within the limits given by the assumptions of the theory used, we make no warranty as to workability of this software or any other licensed material. No warranties either expressed or implied (including warranties of fitness) shall apply. No responsibility is assumed for any errors, mistakes or misrepresentations that may occur from the use of this

# Case 10: Time-varying Transport

# Description

This example illustrates the use of the programs to study time-varying rates of advective-dispersive transport from a landfill, using the Variable Properties special feature. The landfill contains a finite mass of a conservative species, and has a leachate collection system. Initially there is an inward hydraulic gradient causing a hydraulic trap. After 20 years the collection of leachate is terminated and the leachate mound begins to build reaching it's maximum height after another 10 years. The increased leachate mound causes a reversal in the hydraulic gradient, that results in a reversal of the Darcy velocity and the loss of the hydraulic trap.

The analysis starts at time zero which corresponds to the completion of the landfill and the development of a peak leachate concentration ( $c_0$ ) of 1000 mg/L. It is assumed that the average waste thickness is 6.25 m with a density of 600 kg/m3, and that the contaminant represents 0.2% of the total mass of the waste. Thus the total mass of contaminant per unit area of landfill is:

$$m_{tc} = 0.002 * 600 = 6.25 \text{ kg/m}^2$$

The Reference Height of Leachate  $(H_r)$  is then calculated by dividing the total mass of contaminant per unit area  $(m_{tc})$  by the contaminant concentration  $(c_0)$ .

$$H_r = (0.002 * 600 * 6.25) / 1 = 7.5 m$$

It is also assumed that the peak concentration in the landfill is reached relatively early in the life of the landfill, and that the analysis starts at this time. Consequently there is no increase in concentration with time and the Rate of Increase in Concentration  $(c_r)$  with time is zero.

The average infiltration through the cover  $(q_0)$  is assumed to be 0.3 m/a. If the average exfiltration through the base of the landfill is  $v_a$  (which varies with time), then the Volume of Leachate Collected is:

$$Q_c = q_o - v_a = 0.3 - v_a$$

In this example the landfill is situated in a 4 m thick clay, which in underlain by an aquifer. The landfill is assumed to be 200 m long in the direction parallel to the groundwater flow in the aquifer. At the up gradient edge of the landfill the inflow in the aquifer is given by a Darcy velocity of 2 m/a. The outflow Darcy velocity at the down gradient edge of the landfill ( $v_b$ ) is assumed to be 2 m/a from years 0 to 20, then increasing between 20 and 30 years according to the relationship:

$$vb = 2 + 200 * v_a$$

After 30 years the outflow Darcy velocity  $(v_b)$  is 6.2 m/a.

When using the Variable Properties special feature it is possible to independently specify the diffusion coefficient (Dm) and the dispersivity (). In this example the dispersivity is assumed to be zero for inward flow (i.e.,  $v_a < 0$ ), and is 0.4 m for outward flow (i.e.,  $v_a > 0$ ). The coefficient of hydrodynamic dispersion (D) is then calculated by:

$$D = D_m + \alpha * v_a/n$$

where n is the porosity, in this example 0.4.

Following are the parameters used in this example:

<b>Property</b>		<u>Value</u>	<u>Units</u>
Darcy Velocity	va	variable	m/a
Diffusion Coefficient	D	0.02	m <sup>2</sup> /a
Distribution Coefficient	К <sub>d</sub>	0.0	$cm^{3/g}$
Dispersivity ( $v_a < 0$ )		0.0	m
Dispersivity $(v_a > 0)$		0.4	m
Soil Porosity	n	0.4	-
Dry Density		1.5	g/cm <sup>3</sup>
Soil Layer Thickness	Н	4.0	m
Number of Sub-layers		12	-
Source Concentration	c <sub>o</sub>	1000	mg/L
Ref. Height of Leachate	H <sub>r</sub>	7.5	m
Volume of Leachate Collected	Q <sub>c</sub>	variable	m/a
Landfill Length	L	200.0	m
Landfill Width	W	1.0	m
Aquifer Thickness	h	1.0	m
Aquifer Porosity	nb	0.3	-
Aquifer Outflow Velocity	v <sub>b</sub> variat	ole	m/a

When using the Variable Properties special feature the accuracy of the solution is dependent on the number of sub-layers used.

This example is for a hypothetical landfill and is used to illustrate how to prepare an input file and run an analysis using the Variable Properties option. The example is not a prescription for modelling contaminant migration during operation and failure of a landfill. Each landfill has its own unique characteristics and no general prescription can be made. The Variable Properties option should only by used by someone with the hydrogeologic and engineering background necessary to appreciate the subtleties associated with the physical situation and the steps necessary for appropriate modelling of this physical situation.

# **Data Entry**

Start the POLLUTEv7 program and open the Examples project. Select Case 10 and open the model by double clicking on it in the model list. After the model is displayed, the data for the model can be displayed and edited using the Data Entry menu or by clicking on that part of the model.

### **General Data**

The general data for this example can be specified by either clicking on the title or selecting the General Data menu item from the Data Entry menu. In the General Data form below, the Darcy velocity can be specified if the Time-varying Properties special feature is used. Any Darcy velocity entered will be ignored.

General Data		
Title: Case 10: Time-varying velocity; ter	mination of leachate collection	
Number of Layers: 1	Maximum Depth: 5	m 💌
Laplace Transform Parameters		
TAU: 7 N: 20	SIG: 0	RNU: 2
🗸 ОК	X Cancel	<u>H</u> elp

l

### Layer Data

The layer data for the layer can be specified by either clicking on a layer or selecting the Layer Data menu item from the Data Entry menu. On this form the data for the layer can be added as shown below.

Layer Data			
	Layer Number		
Layer Data Layer Symbol			
Name: Aquitard			
Number of Sub Layers	12	Fractures	
Thickness	4 m	None	
Dry Density	1.5 g/cm3	C 1 Dimensional	
Porosity	0.4	C 2 Dimensional	
Coef of Hydro Disp	0.02 cm3/g	C 3 Dimensional	
Distribution Coef	0 m3/kg	-	
<b>~</b> (	)K 🔀 Can	cel <b>?</b> <u>H</u> elp	

## **Boundary Conditions**

The boundary conditions for the model can be specified by either clicking on the top or bottom boundary or selecting the Boundary Conditions menu item from the Data Entry menu. In this example, the top boundary has a finite mass and the bottom boundary is represented by a fixed outflow aquifer, as shown on the Boundary Condition form below. If the Time-varying Properties special feature has been selected, the Mass tab will not be shown and the source parameters will be entered in the Time-Varying Properties form. If the Time-varying Properties special feature has not been selected yet, any parameters entered on the Finite Mass tab will be ignored.

Boundary Conditi	ons	
Boundary Conditions	Bottom - Fixed Outflow Fixed Outflow Symbol	
	Landfill Length: 200 m 💌	
	Landfill Width: 1	
В	ase Thickness: 1 m 💌	
	Base Porosity: 0.3	
	<u>O</u> K <b>X</b> <u>C</u> ancel <b>?</b> <u>H</u> elp	

### **Run Parameters**

To set the times and depths to calculate the concentrations, select the Run Parameters menu item from the Data Entry menu. The concentrations can either be calculated at specified times or the time of the maximum concentration can be found. When the time-varying properties special feature is used the times to calculate the concentrations are specified in the Time-Varying Properties form. In this example the concentrations will be calculated at 5 depths: 0, 1, 2, 3, and 4 m.

# **Special Features**

The time-varying properties for this example is specified using the Special Features menu.

## **Time-Varying Properties**

To specify the time-varying properties, select the Time-Varying Properties menu item from the Special Features form. The Time-Varying Data tab on the Time-Varying Properties form shown below can be used to specify the number of time periods and whether there are variable layer properties and variable decay. In this example there are 3 time periods viz. 0 to 20 years, 20 to 30 years, and 30 to 130 years.

🗖 Time Varying I	Properties - 🗆 🗙
R	Time Period 1  ◀ ◀ ▶ ▶
Time Varying Data	Source Properties
Numbe	r of Time Periods
	Start Time 0
	Properties Increment within Periods
	Variable Layer Properties:
	C Yes G No
	Variable Decay:
	C Yes G No
	OK Cancel ? Help

### **Time Period 1**

The data for each time period is specified on the Source Properties tab shown below. In the first time period, specifying only one time increment means that the concentrations will only be calculated at the end time (i.e., 20 years). A negative Darcy velocity indicates the flow is upwards. Since the first time period corresponds to an operating leachate collection system and there is no additional mass entering the landfill; there is no increase in source concentration, Darcy velocity, Volume of Leachate Collected, or Base velocity.

🇖 Time Varying	g Properties		_		- O ×
		Time Perio	d  1		
Time Varying Data	Source Properties				
Specify	End Time	20	yr	-	
1	lumber of Increments	1			Increments
	Source Conc	1000	mg/L	-	0
	Darcy Velocity	-0.001	m/a	-	0
	Dispersivity	0	m	-	
	Base Velocity	2	m/a	•	0
	Rate for Conc	0	mg/L/yr	•	
	Volume Collected	0.3	m/a	•	0
And either	Waste Thickness	0	m	•	
	Waste Density	0	kg/m3	•	
	Proportion of Mass	0			
	Water Content	0			
	Conv Rate Half Life	0	yr	•	
rO	Ref Hight of Leach	7.5	m	•	
	<b>/</b> 0K	🗙 Cancel		<b>?</b> He	lo I
			_	3 110	P

### **Time Period 2**

The data for time period two can be specified by pressing the next button at the top of the form. This time period is from 20 to 30 years and is shown on the next page.Between the years 20 and 30 the velocities increase linearly with time, this will be approximated by a series of incremental increase at 1 year intervals. Thus there are 10 increments starting at year 21 and ending at year 30. Specifying the source concentration as -1 causes the calculated concentration at the end of the previous period to be used as the concentration at the beginning of this period.

The Darcy velocity and dispersivity are the values at the beginning of the time period. When operation of the leachate collection system is terminated the leachate mound begins to rise causing the Darcy velocity to reverse direction and become positive. A positive Darcy velocity results in the dispersivity becoming 0.4.

### Case 10: Time-varying Advective-dispersive Transport

The increment in Darcy velocity represents the change for each one year increment. Assuming the infiltration through the cover is constant the increment in the volume of leachate collected will be equal and opposite to the increment in the Darcy velocity. The increment in the base velocity is equal to the increment in the Darcy velocity multiplied by the length of the landfill (i.e., 0.0021 \* 200 = 0.42 m/a).

🗖 Time Varying	, Properties			- DX
		Time Perio	<b>d</b> 2	
Time Varying Data	Source Properties			
Specify	End Time	30	yr 🔻	•
N	lumber of Increments	10		 Increments
	Source Conc	-1	mg/L 💌	• 0
	Darcy Velocity	0	m/a 🔻	• 0.0021
	Dispersivity	0.4	m	·
	Base Velocity	2	m/a 💌	0.42
	Rate for Conc	0	mg/L/yr 💌	·
	Volume Collected	0.3	m/a 🗨	• 0.0021
And either	Waste Thickness	0	m	•
	Waste Density	0	kg/m3 🗨	·
	Proportion of Mass	0		
	Water Content	0		
	Conv Rate Half Life	0	уг 💌	·
Or	Ref Hight of Leach	7.5	m	·
	/ OK	✓ Canaal	2	Hab
		Lancel		нер

### Time Period 3

The data for time period three should be entered next, this time period is from 30 to 130 years and is shown on the next page. During the 100 years between 30 and 130 years the velocities remain constant. By specifying 10 increments the concentrations will be calculated and listed every 10 years during this period. The Darcy velocity is the resulting velocity from the build-up of leachate after the failure of the leachate collection system.

Since the leachate collection has completely failed by the start of this time period and the leachate mound has fully developed, there is no further increase in the velocities. Note that there will still be some leachate collected by the toe drains, which are assumed to be functioning even though the leachate collection system has failed.

The volume of leachate collected by the toe drains is equal to the infiltration through the cover minus the downward Darcy velocity (i.e., 0.3 - 0.021 = 0.279 m/a). And the base velocity is equal to the inflow plus the Darcy velocity times the landfill length (i.e., 2 + 200\*0.021 = 6.2 m/a).

### Case 10: Time-varying Advective-dispersive Transport

🗖 Time Varying	Properties	4			
		Time Perio	<b>d</b> 3		
Time Varying Data	Source Properties				
Specify	End Time	130	уг	•	
N	umber of Increments	10			Increments
	Source Conc	-1	mg/L	-	0
	Darcy Velocity	0.021	m/a	-	0
	Dispersivity	0.4	m	-	
	Base Velocity	6.2	m/a	-	0
	Rate for Conc	0	mg/L/yr	-	
	Volume Collected	0.279	m/a	•	0
And either	Waste Thickness	0	m	-	
	Waste Density	0	kg/m3	•	
	Proportion of Mass	0			
	Water Content	0			
	Conv Rate Half Life	0	уг	-	
Or	Ref Hight of Leach	7.5	m	-	
	и ок	🗙 Cancel		? He	lp

# **Model Execution**

To run the model and calculate the concentrations either select the Run menu item from the Execute menu or press the Run button on the toolbar.

# **Model Output**

After the model has been executed, the output for the model will be displayed. The initial display will depend on your settings in the program's preferences.

# **Concentration vs Depth**

The Concentration vs. Depth chart below can be displayed by pressing the Concentration vs Depth button on the Output toolbar or selecting the Concentration vs Depth menu item from the Output menu.



### **Output Listing**

To display the output as a text listing that will show the calculated concentrations as numbers, select the List Output menu item from the Output menu or press the Output Listing button on the Output toolbar.

### Case 10: Time-varying velocity; termination of leachate collection

#### THE VARIABLE VELOCITY AND/OR CONCENTRATION OPTION HAS BEEN USED NOTE THAT THE ACCURACY OF THE CALCULATIONS WITH THIS OPTION WILL DEPEND ON THE NUMBER OF SUBLAYERS USED

### Layer Properties

Layer	Thickness	Number of Sublayers	Coefficient of Hydrodynamic	Matrix Porosity	Distributon Coefficient	Dry Density
Aquitard	4 m	12	Dispersion 0.02 cm3/g	0.4	0 m3/kg	1.5 g/cm3
	•			Ī		

### **Boundary Conditions**

#### Finite Mass Top Boundary

#### Fixed Outflow Bottom Boundary

Landfill Length = 200 m Landfill Width = 1 m Base Thickness = 1 m Base Porosity = 0.3

### VARIATION IN PROPERTIES WITH TIME:

#### TIME PERIODS WITH THE SAME SOURCE AND VELOCITY

ſ	Period	Start Time	No. of	Time Step	Source Conc	Rate of	Height of	Volume
l			Steps	_		Change	Leachate	Collected
ſ	1	0 yr	1	20 yr	1000 mg/L	0	7.5 m	0.3 m/a
I	2	20 yr	10	1 yr	-1 mg/L	0	7.5 m	0.3 m/a
	3	30 ýr	10	10 yr	-1 mg/L	0	7.5 m	0.279 m/a

Period	Start Time	End Time	Darcy Velocity	Dispersivity	Base Velocity
1	O yr	20 yr	-0.001 m/a	0 m	2 m/a
2	20 yr	30 yr	0 m/a	. 0.4 m	. 2 m/a
3	30 yr	130 yr	0.021 m/a	0.4 m	6.2 m/a
		-			

Laplace Transform Parameters

**TAU =** 7 **N =** 20 **SIG =** 0 **RNU =** 2

### Calculated Concentrations at Selected Times and Depths

<b></b>	D == 4	<u> </u>
lime	Depth	Concentration
year	m	mg/L
20	0.000E+00 1.000E+00 2.000E+00 3.000E+00 4.000E+00	4.381E+02 1.739E+02 1.858E+01 5.903E-01 2.130E-03
21	0.000E+00 1.000E+00 2.000E+00 3.000E+00 4.000E+00	4.208E+02 1.762E+02 2.094E+01 7.799E-01 3.240E-03
22	0.000E+00 1.000E+00 2.000E+00 4.000E+00	4.042E+02 1.794E+02 2.391 <u>E+01</u> 1.416E-01
29	0.000E+00 1.000E+00 2.000E+00 3.000E+00 4.000E+00	3.052E+02 2.118E+02 6.485E+01 9.011E+00 2.393E-01
30	0.000E+00 1.000E+00 2.000E+00 2.000E+00 4.000E+00	2.933E+02 2.155E+02 7.342E+01 3.190E+01 3.955E-01
40	0.000E+00 1.000E+00 2.000E+00 3.000E+00 4.000E+00	1.977E+02 2.196E+02 1.466E+02 6.029E+01 1.003E+01
50	0.000E+00 1.000E+00 2.000E+00 3.000E+00 4.000E+00	1.339E+02 1.842E+02 1.687E+02 1.063E+02 3.505E+01
60	0.000E+00 1.000E+00	9.098E+01 1.449E+02

	3.000E+00 4.000E+00	1.298E+02 6.300E+01
70	0.000E+00 1.000E+00 2.000E+00 3.000E+00 4.000E+00	6.198E+01 1.106E+02 1.405E+02 1.336E+02 8.275E+01
80	0.000E+00 1.000E+00 2.000E+00 3.000E+00 4.000E+00	4.233E+01 8.308E+01 1.169E+02 1.253E+02 9.140E+01
90	0.000E+00 1.000E+00 2.000E+00 3.000E+00 4.000E+00	2.897E+01 6.184E+01 9.440E+01 1.108E+02 9.078E+01
100	0.000E+00 1.000E+00 2.000E+00 3.000E+00 4.000E+00	1.986E+01 4.577E+01 7.479E+01 9.434E+01 8.407E+01
110	0.000E+00 1.000E+00 2.000E+00 3.000E+00 4.000E+00	1.365E+01 3.377E+01 5.845E+01 7.812E+01 7.417E+01
120	0.000E+00 1.000E+00 2.000E+00 3.000E+00 4.000E+00	9.400E+00 2.486E+01 4.523E+01 6.338E+01 6.318E+01
130	0.000E+00 1.000E+00 2.000E+00 3.000E+00 4.000E+00	6.486E+00 1.829E+01 3.473E+01 5.061E+01 5.243E+01

# Case 11: Time-varying Source Concentration

# Description

In this example there is a time-varying source concentration history and diffusive transport of a conservative species (i.e., no sorption) from a landfill. Time zero corresponds to the excavation of a landfill cell, the cell then filled quickly with water to a depth of 6 m. No waste was added to the cell for 7 years. The landfill is situated in a clay that contains chloride in its pore water at a concentration of 120 mg/L. During the 7 years that the cell contained water the chloride began to diffused out of the clay pore water and into the cell water. Between the years 7 and 10, waste was added to the cell and the source concentration of chloride increased linearly with time reaching a peak value at year 10 of 2100 mg/L. The source concentration of chloride then remained relatively constant between the years 10 and 13. During the years 13 to 15 the source concentration decreased linearly with time to a value of 1180 mg/L at year 15. The source concentration then remained relatively constant again from years 15 to 19. This example will calculate the predicted chloride distribution with depth at year 19.

There is no leachate collection system in the landfill, and the water level in the waste corresponds to the natural water level. The hydraulic gradient is zero, and hence the Darcy velocity is zero. And the clay is sufficiently thick that it can be assumed to be infinite for the time period under consideration.

When using the Variable Properties special feature it is possible to independently specify the diffusion coefficient (Dm) and the dispersivity (). In this example the dispersivity is assumed to be zero since there is no flow. Clearly if there is no flow then the value of the dispersivity is not relevant since the coefficient of hydrodynamic dispersion (D) is then calculated by:

$$D = D_m + \alpha * v_a / n$$

The Reference Height of Leachate for this example is the same as the depth of water in the cell (i.e., 6 m). In this example the source concentration is assigned specific values at various times by setting the value of the Reference Height of Leachate very large. Setting the Reference Height of Leachate very large will ensure that the source concentration remains constant during that time interval.

Following are the parameters used in this example:

<u>Property</u>		<u>Value</u>	<u>Units</u>
Darcy Velocity	va	0.0	m/a
Diffusion Coefficient	D <sub>m</sub>	0.00663	$m^{2/a}$
Distribution Coefficient	К <sub>d</sub>	0.0	$cm^{3/g}$
Dispersivity		0.0	m
Soil Porosity	n	0.37	-

### Name of Section

<u>Property</u>		Value	<u>Units</u>
Dry Density		1.6	g/cm <sup>3</sup>
Soil Layer Thickness		infinite	m
Thickness of Interest	Н	1.5	m
Number of Sub- layers		15	-
Source Concentration	c <sub>o</sub>	variable	mg/L
Reference Height of Leachate	H <sub>r</sub>	6.0	m
Volume of Leachate Collected	Q <sub>c</sub>	0.0	m/a

When using the Variable Properties special feature the accuracy of the solution is dependent on the number of sub-layers used.

This example is for a hypothetical landfill and is used to illustrate how to prepare an input file and run an analysis using the Variable Properties option. The example is not a prescription for modelling contaminant migration from a landfill. Each landfill has its own unique characteristics and no general prescription can be made. The Variable Properties option should only by used by someone with the hydrogeologic and engineering background necessary to appreciate the subtleties associated with the physical situation and the steps necessary for appropriate modelling of this physical situation.

# **Data Entry**

Start the POLLUTEv7 program and open the Examples project. Select Case 11 and open the model by double clicking on it in the model list. After the model is displayed, the data for the model can be displayed and edited using the Data Entry menu or by clicking on that part of the model.

### **General Data**

The general data for this example can be specified by either clicking on the title or selecting the General Data menu item from the Data Entry menu. In the General Data form on the next page, the Darcy velocity can not be specified if the Time-varying Properties special feature is used. Any Darcy velocity entered will be ignored.

L

General Data	
Title: Juase TT: Variable source concentrati	on history
Number of Layers: 1	Maximum Depth: 1.5 m 🗨
Laplace Transform Parameters	
TAU: 7 N: 20	SIG: 0 BNU: 2
	Cancel ? Help

### Layer Data

The layer data for the layer can be specified by either clicking on a layer or selecting the Layer Data menu item from the Data Entry menu. On this form the data for the layer can be added as shown below. Although the clay layer is assumed to be infinite, the concentrations for only the top 1.5 m will be calculated. This is the depth interval where the contaminant plume is expected.

Layer Data			
	Layer	Number 1	
Layer Data Layer Symbol			
Name: Clay	7		
Number of Sub Layers	15		Fractures
Thickness	1.5	m	None
Dry Density	1.6	g/cm3 💌	C 1 Dimensional
Porosity	0.37		C 2 Dimensional
Coef of Hydro Disp	0.00663	cm3/g 💌	C 3 Dimensional
Distribution Coef	0	m3/kg 💌	
	ок .	🗙 Cancel	<b>?</b> <u>H</u> elp

### **Boundary Conditions**

The boundary conditions for the model can be specified by either clicking on the top or bottom boundary or selecting the Boundary Conditions menu item from the Data Entry menu. In this example, the top boundary has a finite mass and the bottom boundary is represented by a layer of infinite thickness, as shown on the Boundary Condition form below. If the Time-varying Properties special feature has been selected, the Finite Mass tab will not be shown and the source parameters will be entered in the Time-Varying Properties form. If the Time-varying Properties special feature has not been selected yet, any parameters entered on the Finite Mass tab will be ignored.

Boundary Conditions	
Boundary Conditions	
Top Boundary	Zero Flux     Constant Concentration     Finite Mass
Bottom Boundary	<ul> <li>Zero Flux</li> <li>Constant Conc</li> <li>Fixed Outflow Velocity</li> <li>Infinite Thickness</li> </ul>
<u> Ф</u> К	X ⊆ancel ? Help

### **Run Parameters**

To set the times and depths to calculate the concentrations, select the Run Parameters menu item from the Data Entry menu. The concentrations can either be calculated at specified times or the time of the maximum concentration can be found. When the time-varying properties special feature is used the times to calculate the concentrations are specified in the Time-Varying Properties form.

# **Special Features**

The initial concentration profile and time-varying properties for this example are specified using the Special Features menu.

### **Initial Concentration Profile**

To specify the initial concentration profile, select the Initial Concentration Profile menu item from the Special Features form. The Concentration Profile tab on the form shown on the next page can be used to specify the type of profile as either Depth Intervals or Sublayers. The concentration profile can be specified as a constant for given depth intervals or as a different value for every sublayer.

Initial Concentration Profile	-			
Concentration Profile Deth Intervals				
Start Time 🔟 Flux into Soil 0 Flux into Base 0	ул <b>т</b> m2/a <b>т</b> m2/a <b>т</b>			
Type of Profile      O Depth Intervals     Number of Depth Intervals				
V OK X Cancel	? Help			

In this example the background concentration is uniform with depth, and can be specified as a constant 120 mg/L over 1 depth interval.

Initial Concentration Profile						
Concentration Profile	Depth Intervals					
Depth Interva	al 💦 🚺	4 4 🕨 🕨				
Top Depth	q	m				
Bottom Depth	1.5	m 💌				
Concentration	120	mg/L 💌				
🖌 ОК	🗙 Cancel	? Help				

### **Time-Varying Properties**

To specify the time-varying properties, select the Time-Varying Properties menu item from the Special Features form. The Time-Varying Data tab on the Time-Varying Properties form shown below can be used to specify the number of time periods and whether there are variable layer properties and variable decay. In this example there are 5 time periods viz. 0 to 7 years, 7 to 10 years, 10 to 13 years, 13 to 15 years, and 15 to 19 years.

🗖 Time Varying Pro	perties				
	D	Time Peri	od 1		< > >
Time Varying Data So	urce Properties	Ī			
Number of	Time Periods	3			
	Start Time	0	lur	-	
	otal Time	•	μ.	<u> </u>	
F	Properties Increr	ment within Pe	eriods		
	C Yes	œ	No		
L [\	/ariable Layer P	roperties:			
	C Yes	۲	No		
	(				
L L	ariable Decay:				
	C Yes	e	No		
	_		1		1
✓ 0	<u> </u>	🗙 Cancel		7 Help	

### **Time Period 1**

The data for each time period is specified on the Source Properties tab shown on the next page. In the first time period, specifying only one time increment means that the concentrations will only be calculated at the end time (i.e., 7 years). The beginning source concentration is zero, since fresh water is initially filling the cell.

🗖 Time Varying	蓮 Time Varying Properties					
		Time Perio	d  1		< > >	
Time Varying Data	Source Properties					
Specify	EnATime	7	yr	•		
N	lumber of Increments	1				
	Source Conc	0	mg/L	-		
	Darcy Velocity	0	m/a	•		
	Dispersivity	0	m	-		
	Base Velocity	0	m/a 🔤	-		
	Rate for Conc	0	mg/L/yr	-		
	Volume Collected	0	m/a	-		
And either	Waste Thickness	0	m	-		
	Waste Density	0	kg/m3	-		
	Proportion of Mass	0				
	Water Content	0				
	Conv Rate Half Life	0	уг	•		
Or	Ref Hight of Leach	6	m	•		
	/ ОК	🗙 Cancel		<b>?</b> Help		

### **Time Period 2**

The data for time period two can be specified by clicking on the next arrow at the top of the form. This time period is from 7 to 10 years, and is shown below. Between the years 7 and 10 the source concentration increase linearly with time at a rate of 700 mg/L per year.

Only one time increment is necessary, since we are not interested in calculating the concentrations at any intermediate times. Specifying the source concentration as -1 causes the calculated concentration at the end of the previous period to be used as the concentration at the beginning of this period. The Leachate Reference Height is set very high in order to ignore the effects of source depletion.

🗖 Time Varying Properties 📃 🗆 🗙						
		Time Perio	d 2		${}^{\bullet}\!$	M
Time Varying Data	Source Properties					
Specify	End Time	h0	yr	•		
N	lumber of Increments	1				
	Source Conc	-1	mg/L	•		
	Darcy Velocity	0	m/a	-		
	Dispersivity	0	m	•		
	Base Velocity	0	m/a	•		
	Rate for Conc	700	mg/L/yr	•		
	Volume Collected	0	m/a	-		
And either	Waste Thickness	0	m	•		
	Waste Density	0	kg/m3	-		
	Proportion of Mass	0				
	Water Content	0				
	Conv Rate Half Life	0	уг	•		
rO	Ref Hight of Leach	1E15	m	-		
	ОК	🗙 Cancel		? Help	,	

### **Time Period 3**

Next the data for time period three should be entered, this time period is from 10 to 13 years, and is shown below. During the 3 years between 10 and 13 years the source concentration remains constant.

Specifying the beginning concentration as -1 indicates to use the calculated concentration at the end of the previous time period as the concentration at the start of this time period. The Leachate Reference Height is set very high in order to ignore the effects of source depletion.

🗖 Time Varying	🕫 Time Varying Properties 📃 🗖 🗙					
		Time Perio	<b>d</b> 3		• •	
Time Varying Data	Source Properties					
Specify	End Time	<u> 13</u>	yr	-		
N	umber of Increments	1				
	Source Conc	-1	mg/L	-		
	Darcy Velocity	0	m/a	•		
	Dispersivity	0	m	•		
	Base Velocity	0	m/a	•		
	Rate for Conc	0	mg/L/yr	-		
	Volume Collected	0	m/a	•		
And either	Waste Thickness	0	m	•		
	Waste Density	0	kg/m3	•		
	Proportion of Mass	0				
	Water Content	0				
	Conv Rate Half Life	0	yr	•		
10	Ref Hight of Leach	1E15	m	•		
	/ OK	🗙 Cancel	1	<b>?</b> Help		

### Time Period 4

Next the data for time period four should be entered as shown on the form below, this time period is from 13 to 15 years. Between the years 13 and 15 the source concentration decreases linearly with time at the rate of 460 mg/L per year.

Specifying the beginning concentration as -1 indicates to use the calculated concentration at the end of the previous time period as the concentration at the start of this time period. The Leachate Reference Height is set very high in order to ignore the effects of source depletion.

🗖 Time Varying	🗖 Time Varying Properties					
		Time Perio	d 4		• •	M
Time Varying Data	Source Properties					
Specify	TN End Time	þ5	уг	-		
N	umber of Increments	1				
	Source Conc	-1	mg/L	•		
	Darcy Velocity	0	m/a	-		
	Dispersivity	0	m	•		
	Base Velocity	0	m/a	-		
	Rate for Conc	-460	mg/L/yr	•		
	Volume Collected	0	m/a	-		
And either	Waste Thickness	0	m	•		
	Waste Density	0	kg/m3	-		
	Proportion of Mass	0				
	Water Content	0				
	Conv Rate Half Life	0	yr	•		
Or	Ref Hight of Leach	1E15	m	•		
	ГОК	🗙 Cancel		? Help		

### **Time Period 5**

Data for the last time period should be entered, this time period is from 15 to 19 years. For the 4 years between 15 and 19 the source concentration is assumed to remain constant at 1180 mg/L. The Leachate Reference Height is set very high in order to ignore the effects of depletion of the source.

🗖 Time Varying	Properties						
		Time Period	I 5		• •		M
Time Varying Data	Source Properties						
Specify	End Time	19	yr	-			
N	umber of Increments	1	·				
	Source Conc	1180	mg/L	-			
	Darcy Velocity	0	m/a	•			
	Dispersivity	0	m	-			
	Base Velocity	0	m/a	•			
	Rate for Conc	0	mg/L/yr	•			
	Volume Collected	0	m/a	•			
And either	Waste Thickness	0	m	•			
	Waste Density	0	kg/m3	•			
	Proportion of Mass	0					
	Water Content	0					
	Conv Rate Half Life	0	yr	•			
Or	Ref Hight of Leach	1E15	m	-			
	/ ОК	🗙 Cancel		?н	elp	]	

# **Model Execution**

To run the model and calculate the concentrations either select the Run menu item from the Execute menu or press the Run button on the toolbar.

# **Model Output**

After the model has been executed, the output for the model will be displayed. The initial display will depend on your settings in the program's preferences.

# **Concentration vs Depth**

The Concentration vs. Depth chart below can be displayed by pressing the Concentration vs Depth button on the Output toolbar or selecting the Concentration vs Depth menu item from the Output menu.



# **Output Listing**

To display the output as a text listing that will show the calculated concentrations as numbers, select the List Output menu item from the Output menu or press the Output Listing button on the Output toolbar.

### Case 11: Variable source concentration history

# THE VAR $\breve{A}$ BLE VELOCITY AND/OR CONCENTRATION OPTION HAS BEEN USED NOTE THAT THE ACCURACY OF THE CALCULATIONS WITH THIS OPTION WILL DEPEND ON THE NUMBER OF SUBLAYERS USED

### Layer Properties

	Layer	Thickness	Number of Sublayers	Coefficient of Hydrodynamic Dispersion	∦Matrix Porosity )	Distributon Coefficient	Dry Density
ſ	Clay	1.5 m	15	0.00663 cm3/g	0.37	0 m3/kg	1.6 g/cm3

### **Boundary Conditions**

#### Finite Mass Top Boundary

Infinite Thickness Bottom Boundary

### INITIAL CONCENTRATION PROFILE

Time = 0 yr Flux into Soil = 0 m2/a Flux into Base = 0 m2/a

Top Depth	Bottom Depth	Concentration
0 m	1.5 m	120 mg/L

### VARIATION IN PROPERTIES WITH TIME:

#### TIME PERIODS WITH THE SAME SOURCE AND VELOCITY

Period	Start Time	No. of	Time Step	Source Conc	Rate of	Height of	Volume
		Steps			Change	Leachate	Collected
1	O yr	1	7 yr	0 mg/L	0	6 m	0 m/a
2	7 yr	1	3 yr	-1 mg/L	700	1E15 m	0 m/a
3	10 yr	1	3 yr	-1 mg/L	0	1E15 m	0 m/a
4	13 yr	1	2 yr	-1 mg/L	-460	1E15 m	0 m/a
5	15 yr	1	4 yr	1180 mg/L	0	1E15 m	0 m/a
	_		_	_			

Period	Start Time	End Time	Darcy Velocity	Dispersivity	Base Velocity
1	0 yr	7 yr	0 m/a	0 m	0 m/a
2	7 yr	10 yr	0 m/a	0 m	0 m/a
3	10 yr	13 ýr	0 m/a	0 m	0 m/a
4	13 ýr	15 ýr	0 m/a	0 m	0 m/a
5	15 ýr	19 ýr	0 m/a	0 m	0 m/a
	, í				

Laplace Transform Parameters

**TAU =** 7 **N =** 20 **SIG =** 0 **RNU =** 2

### Calculated Concentrations at Selected Times and Depths

Time	Depth	Concentration	
year	m	mg/L	
7	0.000E+00	1.778E+00	
	1.000E-01	3.201E+01	
		5.930E+01	
	3.000E-01	8.141E+UI 9.749E+01	
		9.7490+01	
		1.1420702	
	8.000E-01	1.1740702	
	9,00002-01	1.196E+02	
	1 000E+00	1 199E+02	
	1 100E+00	1 200E±02	
	1 200E+00	1 200E+02	
	1.300E+00	1.200E+02	
	1.400E+00	1.200E+02	
	1.500E+00	1.200E+02	
		-	
10	0.000E+00	2.102E+03	
	1.000E-01	9.048E+02	
	2.000E-01	3.644E+02	
	3.000E-01	1.653E+02	
	4.000E-01	1.107E+02	
	5.000E-01	1.042E+02	
	6.000E-01	1.086E+02	
	7.000E-01	1.134E+02	
	8.000E-01	1.165E+02	
	9.000E-01	1.183E+02	
	1.000E+00	1.192E+02	
		1.197E+02	
		1.1990-102	
		1.2000-102	
	1.400E+00	1.200E+02	
	1.3082.108	1.2002 102	
13	0.000E+00	2.102E+03	
	1.000E-01	1.449E+03	
	2.000E-01	9.023E+02	
	3.000E-01	5.194E+02	
	4.000E-01	2.937E+02	
	5.000E-01	1.816E+02	
	6.000E-01	1.351E+02	

	l 6.000E-01 7.000E-01 8.000E-01 9.000E-00 1.000E+00 1.100E+00 1.200E+00 1.300E+00 1.400E+00 1.500E+00	I 1.351E+02 1.188E+02 1.168E+02 1.171E+02 1.182E+02 1.182E+02 1.190E+02 1.195E+02 1.198E+02 1.199E+02 1.200E+02
15	1         0.000E+00           1.000E-01         2.000E-01           2.000E-01         3.000E-01           4.000E-01         6.000E-01           6.000E-01         6.000E-01           7.000E-01         8.000E-01           9.000E-01         1.000E+00           1.000E+00         1.100E+00           1.300E+00         1.300E+00           1.400E+00         1.500E+00	1.182E+03 1.247E+03 9.934E+02 6.826E+02 2.763E+02 1.879E+02 1.267E+02 1.267E+02 1.267E+02 1.288E+02 1.188E+02 1.188E+02 1.188E+02 1.192E+02 1.196E+02 1.198E+02 1.198E+02 1.199E+02
19	0.000E+00 1.000E-01 2.000E-01 3.000E-01 4.000E-01 5.000E-01 6.000E-01 7.000E-01 8.000E-01 1.000E+00 1.100E+00 1.200E+00 1.300E+00 1.400E+00 1.500E+00	1.180E+03 1.030E+03 8.730E+02 7.092E+02 5.501E+02 4.104E+02 3.005E+02 2.232E+02 1.740E+02 1.457E+02 1.240E+02 1.240E+02 1.241E+02 1.20E+02 1.298E+02 1.198E+02

Ι

#### NOTICE

Although this program has been tested and experience would indicate that it is accurate within the limits given by the assumptions of the theory used, we make no warranty as to workability of this software or any other licensed material. No warranties either expressed or implied (including warranties of fitness) shall apply. No responsibility is assumed for any errors, mistakes or misrepresentations that may occur from the use of this computer program. The user accepts full responsibility for assessing the validity and applicability of the results obtained with this program for any specific case.

# Case 12: POLLUTE vs. Analytical Solution

# Description

The results obtained from POLLUTE are compared to those obtained by an analytical solution developed by Tang et al. (1981) for a single fracture system. A conservative contaminant is considered with a constant source concentration of 1. The fractures are 10  $\mu$ m wide, have a groundwater (seepage) velocity along the fracture of 730 m/a, a dispersivity of zero, and a diffusion coefficient along the fractures of 0.077 m<sup>2</sup>/a. In this comparison the fracture spacing is 1 m. Because of the very low matrix diffusion coefficient there is no interaction between fractures over the time frame considered, thus the same result would be obtained if the fracture spacing were increased to 10 m. The Darcy velocity, which occurs along the fractures, can be calculated by multiplying the fractures per m times the fracture width times the seepage velocity:

$$v_a = 10x10^{-6} * 1 * 730 = 0.73x10^{-2}$$

A porosity of 0.05 and tortuosity (the ratio of effective diffusion coefficient to the molecular diffusion coefficient in water) of 0.0000983 were assumed for the matrix material. The matrix diffusion coefficient is then given by multiplying the fracture diffusion coefficient and the tortuosity:

 $D_m = 0.077 * 0.0000983 = 7.5691 \times 10^{-6}$ 

The following parameters are defined for this example:

<b>Property</b>		<u>Value</u>	<u>Units</u>
Darcy Velocity	va	0.73E-2	m/a
Soil Thickness	Н	400.0	m
Number of Sub-layers		4	-
Fracture spacing	2H <sub>1</sub>	1.0	m
Fracture opening	2h <sub>1</sub>	10E-6	m
Dispersion along fractures	$D_{f}$	0.077	m <sup>2</sup> /a
Fracture Distribution Coef.	K <sub>f</sub>	0.0	$cm^{3}/g$
Matrix Diffusion Coefficient	D <sub>m</sub>	7.57E-6	m <sup>2</sup> /a
Matrix Distribution Coef.	К <sub>m</sub>	1.0	$\mathrm{cm}^{3}/\mathrm{g}$
Matrix Porosity	n <sub>m</sub>	0.05	-
Dry Density of Matrix		0.0	g/cm <sup>3</sup>
Source Concentration	co	1.0	mg/L

# **Data Entry**

Start the POLLUTEv7 program and open the Examples project. Select Case 12 and open the model by double clicking on it in the model list. After the model is displayed, the data for the model can be displayed and edited using the Data Entry menu or by clicking on that part of the model.

### **General Data**

The general data for this example can be specified by either clicking on the title or selecting the General Data menu item from the Data Entry menu. In the General Data form on the next page, the Darcy velocity can be specified as  $0.73 \times 10^{-2}$ .

General Data
Title: Case 12: POLLUTE vs Analytical solution
Number of Layers: 1 Maximum Depth: 400 m
Darcy Velocity: 0.0073 m/year 💌
Laplace Transform Parameters
TAU: 7 N: 20 SIG: 0 RNU: 2
✓ OK X Cancel ? Help

### Layer Data

The layer data for the layer can be specified by either clicking on a layer or selecting the Layer Data menu item from the Data Entry menu. On this form, shown on the next page, the data for the layer can be added.

1

Layer Data	
Layer Number	
Layer Data Layer Symbol   1 immensional Fractures	
Name: Soil	
Number of Sub Layers 4	Fractures
Thickness 400 m	▼ ○ None
Dry Density 0 g/cm3	1 Dimensional
Porosity 0.05	C 2 Dimensional
Coef of Hydro Disp 7.569E-6 m2/a	C 3 Dimensional
Distribution Coef 0 m3/kg	
🗸 ОК 🛛 🗶 Са	ncel ? Help

On the Fractures tab, the data for the one dimensional fractures can be specified. The fracture opening size is the gap between the walls of the fracture.

Layer Data
Layer Number 1     + > >
Layer Data Layer Symbol 1 Dimensional Fractures
Dimension
Spacing 1 m
Opening Size 1E-5 m
Number to Sum 10
Dispersion coefficient 0.077 m2/a
Distirubition Coefficient 0 m3/kg
✓ OK X Cancel ? Help
## **Boundary Conditions**

The boundary conditions for the model can be specified by either clicking on the top or bottom boundary or selecting the Boundary Conditions menu item from the Data Entry menu. In this example, the top boundary has a constant concentration and the bottom boundary is represented by a layer of infinite thickness, as shown on the Boundary Condition form below.

Boundary Conditions				
Boundary Conditions	Top - Constant Conc.			
Constan	t Top Concentration: 1			
	<u>OK</u> ∑ancel ? <u>H</u> elp			

## **Run Parameters**

To set the times and depths to calculate the concentrations, select the Run Parameters menu item from the Data Entry menu. The Run Parameters form on the next page will be displayed. The concentrations can either be calculated at specified times or the time of the maximum concentration can be found. In this example the concentrations will be calculated at 25 years and at 4 depths: 100, 200, 300, and 400 m.

Run Parameters
Type Concentrations at Recified Times
Times     Number of Times:     1       Number:     1     I     I       Time:     25     year     I
All Depths     Number of Depths:       ○ Yes     Number:       ○ No     Depth:
Cancel ? Help

## **Special Features**

The maximum sublayer thickness for this example can be specified using the Special Features menu.

## **Maximum Sublayer Thickness**

The default maximum sublayer thickness is 5 depth units. This maximum is set to avoid problems with exponential overflow, which can sometimes occur if the sublayers are too thick. To override the default maximum sublayer thickness the Maximum Sublayer Thickness feature is used, when over riding this default the user takes the chance that the program will "crash" or give false results - caveat emptor.

Maximum Sublayer Thickness				
Information				
Maximum Sublayer Thickness - When overriding the default the program may crash or give false results				
Maximum Layer Thickness 1100.01				
Cancel ? Help				

### Case 12: POLLUTE vs Analytical Solution

To specify the maximum sublayer thickness select the Maximum Sublayer Thickness menu item from the Special Features menu, the Maximum Sublayer Thickness form on the previous page will be shown. By specifying the maximum sublayer thickness as 100.01 the sublayers can be up to 100.01 units thick. In this example the sublayers are 100 units thick.

## **Model Execution**

To run the model and calculate the concentrations either select the Run menu item from the Execute menu or press the Run button on the toolbar.

## **Model Output**

After the model has been executed, the output for the model will be displayed. The initial display will depend on your settings in the program's preferences.

## **Output Comparison**

The calculated concentrations from the POLLUTE program and the analytical solution by Tang et al. (1981) are listed below. Both solutions give identical results.

Depth	POLLUTE	Analytical Solution
(m)	(mg/L)	(mg/L)
100	0.5930	0.5930
200	0.2838	0.2838
300	0.1069	0.1069
400	0.0311	0.0311

## **Concentration vs Depth**

The Concentration vs. Depth chart below can be displayed by pressing the Concentration vs Depth button on the Output toolbar or selecting the Concentration vs Depth menu item from the Output menu.



## **Output Listing**

To display the output as a text listing that will show the calculated concentrations as numbers, select the List Output menu item from the Output menu or press the Output Listing button on the Output toolbar.

### Case 12: POLLUTE vs Analytical solution --single fracture

#### THE DARCY VELOCITY (Flux) THROUGH THE LAYERS Va = 0.0073 m/year

#### Layer Properties

Layer	⊥ Thickness	Number of Sublayers	Coefficient of Hydrodynamic Dispersion	Matrix Porosity	Distributon Coefficient	Dry Density
Soil	400 m	4	7.569E-6 m2/a	0.05	0 m3/kg	0 g/cm3

Layer	Fracture Spacing 1	Opening Size 1	Number 1	Fracture Spacing 2	Opening Size 2	Number 2	Fracture Spacing 3	Opening Size 3	Number 3
Soil	1 m	1E-5 m	10						

Layer	Dispersion Coefficient in Fractures	Distribution Coefficient in Fractures	Fracture Porosity	Retardation Coefficient in Matrix
Soil	0.077 m2/a	0 m3/kg	1.0000E-05	1.0000E+00

#### **Boundary Conditions**

#### **Boundary Conditions**

Contant Concentration

Source Concentration = 1 mg/L

#### Infinite Thickness Bottom Boundary

**TAU =** 7 **N =** 20 **SIG =** 0 **RNU =** 2

#### Calculated Concentrations at Selected Times and Depths

Time	Depth	Concentration
year	m	mg/L
τ 25	0.000E+00	1.000E+00
L 7	[ 1.000E+02	5.930E-01
	2.000E+02	2.838E-01
	3.000E+02	1.069E-01
	4.000E+02	3.111E-02

# Case 13: Comparison with Analytical Method

## Description

In this example the results of POLLUTE are compared to those obtained by the analytical solution given by TDAST. TDAST is a computer program for 2-D plane dispersion in an infinitely deep porous media, developed by Javandel et al. (1984). An infinitely thick layer is considered, however for comparison purposes the calculations will be restricted to the first 10 m. Below the layer the bottom boundary is assumed to extend to infinity and have the same properties as the layer above. The following parameters are assumed for the example:

<u>Property</u>		<u>Value</u>	<u>Units</u>
Darcy Velocity	va	1.0	m/a
Diffusion Coefficient	D	0.01	m <sup>2</sup> /a
Distribution Coefficient	К <sub>d</sub>	0.0	$cm^{3/g}$
Soil Porosity	n	1.0	-
Dry Density		0.0	g/cm <sup>3</sup>
Soil Layer Thickness	Н	10.0	m
Number of Sub-layers		20	-
Source Concentration	c <sub>o</sub>	1.0	g/L
Times of Interest	t	4	a

## **Data Entry**

Start the POLLUTEv7 program and open the Examples project. Select Case 13 and open the model by double clicking on it in the model list. After the model is displayed, the data for the model can be displayed and edited using the Data Entry menu or by clicking on that part of the model.

## **General Data**

The general data for this example can be specified by either clicking on the title or selecting the General Data menu item from the Data Entry menu. The General Data form on the next page will be displayed. In this example there is one layer and the Darcy velocity is 1 m/a.

l

General Data			
Title: JLase 13: Comparison with an analytical method.			
Number of Layers: 1 Maximum Depth: 10 m			
Darcy Velocity: 1 m/year 💌			
Laplace Transform Parameters			
TAU: 7 N: 100 SIG: 0 RNU: 10			
✓ OK Cancel ? Help			

## Layer Data

The layer data for the layer can be specified by either clicking on a layer or selecting the Layer Data menu item from the Data Entry menu. When there is no sorption (i.e., the distribution coefficient is zero) the dry density is not used and can be specified as zero.

Layer Data	
Layer Number 1	
Layer Data Layer Symbol	
Name:  Soil	
Number of Sub Layers 20	Fractures
Thickness 10 m 💌	None
Dry Density 0 g/cm3 💌	C 1 Dimensional
Porosity 1	C 2 Dimensional
Coef of Hydro Disp 0.01 m2/a 💌	C 3 Dimensional
Distribution Coef 0 m3/kg 💌	
V OK Cancel	? Help

## **Boundary Conditions**

The boundary conditions for the model can be specified by either clicking on the top or bottom boundary or selecting the Boundary Conditions menu item from the Data Entry menu. In this example, the top boundary has a constant concentration and the bottom boundary is represented by a layer of infinite thickness, as shown on the Boundary Condition form below.

Boundary Conditi	ons		
Boundary Conditions	Top - Constant Conc.		
Constan	t Top Concentration: 1	mg/L 💌	
	<u>D</u> K X Canc	sel <b>?</b> Help	

## **Run Parameters**

To set the times and depths to calculate the concentrations, select the Run Parameters menu item from the Data Entry menu. The Run Parameters form on the next page will be displayed. The concentrations can either be calculated at specified times or the time of the maximum concentration can be found. In this example the concentrations will be calculated at 4 years and at 14 depths from 0.5 to 10 m.

Run Parameters
Type Concentrations at Specified Times
Times Number of Times: 1 Number: 1 I I I I I I I Time: 4
All Depths     Number of Depths:     15       ○ Yes     Number:     1     I     I     I     I       Image: No     Depth:     0.5     Image: Im
✓ OK X Cancel ? Help

## **Model Execution**

To run the model and calculate the concentrations either select the Run menu item from the Execute menu or press the Run button on the toolbar.

## **Model Output**

After the model has been executed, the output for the model will be displayed. The initial display will depend on your settings in the program's preferences.

## **Concentration vs Depth**

The Concentration vs. Depth chart on the next page can be displayed by pressing the Concentration vs Depth button on the Output toolbar or selecting the Concentration vs Depth menu item from the Output menu.

### **Case 13: Comparison with Analytical Method**



The results of the POLLUTE program are compared to those obtained by the TDAST program in the figure below. Concentrations obtained by both methods are in close agreement for a dispersion coefficient of 0.01 m2/a. However, it should be noted that at higher values of dispersion coefficient, for example 5 or 10 m<sup>2</sup>/a, the POLLUTE program will not give the same result as TDAST. This is because POLLUTE considers only 1-dimensional migration in the layer below the source, whereas TDAST considers 2-dimensional migration.

## **Output Listing**

To display the output as a text listing that will show the calculated concentrations as numbers, select the List Output menu item from the Output menu or press the Output Listing button on the Output toolbar.

## Case 13: Comparison with an analytical method.

THE DARCY VELOCITY (Flux) THROUGH THE LAYERS Va = 1 m/year

#### Layer Properties

Layer	Thickness	Number of Sublayers	Coefficient of Hydrodynamic Dispersion	Matrix Porosity	Distributon Coefficient	Dry Density
Soil	10 m	20	0.01 m2/a	1	0 m3/kg	0 g/cm3

#### Boundary Conditions

Ι

Contant Concentration Source Concentration = 1 mg/L

Infinite Thickness Bottom Boundary

#### Laplace Transform Parameters

**TAU** = 7 **N** = 100 **SIG** = 0 **RNU** = 10

#### Calculated Concentrations at Selected Times and Depths

Time	Depth	Concentration
year	m m	mg/L
4	0.000E+00	1.000E+00
	5.000E-01	1.000E+00
	1.000E+00	1.000E+00
	1.500E+00	1.000E+00
	2.000E+00	1.000E+00
	2.500E+00	1.000E+00

3.000E+00 3.500E+00	9.998E-01 9.646E-01
4.000E+00	5.141E-01
	4.133E-02
6.000E+00	1.928E-09
7.000E+00	1.927E-09
8.000E+00	1.927E-09
9.000E+00 1.000E+01	1.927E-09 1.927E-09
1.0002.101	1.021 E-00

#### NOTICE

Although this program has been tested and experience would indicate that it is accurate within the limits given by the assumptions of the theory used, we make no warranty as to workability of this software or any other licensed material. No warranties either expressed or implied (including warranties of fitness) shall apply. No responsibility is assumed for any errors, mistakes or misrepresentations that may occur from the use of this computer program. The user accepts full responsibility for assessing the validity and applicability of the results obtained with this program for any specific case.

# **Case 14: Primary and Secondary Collection**

## Description

In this example a landfill with both a primary and a secondary leachate collection system is modelled using the Passive Sink special feature. The landfill contains a finite mass of a conservative contaminant species, and is underlain by an aquifer with fixed outflow. A passive sink is used to model the secondary leachate collection system, which is assumed to be composed of a 0.3 m thick granular layer. The Darcy velocity is assumed to be 0.01 m/a downward from the landfill to the secondary leachate collection system, and 0.0 m/a between the secondary leachate collection system and the aquifer (i.e., the water table is assumed to be at the base of the secondary leachate collection system).

The analysis starts at time zero which corresponds to the completion of the landfill and the development of a peak leachate concentration ( $c_0$ ) of 1000 mg/L. It is assumed that the average waste thickness is 6.25 m with a density of 600 kg/m3, and that the contaminant represents 0.2% of the total mass of the waste. Thus the total mass of contaminant per unit area of landfill is:

$$m_{tc} = 0.002 * 600 * 6.25 = 7.5 \text{ kg/m}^2$$

The Reference Height of Leachate  $(H_r)$  is then calculated by dividing the total mass of contaminant per unit area  $(m_{tc})$  by the contaminant concentration  $(c_0)$ .

$$H_r = 0.002 * 600 * 6.25 / 1 = 7.5 m$$

It is also assumed that the peak concentration in the landfill is reached relatively early in the life of the landfill, and that the analysis starts at this time. Consequently there is no increase in concentration with time and the Rate of Increase in Concentration  $(c_r)$  with time is zero.

The average infiltration through the cover  $(q_0)$  is assumed to be 0.3 m/a. If the average exfiltration through the base of the landfill  $(v_a)$  is 0.01 m/a, then the Volume of Leachate Collected is:

$$Q_c = q_0 - v_a = 0.3 - 0.01 = 0.29 \text{ m/a}$$

The strata beneath the landfill consists of a 1 m clay layer, a 0.3 m granular layer (i.e., secondary leachate collection system), a 2 m aquitard layer, underlain by a 1 m thick aquifer. The landfill is assumed to be 200 m long in the direction parallel to the groundwater flow in the aquifer. At the up gradient edge of the landfill the inflow in the aquifer is given by a Darcy velocity of 4 m/a.

#### **Case 14: Primary and Secondary Leachate Collection**

The outflow Darcy velocity at the down gradient edge of the landfill  $(v_b)$  is then by multiplying the landfill length (200 m) by the Darcy velocity below the secondary leachate collection system (0.0 m/a) and adding the inflow, viz:

$$v_b = 4 + 200 / 1 * v_a = 4 m/a$$

When using the Passive Sink Properties special feature the deposit is divided into layers which can have vertical and horizontal flows In the example 3 layers are necessary, the first is from the base of the landfill to the top of the secondary leachate collection system, the second is the secondary leachate collection system, and the third is from the base of the secondary leachate collection system to the aquifer. In the first layer there is a vertical downwards Darcy velocity of 0.01 m/a and no horizontal flow. The second layer has a horizontal flow which is equal to the difference in Darcy velocity between the layers above and below, multiplied by the landfill length and divided by the layer thickness, viz:

 $v_s = (v_{a1} - v_{a2}) * L/h = (0.01 - 0.0) * 200 / 0.3 = 6.67 m/a$ 

In the third layer there is no vertical or horizontal advective flow, there will however still be diffusive flow.

Following are the parameters used in this example:

<b>Property</b>		<u>Value</u>	<u>Units</u>
Darcy Velocity	v <sub>a</sub>	variable	m/a
Sink Outflow Velocity	v <sub>s</sub>	variable	m/a
Diffusion Coefficient	D	variable	m <sup>2</sup> /a
Distribution Coefficient	K <sub>d</sub>	0.0	cm <sup>3</sup> /g
Soil Porosity	n	0.4	-
Granular Layer Porosity	n	0.3	-
Dry Density		1.5	g/cm <sup>3</sup>
Layer 1 Thickness	Н	1.0	m
Layer 2 Thickness	Н	0.3	m
Layer 3 Thickness	Н	2.0	m
Source Concentration	c <sub>o</sub>	1000	mg/L
Ref. Height of Leachate	H <sub>r</sub>	7.5	m
Vol. of Leachate Collected	Qc	0.29	m/a
Landfill Length	L	200.0	m
Landfill Width	W	1.0	m
Aquifer Thickness	h	1.0	m
Aquifer Porosity	nb	0.3	-
Aquifer Outflow Velocity	v <sub>b</sub>	4.0	m/a

This example is for a hypothetical landfill and is used to illustrate how to prepare an input file and run an analysis using the Passive Sink option. The example is not a prescription for modelling contaminant migration during operation of a landfill. Each landfill has its own unique characteristics and no general prescription can be made. The Passive Sink option should only by used by someone with the hydrogeotechnical background necessary to appreciate the subtleties associated with the physical situation and the steps necessary for appropriate modelling of this physical situation.

## **Data Entry**

Start the POLLUTEv7 program and open the Examples project. Select Case 14 and open the model by double clicking on it in the model list. After the model is displayed, the data for the model can be displayed and edited using the Data Entry menu or by clicking on that part of the model.

## **General Data**

The general data for this example can be specified by either clicking on the title or selecting the General Data menu item from the Data Entry menu. The General Data form on the next page will be displayed. In this example the Darcy velocity will be ignored, the Darcy velocity will be read during the input of the Passive Sink parameters. After the Passive Sink special feature has been selected the Darcy velocity will no longer appear in the General Data form.

General Data 🛛 👌	
Title: Case 14: Landfill with Primary and S	Secondary Leachate Collection
Number of Layers: 3	Maximum Depth: 4.3 m 💌
. ,	· , , <u> </u>
Lanlace Transform Parameters	
	SIG: 0 BNUE 2
	old, jo Tino, je
<b>V</b> 0K	X Cancel ? Help

1

## Case 14: Primary and Secondary Leachate Collection

## Layer Data

The layer data for the 3 layers can be specified by either clicking on a layer or selecting the Layer Data menu item from the Data Entry menu.

### Layer 1

Layer Data			
	Layer Number	1	
Layer Data Layer Symbol			
Name: Clay	1		
Number of Sub Layers	4		Fractures
Thickness	1 m	•	None
Dry Density	1.5 g/cm3	•	C 1 Dimensional
Porosity	0.4		C 2 Dimensional
Coef of Hydro Disp	0.02 m2/a	•	C 3 Dimensional
Distribution Coef	0 m3/kg	-	
<b>V</b> (	DK 🗙 Car	ncel	? <u>H</u> elp

## Layer 2

Layer Data	
Lay Number 2	
Layer Data Layer Symbol	
Name: Collection System	
Number of Sub Layers 4	Fractures
Thickness 0.3 m	None
Dry Density 1.5 g/cm3 💌	C 1 Dimensional
Porosity 0.3	C 2 Dimensional
Coef of Hydro Disp 10 m2/a 💌	C 3 Dimensional
Distribution Coef 0 m3/kg 💌	
V DK X Cancel	? Help

### Layer 3

Layer Data		
	Layer Number 3	
Layer Data Layer Symbol		
Name: Aquitard	7	
Number of Sub Layers	4	Fractures
Thickness	2 m 💌	None
Dry Density	1.5 g/cm3 💌	C 1 Dimensional
Porosity	0.4	C 2 Dimensional
Coef of Hydro Disp	0.02 m2/a 💌	C 3 Dimensional
Distribution Coef	0 m3/kg 💌	
<b>V</b> (	OK 🗶 Cancel	? Help

## **Boundary Conditions**

The boundary conditions for the model can be specified by either clicking on the top or bottom boundary or selecting the Boundary Conditions menu item from the Data Entry menu. In this example, the top boundary has a finite mass and the bottom boundary is represented by a fixed outflow aquifer, as shown on the Boundary Condition forms below.

Boundary Conditi	ons			
Boundary Conditions Specify	Top - Finite Mass	Bottom - Fixed O	utflow   Fix	ed Outflow Symbol
Initial	Source Concentration	n: 1000	mg/L	•
Rat	e of Increase in Con	× 0	mg/L/yr	•
Volume (	of Leachate Collecte	± 0.29	m/a	•
and either				
	Thickness of Was	e: 0	m	<b>-</b>
	Waste Densit	y: 0	g/cm3	•
	Proportion of Mas	s: 0		
Volu	imetric Water Conter	it 0		
Con or	version Rate Half Lif	e: 0	year	•
B	ef Height of Leachat	e: 7.5	m	-
	<u>o</u> k	Cancel	?	<u>H</u> elp

### **Case 14: Primary and Secondary Leachate Collection**

Boundary Conditions
Boundary Conditions   Top - Finite Mass   Bottom - Fixed Outflow   Fixed Outflow Symbol
Landfill Length: 200 m
Landfill Width: 1
Base Thickness: 1
Base Porosity: 0.3
Base Outflow Velocity: 4 m/a 💌
✓ <u>Q</u> K X Cancel ? Help

## **Run Parameters**

To set the times and depths to calculate the concentrations, select the Run Parameters menu item from the Data Entry menu. The Run Parameters form below will be displayed. The concentrations can either be calculated at specified times or the time of the maximum concentration can be found. In this example the concentrations will be calculated at 10, 25, 50, 100, and 150 years.

Run Pa	arameters
Туре	Concentrations at Specified Times
Tir	Number of Times: 5 Number: 1 I I I I I
All C	Depths Yes No
[	VOK Cancel ? Help

## **Special Features**

The passive sink data for this model can be entered using the Passive Sink menu item in the Special Features menu.

## **Passive Sink**

When the Passive Sink menu item is selected the Passive Sink form below will be displayed. On the Data tab the number of depths and whether there is a phase change or inflow can be specified. In this example there are 3 depth intervals. The first depth interval is for the clay liner, the second for the secondary leachate collection system, and the third for the aquitard.

Passive Sink
Data Istanus Data
Number of Intervals 3
Inflow Rate
No     C Yes
V OK X Cancel ? Help

## Case 14: Primary and Secondary Leachate Collection

## Sink Interval 1

Passive Sink	
R	
Data Interval Data	
Depth Interval: 1 🛛 🖌 化	• •
Top Depth 0 m	•
Bottom Depth 1 m	•
Darcy Velocity 0.01 m/a	•
Rate of Removal 0 m/a	•
UK X Cancel	Help

## Sink Interval 2

Passiv	e Sink
Data	R Interval Data
'	Depth Interval: 2   ( + )
	Top Depth 11 m 💌 Bottom Depth 1.3 m 💌
	Darcy Velocity 0.01 m/a Rate of Removal 6.67 m/a
	✓ OK X Cancel ? Help

Sink Interval 3

Passive Sink	
R	
Data Interval Data	
Depth Interval: 3 4 4 4	
Top Depth 1.3 m 💌	
Bottom Depth 3.3 m 💌	
Darcy Velocity 0 m/a 💌	
Rate of Removal 0 m/a 💌	
V OK X Cancel ? Help	

## **Model Execution**

To run the model and calculate the concentrations either select the Run menu item from the Execute menu or press the Run button on the toolbar.

## **Model Output**

After the model has been executed, the output for the model will be displayed. The initial display will depend on your settings in the program's preferences.

## **Concentration vs Depth**

The Concentration vs. Depth chart below can be displayed by pressing the Concentration vs Depth button on the Output toolbar or selecting the Concentration vs Depth menu item from the Output menu.



## **Output Listing**

To display the output as a text listing that will show the calculated concentrations as numbers, select the List Output menu item from the Output menu or press the Output Listing button on the Output toolbar.

### Case 14: Landfill with Primary and Secondary Leachate Collection

#### THE PASSIVE SINK OPTION HAS BEEN USED NOTE : THE USER IS RESPONSIBLE FOR ENSURING THAT VELOCITY CHANGES ARE CONSISTENT WITH THE PASSIVE SINK

#### Layer Properties

Layer	Thickness	Number of Sj̃ublayers	Coefficient of Hydrodynamic Dispersion	Matrix Porosity	Distributon Coefficient	Dry Density
Clay Collection	1 m 0.3 m	4 4	0.02 m2/a 10 m2/a	0.4 0.3	0 m3/kg 0 m3/kg	1.5 g/cm3 1.5 g/cm3
Aquitard	2 m	4	0.02 m2/a	0.4	0 m3/kg	1.5 g/cm3

#### **Boundary Conditions**

#### Finite Mass Top Boundary

Initial Concentration = 1000 mg/L Rate of Increase = 0 mg/L/yr Volume of Leachate Collected = 0.29 m/a Thickness of Waste = 0 m Waste Density = 0 g/cm3 Proportion of Mass = 0 Volumetric Water Content = 0 Conversion Rate Half Life = 0 year Reference Height of Leachate = 7.5 m

#### Fixed Outflow Bottom Boundary

Landfill Length = 200 m Landfill Width = 1 m Base Thickness = 1 m Base Porosity = 0.3 Base Outflow Velocity = 4 m/a

#### VELOCITY AND SINK PROFILE:

Time Period	Minimum Depth	Maximum Depth	Vertical Velocity	Horizontal Outflow
1	0 m	. 1 m	0.01 m/a	0 m/a
	1 m	1.3 m	0.01 m/a	6.67 m/a
	1.3 m	3.3 m	0 m/a	0 m/a

#### Laplace Transform Parameters

**TAU =** 7 **N =** 20 **SIG =** 0 **RNU =** 2

Time	Depth	Concentration
year	m	mg/L
10	0.000E+00	6.589E+02
	2.500E-01	i 5.818E+02
	5.000E-01	I 4.425E+02
	7.500E-01	2.803E+02
т	1.000E+00	1.231E+02
	1.075E+00	1.230E+02
	1.150E+00	1.229E+02
	1.225E+00	1.228E+02
	1.300E+00	1.228E+02
	1.800E+00	1.873E+01
	2.300E+00	1.587E+00
	2.800E+00	7.432E-02
	3.300E+00	5 162E-04
	0.0002.000	0.1022 01
25	0.000E+00	3.627E+02
	2.500E-01	3.891E+02
	5.000E-01	3.801E+02
	7.500E-01	3.364E+02
	1.000E+00	2.632E+02
	1.075E+00	2.631E+02
	1.150E+00	2.631E+02
	1.225E+00	2.630E+02
	1.300E+00	2.630E+02
	1.800E+00	1.245E+02
	2.300E+00	4.525E+01
	2.800E+00	1.254E+01
	3.300E+00	1.337E+00
50	0.000E+00	1.363E+02
	2.500E-01	1.698E+02
	5.000E-01	1.948E+02
	7.500E-01	2.086E+02
	1.000E+00	2.097E+02
	1.075E+00	2.097E+02
	1.150E+00	2.098E+02
	1.225E+00	2.098E+02
	1.300E+00	2.098E+02
	1.800E+00	1.627E+02
	2.300E+00	1.040E+02
	2.800E+00	P 5.353E+01
	3.300E+00	1.598E+01
100	0.0005.400	2.0195+01
100		
	7 500 - 01	4.033⊑±01 6.132⊑±01
		7 553 101
	1 075E+00	7.553E+01
	1 150E+00	7.554E+01
	1 225E+00	7 558E+01
	1 300E+00	7 560E+01
	1 800 - +00	8 454 E+01
	2 300E+00	7 584E+01
	2 800 E +00	5 456E+01
	3.300E+00	2.635E+01
	0.0002.00	2.0002.01

### Calculated Concentrations at Selected Times and Depths

### **Case 14: Primary and Secondary Leachate Collection**

	·	
150	0.000E+00	3.300E+00
	2.500E-01	7.810E+00
	5.000E-01	1.322E+01
	7.500E-01	1.948E+01
	1.000E+00	2.649E+01
	1.075E+00	2.649E+01
	1.150E+00	2.650E+01
	1.225E+00	2.651E+01
	1.300E+00	2.652E+01
	1.800E+00	3.452E+01
	2.300E+00	3.469E+01
	2.800E+00	2.753E+01
	3.300E+00	1.491E+01

#### NOTICE

Although this program has been tested and experience would indicate that it is accurate within the limits given by the assumptions of the theory used, we make no warranty as to workability of this software or any other licensed material. No warranties either expressed or implied (including warranties of fitness) shall apply. No responsibility is assumed for any errors, mistakes or misrepresentations that may occur from the use of this computer program. The user accepts full responsibility for assessing the validity and applicability of the results obtained with this program for any specific case.

## Description

This example is similar to case 14 except the failure of the primary leachate collection system is also modelled using the Variable Properties special feature. Prior to the failure of the primary leachate collection system there is a downward Darcy velocity of 0.01 m/a between the landfill and the secondary leachate collection system. The primary leachate collection system is assumed to fail between 20 and 30 years, causing the leachate mound in the landfill to rise resulting in an increase in the Darcy velocity. After 30 years the collection system has completely failed and the Darcy velocity is now assumed to be 0.1 m/a.

As in case 14 the landfill contains a finite mass of a conservative species, and is underlain by an aquifer with fixed outflow. A passive sink is used to model the secondary leachate collection system, which is assumed to be composed of a 0.3 m thick granular layer. The Darcy velocity is assumed to be initially 0.01 m/a downward from the landfill to the secondary leachate collection system, and 0.0 m/a between the secondary leachate collection system and the aquifer (i.e., the water table is assumed to be at the base of the secondary leachate collection system).

The analysis starts at time zero which corresponds to the completion of the landfill and the development of a peak leachate concentration ( $c_0$ ) of 1000 mg/L. As in example 14 the Reference Height of Leachate is 7.5 m, and the Rate of Increase in Concentration is zero.

The average infiltration through the cover  $(q_0)$  is assumed to be 0.3 m/a. If the average exfiltration through the base of the landfill  $v_a$  (which varies with time), then the Volume of Leachate Collected is:

$$Q_c = q_0 - v_a = 0.3 - v_a$$

The strata beneath the landfill, landfill dimensions, and aquifer characteristics are the same as in example 14.

Passive sink layers are divided the same as in example 14, except that the Darcy velocity in the first layer and the outflow in the second layer will be variable. The Darcy velocity in the first layer will be 0.01 m/a between 0 and 20 years, then will increase linearly between 20 and 30 years to 0.1 m/a, and then will be 0.1 m/a.

In the second layer the horizontal outflow is equal to the difference in Darcy velocity between the layers above and below, multiplied by the landfill length and divided by the layer thickness, viz:

$$v_s = (v_{a2} - v_{a1}) * 200/0.3 \text{ m/a}$$

In the third layer there is no vertical or horizontal advective flow, there will however still be diffusive flow.

When using the Variable Properties special feature with the Passive special feature it is possible to specify the Darcy velocities in both features. The Darcy velocity used by POLLUTE will be the result from the multiplication of the two velocities. For most practical applications, it is recommended that the Darcy velocity be entered as 1.0 in one of the features, and then the actual value entered in the other feature. In this example the Darcy velocity is entered as 1.0 in the Variable Properties special feature, and the actual values are entered in the Passive Sink special feature.

Using the Variable Properties special feature the dispersivity can also be specified, in this example it is assumed to be 0.4 since there is outward flow from the landfill.

Following are the parameters used in this example:

<b>Property</b>		<u>Value</u>	<u>Units</u>
Darcy Velocity	v <sub>a</sub>	variable	m/a
Sink Outflow Velocity	v <sub>s</sub>	variable	m/a
Diffusion Coefficient	D	0.02	m <sup>2</sup> /a
Dispersivity		0.4	m
Distribution Coefficient	Kd	0.0	$cm^{3}/g$
Soil Porosity	n	0.4	-
Granular Layer Porosity	n	0.3	-
Dry Density		1.5	g/cm <sup>3</sup>
Layer 1 Thickness	Н	1.0	m
Layer 2 Thickness	Н	0.3	m
Layer 3 Thickness	Н	2.0	m
Source Concentration	c <sub>o</sub>	1000	mg/L
Ref. Height of Leachate	H <sub>r</sub>	7.5	m
Vol. of Leachate Collected	Q <sub>c</sub>	variable	m/a
Landfill Length	L	200.0	m
Landfill Width	W	1.0	m
Aquifer Thickness	h	1.0	m
Aquifer Porosity	nb	0.3	-
Aquifer Outflow Velocity	v <sub>b</sub>	4.0	m/a

When using the Variable Properties special feature the accuracy of the results is dependent on the number of sublayers used.

This example is for a hypothetical landfill and is used to illustrate how to prepare an input file and run an analysis using the Variable Properties and Passive Sink option. The example is not a prescription for modelling contaminant migration during operation of a landfill. Each landfill has its own unique characteristics and no general prescription can be made. These options should only by used by someone with the hydrogeologic and engineering background necessary to appreciate the subtleties associated with the physical situation and the steps necessary for appropriate modelling of this physical situation.

## **Data Entry**

Start the POLLUTEv7 program and open the Examples project. Select Case 15 and open the model by double clicking on it in the model list. After the model is displayed, the data for the model can be displayed and edited using the Data Entry menu or by clicking on that part of the model.

## **General Data**

The general data for this example is the same as for Case 14, except that the title is different.

## Layer Data

The layer data for this example is the same as for Case 14.

## **Boundary Conditions**

The boundary conditions for this example is the same as for Case 14.

## **Run Parameters**

The run parameters for this example is the same as for Case 14.

## **Special Features**

The time-varying data and passive sink data for this model can be entered using the Time-varying Data and Passive Sink menu items in the Special Features menu.

1

## **Time-varying Data**

To specify the time-varying properties, select the Time-Varying Properties menu item from the Special Features form. The Time-Varying Data tab on the Time-Varying Properties form shown below can be used to specify the number of time periods and whether there are variable layer properties and variable decay. In this example there are 5 time periods.

🔎 Time Varying P	roperties	
Time Varying Data S	Time Period 1	
Number	of Time Periods 🗐 Start Time 🛛 🛛 yr 💽	
	Properties Increment within Periods	
	-Variable Layer Properties: C Yes	
	Variable Decay: C Yes ⓒ No	
	OK X Cancel ? H	lelp

#### **Time Period 1**

The data for each time period is specified on the Source Properties tab shown on the next page. In the first time period, specifying only one time increment means that the concentrations will only be calculated at the end time (i.e., 20 years). The Darcy velocity is set to one here and will be entered in the Passive Sink option. Since this is the first time period the primary leachate collection system is still functioning and there is no increase in any of the above parameters.

📮 Time Varying	; Properties				
		Time Perio	d  1		< > >
Time Varying Data	Source Properties				
Specify	End Time	20	yr	-	
N	lumber of Increments	1			Increments
	Source Conc	1000	mg/L	-	0
	Darcy Velocity	1	m/a	•	0
	Dispersivity	0.4	m	•	
	Base Velocity	4	m/a	•	0
	Rate for Conc	0	Rate	•	
	Volume Collected	0.29	m/a	•	0
And either	Waste Thickness	0	m	•	
	Waste Density	0	kg/m3	•	
	Proportion of Mass	0			
	Water Content	0			
	Conv Rate Half Life	0	yr	•	
Or	Ref Hight of Leach	7.5	m	-	
	🖊 ОК	🗙 Cancel		? Hel	p

### **Time Period 2**

The data for the second time period, from 20 to 30 years, can be specified by pressing the next arrow at the top of the form. The increment in the Leachate collected results from the increasing Darcy velocity during this period. This increase in Darcy velocity will be taken into account in the Passive Sink option.

🗖 Time Varying	Properties				- OX
		Time Period	2		
Time Varying Data	Source Properties				
Specify	End Time	β0	yr	-	
N	umber of Increments	5			Increments
	Source Conc	-1	mg/L	-	0
	Darcy Velocity	1	m/a	-	0
	Dispersivity	0.4	m	-	
	Base Velocity	4	m/a	-	0
	Rate for Conc	0	Rate	-	
	Volume Collected	0.2	m/a	-	-0.018
And either	Waste Thickness	0	m	-	
	Waste Density	0	kg/m3	-	
	Proportion of Mass	0			
	Water Content	0			
	Conv Rate Half Life	0	yr	-	
Or	Ref Hight of Leach	7.5	m	•	
~	/ OK	🗙 Cancel		? He	Ip

#### **Time Period 3**

Next the data for time period three from 30 to 50 years must now be entered.. Two increments are used to calculate the concentrations at 40 and 50 years. At this point the primary leachate collection system has completely failed and there is no further increase in the Darcy velocity. The Volume of Leachate collected is now equal to the infiltration through the cover 0.3 m/a minus the final Darcy velocity 0.1 m/a.

🗖 Time Varying	Properties				- O X
		Time Perio	<b>d</b> 3		
Time Varying Data	Source Properties				
Specify	End Time	Joa	yr	-	
N	umber of Increments	2			Increments
	Source Conc	-1	mg/L	-	0
	Darcy Velocity	1	m/a	-	0
	Dispersivity	0.4	m	-	
	Base Velocity	4	m/a	-	0
	Rate for Conc	0	Rate	-	
	Volume Collected	0.2	m/a	-	0
And either	Waste Thickness	0	m	-	
	Waste Density	0	kg/m3	•	
	Proportion of Mass	0			
	Water Content	0			
	Conv Rate Half Life	0	yr	•	
Or	Ref Hight of Leach	7.5	m	•	
	и ок	🗙 Cancel		? He	lp

### **Time Period 4**

The data for time period four should now be entered. Five increments are used to calculate the concentrations at 60, 70, 80, 90, and 100 years.

🗖 Time Varying Properties					
		Time Perio	d 4	•	
Time Varying Data	Source Properties	R			
Specify	End Time	100	yr	-	
N	umber of Increments	5			Increments
	Source Conc	-1	mg/L	•	0
	Darcy Velocity	1	m/a	-	0
	Dispersivity	0.4	m	-	
	Base Velocity	4	m/a	-	4
	Rate for Conc	0	Rate	-	
	Volume Collected	0.2	m/a	-	0
And either	Waste Thickness	0	m	-	
	Waste Density	0	kg/m3	-	
	Proportion of Mass	0			
	Water Content	0			
	Conv Rate Half Life	0	yr	-	
rO	Ref Hight of Leach	7.5	m	•	
	🖊 ОК	🗙 Cancel 🛛		? Не	elp

### **Time Period 5**

Finally the data for time period five is entered. Five increments are used to calculate the concentrations at 120, 140, 160, 180, and 200 years.

🗖 Time Varying	g Properties				- DX
	1	Time Perio	d 5		
Time Varying Data	Source Properties				
Specify	End Time	200	yr	-	
N	lumber of Increments	5		_	Increments
	Source Conc	-1	mg/L	-	0
	Darcy Velocity	1	m/a	-	0
	Dispersivity	0.4	m	•	
	Base Velocity	4	m/a	•	0
	Rate for Conc	0	Rate	-	
	Volume Collected	0.2	m/a	•	0
And either	Waste Thickness	0	m	•	
	Waste Density	0	kg/m3	-	
	Proportion of Mass	0			
	Water Content	0			
	Conv Rate Half Life	0	yr	•	
Or	Ref Hight of Leach	7.5	m	•	
	<i>t</i> .ov. ]			<b>.</b>	. 1
		X Cancel	_	🌠 He	ip

## Passive Sink

When the Passive Sink menu item is selected the Passive Sink form on the next page will be displayed. On the Data tab the number of depths and whether there is a phase change or inflow can be specified. In this example there are 3 depth intervals. The first depth interval is for the clay liner, the second for the secondary leachate collection system, and the third for the aquitard.

When the Time-varying Properties special feature is also used, the current time period is displayed and controlled at the top of the form. The passive sink data must be entered for each time period.

### **Time Period 1**

The first time period corresponds from 0 to 20 years. For this time period the data for the 3 passive sink depth intervals can be entered on the Interval tab as shown below.

Passive Sink       Variable Properties       Time Period:       1       Variable Properties       Data	Passive Sink       Variable Proferries       Time Period:       1       Data	Passive Sink       Variable Properties       Time Period:       1       Jata
Depth Interval: 1 🛛 🛛 🖌 🕨	Depth Interval: 2 🛛 🛛 🖌 🕨	Depth Interval: 3 🛛 🛛 🕹 🕨
Top Depth 0 m v Bottom Depth 1 m v Darcy Velocity 0.01 m/a v Rate of Removal 0 m/a v	Top Depth     Im       Bottom Depth     1.3       Darcy Velocity     0.01       M/a     Im/a	Top Depth 11.3 m  Bottom Depth 13.3 m  Darcy Velocity 0 m/a  Rate of Removal 0 m/a
Cancel ? Help	V DK X Cancel ? Help	✓ OK

#### **Time Period 2**

The first time period corresponds from 20 to 30 years. For this time period the data for the 3 passive sink depth intervals can be entered on the Interval tab as shown on the next page. There is an increase in the Darcy velocity during this time period due to the failure of the primary leachate collection system. This will also result in a proportional increase in the Outflow velocity of the secondary leachate collection system as shown.

Passive Sink Variable Properties Time Period: 2   (   )	Passive Sink Variable Properties Time Period: 2   4 + >   Data Interval Data	Passive Sink       Variable Properties       Time Period:     2       Image: Constraint of the period:     1       Data     Interval Data
Depth Interval: 1 (4 4 )	Depth Interval: 2   ( )	Depth Interval: 3 🖌 🖌 🕨
Top Depth     0     m     ▼       Bottom Depth     1     m     ▼       Darcy Velocity     0.028     m/a     ▼       Rate of Removal     0     m/a     ▼	Top Depth     Im       Bottom Depth     1.3       Darcy Velocity     0.028       m/a     Im/a	Top Depth     11.3     m     ▼       Bottom Depth     3.3     m     ▼       Darcy Velocity     0     m/a     ▼       Rate of Removal     0     m/a     ▼
OK X Cancel ? Help	Cancel ? Help	V DK X Cancel ? Help

### **Time Period 3**

The first time period corresponds from 30 to 50 years. For this time period the data for the 3 passive sink depth intervals can be entered on the Interval tab as shown below.

Passive Sink	Passive Sink	Passive Sink
Variable Properties	Variable Properties	Variable Properties
Time Period: 3 🛛 🖌 🖌 🕨	Time Period: 3 🛛 🖣 🔶 🕨	Time Period: 3
Data Interval Data	Data Interval Data	Data Interval Data
Depth Interval: 1 🛛 🛛 🖌 🕨	Depth Interval: 2 🛛 🛛 🖌 🕨	Depth Interval: 3 🛛 🛛 🕹 🕨
Top Depth 0 m	Top Depth 1 m 💌	Top Depth 1.3 m 💌
Bottom Depth 1 m 💌	Bottom Depth 1.3 m 👻	Bottom Depth 3.3 m 👻
Darcy Velocity 0.046 m/a 💌	Darcy Velocity 0.046 m/a 💌	Darcy Velocity 0 m/a 💌
Rate of Removal 0 m/a 💌	Rate of Removal 30.7 m/a 💌	Rate of Removal 0 m/a 💌
VOK X Cancel ? Help	V OK X Cancel ? Help	V OK X Cancel ? Help
### **Case 15: Leachate Collection with Failure**

### **Time Period 4**

The first time period corresponds from 50 to 100 years. For this time period the data for the 3 passive sink depth intervals can be entered on the Interval tab as shown below.

Passive Sink       Variable Properties       Time Period:       4       Variable Interval Data	Passive Sink       Variable Properties       Time Period:       4       A       Data	Passive Sink     Image: Constraint of the second seco
Depth Interval: 1 🛛 🛛 🖌 🕨	Depth Interval: 2 🛛 🖌 🖌 🕨	Depth Interval: 3 🛛 🖌 🖌 🕨
Top Depth D m  Bottom Depth 1 m  Darcy Velocity 0.064 m/a  Rate of Removal 0 m/a	Top Depth     In     m     ▼       Bottom Depth     1.3     m     ▼       Darcy Velocity     0.064     m/a     ▼       Rate of Removal     42.7     m/a     ▼	Top Depth     11.3     m     ▼       Bottom Depth     3.3     m     ▼       Darcy Velocity     0     m/a     ▼       Rate of Removal     0     m/a     ▼
V OK X Cancel ? Help	V DK X Cancel ? Help	V DK X Cancel ? Help

### **Time Period 5**

The first time period corresponds from 100 to 200 years. For this time period the data for the 3 passive sink depth intervals can be entered on the Interval tab as shown below.

Passive Sink	Passive Sink	Passive Sink
Variable Properties	Variable Properties	Variable Properties
Time Period: 5  ◀ ◀ ▶ ▶	Time Period <sup>3</sup> 5  4 4 <b>&gt;</b> 1	Time Period: 5
Data Interval Data	Data Interval Data	Data Interval Data
Depth Interval: 1  4 4 🕨 🕅	Depth Interval: 2 🖌 🖌 🖌 🕨	Depth Interval: 3 🖌 🖌 🕨
Top Depth D m 💌	Top Depth 1 m 💌	Top Depth 11.3 m 💌
Bottom Depth 1 m	Bottom Depth 1.3 m 💌	Bottom Depth 3.3 m 💌
Darcy Velocity 0.082 m/a 💌	Darcy Velocity 0.082 m/a 💌	Darcy Velocity 0 m/a 💌
Rate of Removal 0 m/a 💌	Rate of Removal 54.7 m/a 💌	Rate of Removal 0 m/a 💌
OK X Cancel ? Help	V OK Cancel ? Help	OK Cancel ? Help

# **Model Execution**

To run the model and calculate the concentrations either select the Run menu item from the Execute menu or press the Run button on the toolbar.

# **Model Output**

After the model has been executed, the output for the model will be displayed. The initial display will depend on your settings in the program's preferences.

## **Concentration vs Depth**

The Concentration vs. Depth chart below can be displayed by pressing the Concentration vs Depth button on the Output toolbar or selecting the Concentration vs Depth menu item from the Output menu.



# **Output Listing**

To display the output as a text listing that will show the calculated concentrations as numbers, select the List Output menu item from the Output menu or press the Output Listing button on the Output toolbar.

### Case 15: Leachate Collection with Failure.

### THE VARIABLE VELOCITY AND/OR CONCENTRATION OPTION HAS BEEN USED NOTE THAT THE ACCURACY OF THE CALCULATIONS WITH THIS OPTION WILL DEPEND ON THE NUMBER OF SUBLAYERS USED

THE PASSIVE SINK OPTION HAS BEEN USED NOTE : THE USER IS RESPONSIBLE FOR ENSURING THAT VELOCITY CHANGES ARE CONSISTENT WITH THE PASSIVE SINK

#### Layer Properties

Layer	Thickness	Number of Sublayers	Coefficient of Hydrodynamic Dispersion	- Matrix Porosity	Distributon Coefficient	- Dry Density
Clay Collection	1 m 0.3 m	4 4	0.02 m2/a 10 m2/a	0.4 0.3	0 mL/g 0 mL/g	1.5 g/cm3 1.5 g/cm3
Aquitard	2 m	4	0.02 m2/a	0.4	0 mL/g	1.5 g/cm3

#### **Boundary Conditions**

#### Finite Mass Top Boundary

#### Fixed Outflow Bottom Boundary

Landfill Length = 200 m Landfill Width = 1 m Base Thickness = 1 m Base Porosity = 0.3

### VARIATION IN PROPERTIES WITH TIME:

#### TIME PERIODS WITH THE SAME SOURCE AND VELOCITY

Period	Start Time	No. of	Time Step	Source Conc	Rate of	Height of	Volume
		Steps	_		Change	Leachate	Collected
1	O yr	1	20 yr	1000 mg/L	0	7.5 m	0.29 m/a
2	20 yr	τ 5	2 yr	-1 mg/L	0	7.5 m	0.2 m/a
3	30 yr	2	10 yr	-1 mg/L	0	7.5 m	0.2 m/a
4	50 yr	5	10 yr	-1 mg/L	0	7.5 m	0.2 m/a
5	100 yr	5	20 yr	-1 mg/L	0	7.5 m	0.2 m/a
	-		-	-			

Period	Start Time	End Time	Darcy Velocity	* Dispersivity	'Base Velocity
1	0 yr	20 yr	1 m/a	0.4 m	4 m/a
2	20 yr	30 yr	1 m/a	0.4 m	4 m/a
3	30 yr	50 yr	1 m/a	0.4 m	4 m/a
4	50 ýr	100 yr	1 m/a	0.4 m	4 m/a
5	100 yr	200 ýr	1 m/a	0.4 m	4 m/a
	, i				

# VELOCITY AND SINK PROFILE:

Time Period	" Minimum Depth	Maximum Depth	Vertical Velocity	Horizontal Outflow
1	, Om	1 m	0.01 m/a	0 m/a
	y 1 m	1.3 m	0.01 m/a	6.67 m/a
	: 1.3 m	3.3 m	0 m/a	i Om/a
2	0 m	1 m	0.028 m/a	0 m/a
_	1 m	i 1.3 m	0.028 m/a	18.7 m/a
	1.3 m	j 3.3 m	€ Om/a	Om/a
3	0 m	1 m	₽ ╤ 0.046 m/a	0 m/a
	1 m	(1.3 m	ş 0.046 m/a	30.7 m/a
	1.3 m	( 3.3 m	ş Om/a	0 m/a
4	0 m	1 m	0.064 m/a	0 m/a
	1 m	1.3 m	0.064 m/a	42.7 m/a
	1.3 m	3.3 m	Um/a	Um/a
5	0 m	1 m	0.082 m/a	0_m/a
	1 m	1.3 m	0.082 m/a	54.7 m/a
	l 1.3 m	3.3 m	Um/a	Um/a
6	0 m	1 m	0.1 m/a	0 m/a
	) <u>1</u> m	1.3 m	0.1 m/a	66.7 m/a
	1.3 m	3.3 m	Um/a	Um/a
7	0 m	1 m	0.1 m/a	0 m/a
	1 m	1.3 m	0.1 m/a	66.7 m/a
	1.3 m	3.3 m	Um/a	Um/a
8	0 m	1 m	0.1 m/a	0_m/a
	t 1 m	1.3 m	U.1 m/a	66./m/a
	1.3 m	3.3 m	ĭ Um/a ş	Um/a
9	0 m	1 m	0.1 m/a	0 m/a
	1 m	1.3 m	° 0.1 m/a	66.7 m/a
	- 1.3 m	- 3.3 m	- Om/a	- Om/a
10	0 m	1 m	0.1 m/a	0 m/a
	1 m	1.3 m	0.1 m/a	66.7 m/a
	1.3 m T	3.3 m	U m/a	0 m/a
11	<u> </u>	1 m	0.1 m/a	0 m/a
	/ 1 m	1.3 m	0.1 m/a	66.7 m/a
	/ 1.3 m	3.3 m	0 m/a	0 m/a
12	0 m	1 m	0.1 m/a	0 m/a
	- 1 m	- 1.3 m	- 0.1 m/a	- 66.7 m/a
	. 1.3 m	_ 3.3 m	- Om/a	- Om/a

L				l
13	0 m	1 m	0.1 m/a	0 m/a
	1 m	1.3 m	0.1 m/a	66.7 m/a
	1.3 m	2 33 m	Γ Π m/a	Ωm/a
	1.0	5	5	0 11/0
14	0 m	۱ m	∮ 0.1 m/a	0 m/a
	1 m	[ 1.3 m	⊧ 0.1 m/a	66.7 m/a
	13 m	33 m	0 m/a	0 m/a
Т		3.5 11		
15	0 m	1 m	0.1 m/a	0 m/a
	1 m	13 m	0.1 m/a	66.7 m/a
	13 m	33 m	0 m/a	0 m/a
	1.5 11	5.5 m	0 11//a	0 11/4
10		1 m	0.1 m/a	0 m/a
10		4.2		
	y im	1.3 m	U.1 m/a	66.7 m/a
	y 1.3 m	3.3 m	Om/a	) Om/a
	<u>y</u>			·
17	: Om	1 m	0.1 m/a	0 m/a
	1 m	1.3 m	0.1 m/a	66.7 m/a
	[ 1.3 m	[ 3.3 m	[ 0 m/a	0 m/a
		κ		
18	0 m	2 1 m	s 0.1 m/a	0 m/a
	l 1 m	8 1.3 m	6 0.1 m/a	66.7 m/a
	13 m	33 m	0 m/a	0 m/a
	1.5 m	, 3.3 m		0 11/4
		•	Þ.	

#### Laplace Transform Parameters

**TAU =** 7 **N =** 20 **SIG =** 0 **RNU =** 2

### Calculated Concentrations at Selected Times and Depths

Time	Depth	Concentration
yr	m	mg/L
20	0.000E+00	4.395E+02
	2.500E-01	4.454E+02
	5.000E-01	4.211E+02
	7.500E-01	3.712E+02
	1.000E+00	3.033E+02
	. 1.075E+00	- 3.033E+02
	1.150E+00	3.032E+02
	1.225E+00	3.032E+02
	1.300E+00	3.032E+02
		- 1.307E+02
	2.3000 +00	4.108E+01 0.201E+00
Τ	2.80000000	9.391E+00 7.005E-01
<u> </u>	3.300E+00	7.0952-01
22	0.000E+00	4.137E+02
	2.500E-01	4.158E+02
	5.000E-01	4.017E+02
	- 7.500E-01	- 3.701E+02
	1.000E+00	3.224E+02
	1.075E+00	3.223E+02
	1.150E+00	3.223E+02
	1.225E+00	- 3.224E+U2
	1.300E+00	3.225E+U2
		1.411E+02

I	7.500E-01 1.000E+00 1.075E+00 1.150E+00 1.225E+00 1.300E+00 1.800E+00 2.300E+00 3.300E+00	3.701E+02 3.224E+02 3.223E+02 3.223E+02 3.224E+02 3.225E+02 1.411E+02 4.899E+01 - 1.236E+01 1.062E+00
24	0.000E+00 2.500E-01 5.000E-01 7.500E-01 1.000E+00 1.075E+00 1.150E+00 1.225E+00 1.300E+00 2.300E+00 2.800E+00 3.300E+00	3.895E+02 3.927E+02 3.861E+02 3.679E+02 3.372E+02 3.372E+02 3.372E+02 3.373E+02 3.373E+02 3.376E+02 5.647E+01 1.651E+01 1.518E+00
26	0.000E+00 2.500E-01 5.000E-01 7.500E-01 1.000E+00 1.075E+00 1.150E+00 1.225E+00 1.300E+00 1.800E+00 2.300E+00 2.800E+00 3.300E+00	3.667E+02 3.717E+02 3.705E+02 3.614E+02 3.426E+02 3.426E+02 3.427E+02 3.430E+02 3.430E+02 3.434E+02 1.645E+02 6.390E+01 1.875E+01 2.077E+00
28	0.000E+00 2.500E-01 5.000E-01 7.500E-01 1.000E+00 1.075E+00 1.150E+00 1.225E+00 1.300E+00 1.800E+00 2.300E+00 3.300E+00	3.454E+02 3.512E+02 3.531E+02 3.497E+02 3.388E+02 3.388E+02 3.390E+02 - 3.394E+02 3.399E+02 1.741E+02 7.118E+01 - 2.208E+01 2.737E+00
30	0.000E+00 - 2.500E-01 5.000E-01 7.500E-01 1.000E+00 - 1.075E+00 1.150E+00 1.225E+00 1.300E+00	3.253E+02 - 3.312E+02 3.345E+02 3.341E+02 3.282E+02 - 3.282E+02 3.285E+02 3.285E+02 3.289E+02 3.289E+02 3.296E+02

	1.300E+00 1.800E+00 2.300E+00 2.800E+00 3.300E+00	3.296E +02 1.808E +02 7.803E +01 2.547E +01 . 3.490E +00
40 I	0.000E+00 2.500E-01 5.000E-01 7.500E-01 1.000E+00 1.075E+00 1.150E+00 1.225E+00 1.300E+00 1.800E+00 2.300E+00 3.300E+00	2.199E+02 2.276E+02 2.345E+02 2.401E+02 2.437E+02 2.437E+02 2.437E+02 2.440E+02 2.443E+02 2.449E+02 1.881E+02 1.881E+02 1.076E+02 4.712E+01 1.035E+01
50	. 0.000E+00 2.500E-01 5.000E-01 7.500E-01 1.000E+00 1.075E+00 1.150E+00 1.225E+00 1.300E+00 2.300E+00 2.800E+00 3.300E+00	- 1.488E+02 1.546E+02 1.602E+02 1.656E+02 1.704E+02 1.705E+02 1.705E+02 1.705E+02 1.709E+02 1.713E+02 1.603E+02 1.120E+02 5.985E+01 1.789E+01
60	0.000E+00 2.500E-01 5.000E-01 7.500E-01 1.000E+00 1.075E+00 1.150E+00 1.225E+00 1.300E+00 2.300E+00 2.800E+00 3.300E+00	1.008E+02 1.050E+02 1.093E+02 1.138E+02 1.138E+02 1.184E+02 1.184E+02 1.187E+02 1.187E+02 1.187E+02 1.187E+02 1.282E+02 1.023E+02 6.254E+01 - 2.307E+01
70 ]	0.000E+00 2.500E-01 5.000E-01 7.500E-01 1.000E+00 1.075E+00 1.150E+00 1.225E+00 1.300E+00 2.300E+00 2.800E+00 3.300E+00	6.828E+01 7.132E+01 7.456E+01 8.201E+01 8.206E+01 8.215E+01 8.230E+01 8.230E+01 8.230E+01 8.249E+01 9.970E+01 5.698E+01 1.817E+01

1	1	
80	0.000E+00 2.500E-01 5.000E-01 1.000E+00 1.075E+00 1.150E+00 1.225E+00 1.300E+00 2.300E+00 2.800E+00 3.300E+00	4.629E+01 4.847E+01 5.087E+01 5.368E+01 5.679E+01 5.682E+01 5.689E+01 5.689E+01 5.699E+01 7.584E+01 7.026E+01 4.642E+01 1.154E+01
90	0.000E+00 2.500E-01 5.000E-01 7.500E+00 1.000E+00 1.075E+00 1.150E+00 1.225E+00 1.300E+00 2.300E+00 2.800E+00 3.300E+00	3.140E+01 3.295E+01 3.470E+01 3.674E+01 3.925E+01 3.927E+01 3.932E+01 3.939E+01 3.949E+01 5.637E+01 3.537E+01 6.863E+00
100	0.000E+00 2.500E-01 5.000E-01 7.500E-01 1.000E+00 1.075E+00 1.150E+00 1.225E+00 1.300E+00 2.300E+00 2.300E+00 2.800E+00 3.300E+00	2.130E+01 2.240E+01 2.366E+01 2.516E+01 2.705E+01 2.707E+01 2.715E+01 2.715E+01 2.722E+01 4.101E+01 4.000E+01 2.597E+01 4.082E+00
120	0.000E+00 2.500E-01 5.000E-01 1.000E+00 1.075E+00 1.150E+00 1.225E+00 1.300E+00 2.300E+00 2.300E+00 3.300E+00	9.819E+00 1.037E+01 1.101E+01 1.182E+01 1.287E+01 1.288E+01 1.290E+01 1.293E+01 1.296E+01 2.176E+01 2.284E+01 1.723E+01 8.038E+00
140	0.000E+00 2.500E-01 5.000E-01 7.500E-01 1.000E+00	4.534E+00 - 4.811E+00 5.153E+00 5.595E+00 6.199E+00

	1.000=+00 1.075E+00 1.150E+00 1.225E+00 1.300E+00 2.300E+00 2.800E+00 3.300E+00	6.199E+00 6.204E+00 6.213E+00 6.226E+00 6.243E+00 7 1.201E+01 1.374E+01 1.149E+01 6.350E+00
160	0.000E+00 2.500E-01 5.000E-01 1.800E+00 1.875E+00 1.150E+00 1.225E+00 1.300E+00 1.800E+00 2.300E+00 2.800E+00 3.300E+00	2.099E+00 2.243E+00 2.428E+00 3.030E+00 3.033E+00 3.038E+00 3.038E+00 3.044E+00 3.052E+00 6.754E+00 8.230E+00 7.255E+00 4.279E+00
180	0.000E+00 2.500E-01 5.000E-01 7.500E+00 1.000E+00 1.225E+00 1.300E+00 1.800E+00 2.300E+00 2.800E+00 3.300E+00	9.745E-01 1.050E+00 1.151E+00 1.292E+00 1.498E+00 1.500E+00 1.505E+00 1.510E+00 3.809E+00 4.858E+00 4.426E+00 2.701E+00
200 I	0.000E+00 2.500E-01 5.000E-01 7.500E-01 1.000E+00 1.075E+00 1.150E+00 1.225E+00 1.300E+00 2.300E+00 2.300E+00 3.300E+00	4.542E-01 - 4.945E-01 5.499E-01 6.294E-01 7.481E-01 - 7.490E-01 7.503E-01 7.502E-01 7.522E-01 - 2.144E+00 2.830E+00 2.637E+00 1.644E+00

#### NOTICE

Although this program has been tested and experience would indicate that it is accurate within the limits given by the assumptions of the theory used, we make no warranty as to workability of this software or any other licensed material. No warranties either expressed or implied (including warranties of fitness) shall apply. No responsibility is assumed for any errors, mistakes or misrepresentations that may occur from the use of this computer program. The user accepts full responsibility for assessing the validity and applicability of the results obtained with this program for any specific case.

# Case 16: Monte Carlo Simulation

# Description

In this example, Monte Carlo simulation will be used to examine the effect of uncertainty in the service life of a Primary Leachate Collection system. The landfill from example 15 will be used, except the time that the Primary Leachate Collection system begins to fail will vary between 20 and 50 years with a mode of 25 years. Case 15 should be reviewed prior to reading this example, where the implementation of the Variable Properties and Passive Sink special features are described in detail.

The parameters for this example are the same as in Case 15, except for the addition of the Monte Carlo parameters.

<b>Property</b>		<u>Value</u>	<u>Units</u>
Darcy Velocity	va	variable	m/a
Sink Outflow Velocity	v <sub>s</sub>	variable	m/a
Diffusion Coefficient Dispersivity	D	0.02 0.4	m <sup>2</sup> /a m
Distribution Coefficient Soil Porosity Granular Layer Porosity	K n n	0.0 0.4 0.3	cm <sup>3</sup> /g
Dry Density Layer 1 Thickness Layer 2 Thickness Layer 3 Thickness Source Concentration	H H H c <sub>o</sub>	1.5 1.0 0.3 2.0 1000	g/cm <sup>3</sup> m m m mg/L
Ref. Height of Leachate	H <sub>r</sub>	7.5	cm
Vol. of Leachate Collected	Q <sub>c</sub>	variable	m/a
Landfill Length Landfill Width Aquifer Thickness Aquifer Porosity	L W h n <sub>b</sub>	200.0 1.0 1.0 0.3	m m m
Aquifer Outflow Velocity	v <sub>b</sub>	4.0	m/a
Minimum Failure Start Time Modal Failure Start Time Maximum Failure Start Time		20 25 50	a a a

This example is for a hypothetical landfill and is used to illustrate how to prepare an input file and run an analysis using the Variable Properties and Passive Sink option. The example is not a prescription for modelling contaminant migration during operation of a landfill. Each landfill has its own unique characteristics and no general prescription can be made. These options should only by used by someone with the hydrogeologic and engineering background necessary to appreciate the subtleties associated with the physical situation and the steps necessary for appropriate modelling of this physical situation. This option should not be used for an actual project of importance without the guidance of the program developers.

The use of the Monte Carlo simulation feature for the variation of Variable Properties time periods should be done in consultation with the program developers, since it requires a very thorough knowl-edge of the program.

# **Data Entry**

l

Start the POLLUTEv7 program and open the Examples project. Select Case 16 and open the model by double clicking on it in the model list. After the model is displayed, the data for the model can be displayed and edited using the Data Entry menu or by clicking on that part of the model.

# **General Data**

The general data for this example is the same as for Case 15, except that the title is different.

# Layer Data

The layer data for this example is the same as for Case 15.

# **Boundary Conditions**

The boundary conditions for this example is the same as for Case 15.

## **Run Parameters**

The run parameters for this example are the same as for Case 15, except that the concentrations will be only be calculated at a depth off 3.3 m. This depth corresponds to the base of the aquitard.

Run Parameters						
Type Concentration	is at Specified Times   🍡					
All Depths C Yes	Number of Depths: 1					
© No	Depth: 3.3 m					

# **Special Features**

The time-varying data, passive sink, and Monte Carlo simulation data for this model can be entered using the Time-varying Data and Passive Sink menu items in the Special Features menu.

# **Time-Varying Properties**

The time-varying properties for this example is the same as for Case 15.

# **Passive Sink**

The passive sink data for this example is the same as for Case 15.

# Monte Carlo Simulation

The Monte Carlo simulation data can be specified by selecting the Monte Carlo Simulation menu item from the Special Features menu, the form below will be displayed. The number of simulations, variables, and data ranges can be specified on the General tab. The number of simulations is usually between 1000 and 10000. However, the time to compute this many simulations may be quite large. It is suggested as a trial to use less than 50 simulations. In this example we are only going to have one variable.

Monte Carlo Simulation	
General Variable Entry	<b>₽</b>
	Number of Simulations 5000
	Number of Variables 1
	Number of Data Ranges 20
	List All Results
	Cancel 7 Help

On the Variable Entry tab below, the type and distribution for the variable can be specified. To vary the failure time of the Primary Leachate Collection system, the Variable Properties end time that corresponds to the time of failure in the input data set is used.

Monte Carlo Simulation	
General Variable Entry	4
Variable Type C Initial Source Concentration C Darcy Velocity C Layer Thickness C Diffusion Coefficient C Distribution Coefficient Variable Properties End Time	Variable Number 1 (4 4 ) )
Distribution Type C Uniform Triangular C General C Normal C Lognormal	Minimum: 15 Maximum: 50 Mode Value: 25
V OK	X Cancel ? Help

# **Model Execution**

To run the model and calculate the concentrations either select the Run menu item from the Execute menu or press the Run button on the toolbar.

# **Model Output**

After the model has been executed, the output for the model will be displayed. The initial display will depend on your settings in the program's preferences.

## **Distribution of Peak Concentration**

The Distribution of Peak Concentration chart below can be displayed by pressing the Distribution of Peak Concentration button on the Output toolbar or selecting the Distribution of Peak Concentration menu item from the Output menu.



Using the chart of the probability of peak chloride concentration predictions can be made about the concentration in the aquifer. For example, in this case, the expected maximum concentration is 23.5 mg/L.

## **Distribution of the Time of Peak Concentration**

The Distribution of the Time Peak Concentration chart below can be displayed by pressing the Distribution of Time of Peak Concentration button on the Output toolbar or selecting the Distribution of Time of Peak Concentration menu item from the Output menu. Using this chart the expected time of the maximum concentration can be predicted. In this example, the expected time is 68.5 years.



## **Distribution of Variable**

The Distribution of Variable chart below can be displayed by pressing the Distribution of Variable button on the Output toolbar or selecting the Distribution of Variable menu item from the Output menu. Using this chart the distribution of the variable can be checked against the distribution that was specified. In this example, the specified distribution was a triangular distribution with a minimum of 15, mode of 25 and maximum of 50.



# **Output Listing**

To display the output as a text listing that will show the calculated concentrations as numbers, select the List Output menu item from the Output menu or press the Output Listing button on the Output toolbar.

### Case 16: Monte Carlo Simulation

#### THE VARIABLE VELOCITY AND/OR CONCENTRATION OPTION HAS BEEN USED NOTE THAT THE ACCURACY OF THE CALCULATIONS WITH THIS OPTION WILL DEPEND ON THE NUMBER OF SUBLAYERS USED

#### THE PASSIVE SINK OPTION HAS BEEN USED NOTE : THE USER IS RESPONSIBLE FOR ENSURING THAT VELOCITY CHANGES ARE CONSISTENT WITH THE PASSIVE SINK

Ι

#### Layer Properties

Layer	Thickness	Number of Sublayers	Coefficient of Hydrodynamic Dispersion	Matrix Porosity	Distributon Coefficient	Dry Density
Clay	1 m	4	0.02 m2/a	0.4	0 cm3/g	1.5 g/cm3
Collection System	0.3 m	4	10 m2/a	0.3	0 cm3/g	1.5 g/cm3
Aquitard	2 m	4	0.02 m2/a	0.4	0 cm3/g	1.5 g/cm3

#### Boundary Conditions

#### Finite Mass Top Boundary

#### Fixed Outflow Bottom Boundary

Landfill Length = 200 m Landfill Width = 1 m Base Thickness = 1 m Base Porosity = 0.3

#### VARIATION IN PROPERTIES WITH TIME:

Period	Start Time	No. of	Time Step	Source Conc	Rate of	Height of	Volume
		Steps			Change	Leachate	Collected
1	0 yr	1	20 yr	1000 mg/L	0	7.5 m	0.29 m/a
2	20 yr	5	2 yr	-1 mg/L	0	7.5 m	0.2 m/a
3	30 yr	2	10 yr	-1 mg/L	0	7.5 m	0.2 m/a
4	50 yr	5	10 yr	-1 mg/L	0	7.5 m	0.2 m/a
5	100 yr	5	20 ýr	-1 mg/L	0	7.5 m	0.2 m/a
	, , , , , , , , , , , , , , , , , , ,			Ŭ			

Period	Start Time	Ens Time	Darcy Velocity	Dispersivity	Base Velocity
1	O yr	2-Ðγr	1 m/a	0.4 m	4 m/a
2	20 yr	30 yr	1 m/a	0.4 m	4 m/a
3	30 yr	50 yr	1 m/a	0.4 m	4 m/a
4	50 ýr	100 yr	1 m/a	0.4 m	4 m/a
5	100 yr	200 ýr	1 m/a	0.4 m	4 m/a
				-	•

VELOCITY AND SINK PROFILE:

Time Period	Minimum Depth	Maximum Depth	Vertical Velocity	Horizontal Outflow
1	0 m	1 m	0.01 m/a	0 m/a
	• 1 m	1.3 m	0.01 m/a	6.67 m/a
	1.3 m	3.3 m	0 m/a	0 m/a
2	От 1 m 1.3 m I	1 m 1.3 m 3.3 m	0.028 m/a 0.028 m/a 0 m/a	0 m/a 18.7 m/a 0 m/a
3	0 m	1 m	0.046 m/a	0 m/a
	1 m	1.3 m	0.046 m/a	30.7 m/a
	1.3 m	3.3 m	0 m/a	0 m/a
4	0 m	1 m	0.064 m/a	0 m/a
	1 m	1.3 m	0.064 m/a	42.7 m/a
	1.3 m	3.3 m	0 m/a	0 m/a
5	0 m	1 m	0.082 m/a	0 m/a
	1 m	1.3 m	0.082 m/a	54.7 m/a
	1.3 m	3.3 m	0 m/a	0 m/a
6	0 m	1 m	0.1 m/a	0 m/a
	1 m	1.3 m	0.1 m/a	, 66.7 m/a
	1.3 m	3.3 m	0 m/a	_ 0 m/a
7	0 m	1 m	0.1 m/a	0 m/a
	1 m	1.3 m	0.1 m/a	66.7 m/a
	1.3 m	3.3 m	0 m/a	0 m/a
8	0 m	1 m	0.1 m/a	0 m/a
	1 m	1.3 m	0.1 m/a	66.7 m/a
9	0 m	1 m	0.1 m/a	0 m/a
	≰ 1 m	1.3 m	0.1 m/a	66.7 m/a
	1.3 m	3.3 m	0 m/a	0 m/a
10	0 m	1 m	0.1 m/a	0 m/a
	1 m	1.3 m	0.1 m/a	66.7 m/a
	1.3 m	3.3 m	0 m/a	0 m/a
11	0 m	1 m	0.1 m/a	0 m/a
	1 m	1.3 m	0.1 m/a	66.7 m/a
	1.3 m	3.3 m	0 m/a	0 m/a
12	0 m	1 m	0.1 m/a	0 m/a
	1 m	1.3 m	0.1 m/a	66.7 m/a
	1.3 m	3.3 m	0 m/a	0 m/a
13	0 m	1 m	0.1 m/a	0 m/a
	1 m	1.3 m	0.1 m/a	66.7 m/a
	1.3 m	3.3 m	0 m/a	0 m/a
14	0 m	1 m	0.1 m/a	0 m/a
	1 m	1.3 m	0.1 m/a	66.7 m/a
	I 1.3 m	3.3 m	0 m/a	0 m/a
15	, 0 m	1 m	0.1 m/a	0 m/a
	1 m	1.3 m	0.1 m/a	66.7 m/a
	1.3 m	3.3 m	0 m/a	0 m/a

16	0 m 1 m 1.3 m I	1 m 1.3 m 3.3 m	0.1 m/a 0.1 m/a 0 m/a	0 m/a 66.7 m/a 0 m/a
17	0 m	1 m	0.1 m/a	0 m/a
	1 m	1.3 m	0.1 m/a	66.7 m/a
	1.3 m	3.3 m	0 m/a	0 m/a
18	0 m	1 m	0.1 m/a	0 m/a
	1 m	1.3 m	0.1 m/a	66.7 m/a
	1.3 m	3.3 m	0 m/a	0 m/a

#### Laplace Transform Parameters

**TAU** = 7 **N** = 20 **SIG** = 0 **RNU** = 2

#### Monte Carlo Simulation Results

Number of Simulations = 5000 Number of Variables = 1 Number of Data Ranges = 20

Variable # 1 Variable Properties End Time Time Period = 1 Triangular Distribution (Minimum = 15 Maximum = 50 Mode = 25)

Depth = 3.3

#### DISTRIBUTION OF PEAK CONCENTRATION

Minimum	Maximum	Number	Probability	Cumulative	Expected
Value	Value T	Occur.	_	Probability	Value
2.285E+01	2.294E+01	78	0.02	0.02	3.572E-01
2.294E+01	2.303E+01	196	0.04	0.05	9.011E-01
2.303E+01	2.313E+01	208	0.04	0.10	9.601E-01
2.313E+01	2.322E+01	304	0.06	0.16	1.409E+00
2.322E+01	2.331E+01	383	0.08	0.23	1.782E+00
2.331E+01	2.340E+01	489	0.10	0.33	2.284E+00
2.340E+01	2.350E+01	541	0.11	0.44	2.537E+00
2.350E+01	2.359E+01	1044	0.21	0.65	4.916E+00
2.359E+01	2.368E+01	1133	0.23	0.88	5.356E+00
2.368E+01	2.377E+01	66	0.01	0.89	3.132E-01
2.377E+01	2.387E+01	83	0.02	0.91	. 3.954E-01
2.387E+01	2.396E+01	64	0.01	0.92	3.061E-01
2.396E+01	2.405E+01	73	0.01	0.93	3.505E-01
2.405E+01	2.414E+01	73	0.01	0.95	3.518E-01
2.414E+01	2.424E+01	69	0.01	0.96	3.338E-01
2.424E+01	2.433E+01	65	0.01	0.97	3.157E-01
2.433E+01	2.442E+01	57	0.01	0.99	2.779E-01
2.442E+01	2.451E+01	64	0.01	1.00	3.132E-01
2.451E+01	2.461E+01	6	0.00	1.00	2.947E-02
2.461E+01	2.470E+01	4	0.00	1.00	1.972E-02

Expected Maximum Concentration = 2.351E+01

#### DISTRIBUTION OF TIME OF PEAK CONCENTRATION

Minimum	Maximum	Number	Probability	Cumulative	Expected
Value	Value	Occur.	_	Probability	Value
5.500E+01	5.619E+01	20	0.00	0.00	2.224E-01
5.619E+01	5.737E+01	52	0.01	0.01	5.905E-01
5.737E+01	5.856E+01	107	0.02	0.04	1.241E+00
5.856E+01	5.975E+01	140	0.03	0.06	1.656E+00
5.975E+01	6.094E+01	jr 163	0.03	0.10	1.967E+00
6.094E+01	6.212E+01	r 216	0.04	0.14	2.658E+00
6.212E+01	6.331E+01	264	0.05	0.19	3.311E+00
6.331E+01	6.450E+01	303	0.06	0.25	3.873E+00
6.450E+01	6.568E+01	334	0.07	0.32	4.348E+00
6.568E+01	6.687E+01	324	0.06	0.38	4.295E+00
6.687E+01	6.806E+01	300	0.06	0.44	4.048E+00
6.806E+01	6.925E+01	369	0.07	0.52	5.067E+00
6.925E+01	7.043E+01	447	0.09	0.61	6.244E+00
7.043E+01	7.162E+01	380	0.08	0.68	5.398E+00
7.162E+01	7.281E+01	355	0.07	0.75	5.127E+00
7.281E+01	7.400E+01	320	0.06	0.82	4.698E+00
7.400E+01	7.518E+01	279	0.06	0.87	4.162E+00
7.518E+01	7.637E+01	223	0.04	0.92	3.380E+00
7.637E+01	7.756E+01	231	0.05	0.97	3.556E+00
7.756E+01	7.874E+01	173	0.03	1.00	2.704E+00

Expected Time of Maximum Concentration = 68.5444649240847

#### VARIABLE NUMBER: 1

Minimum	Maximum	Number	Probability	Cumulative	Expected
Value	Value	Occur.	_	Probability	Value
1.500E+01	1.674E+01	42	0.01	0.01	1.333E-01
1.674E+01	1.847E+01	128	0.03	0.03	4.506E-01
1.847E+01	2.021E+01	210	0.04	0.08	8.122E-01
2.021E+01	2.194E+01	276	0.06	0.13	1.163E+00
2.194E+01	2.368E+01	403	0.08	0.21	1.838E+00
2.368E+01	2.541E+01	475	0.10	0.31	2.332E+00
2.541E+01	2.715E+01	460	0.09	0.40	2.418E+00
2.715E+01	2.888E+01	455	0.09	0.49	2.549E+00
2.888E+01	3.062E+01	418	0.08	0.57	2.487E+00
3.062E+01	3.235E+01	360	0.07	0.65	2.267E+00
3.235E+01	3.409E+01	333	0.07	0.71	2.212E+00
3.409E+01	3.582E+01	295	0.06	0.77	2.062E+00
3.582E+01	3.756E+01	259	0.05	0.82	1.901E+00
3.756E+01	3.929E+01	209	0.04	0.86	1.606E+00
3.929E+01	4.103E+01	212	0.04	0.91	1.703E+00
4.103E+01	4.276E+01	163	0.03	0.94	1.366E+00
4.276E+01	4.450E+01	133	0.03	0.97	1.161E+00
4.450E+01	4.623E+01	81	0.02	0.98	7.349E-01
4.623E+01	4.797E+01	64	0.01	1.00	6.029E-01
4.797E+01	4.970E+01	24	0.00	1.00	2.344E-01

Expected Value = 3.003E+01

# Description

This example demonstrates how to create a landfill with a composite primary liner, primary and secondary leachate collection systems, and a compacted clay secondary liner. The composite primary liner is composed of a 60 mil (1.5 mm) geomembrane in good contact with a 0.9 m thick compacted clay liner. Small holes with an area of  $0.1 \text{ cm}^2$  and a frequency of 2.5 per hectare (1 per acre) are assumed for the geomembrane. The method proposed by Giroud et al (1992) is used to calculate the flow (leakage) through the composite liner, these calculations are performed automatically by POLLUTE. Below the composite primary liner is a 0.3 m thick granular secondary leachate collection system, overlying a 0.9 m thick compacted clay secondary liner. There is a 3 m thick aquitard under the secondary liner, which overlies a 3 m thick aquifer.

The landfill has a length (L) of 200 m in the direction parallel to groundwater flow in the underlying aquifer. Consideration is being given to a volatile organic contaminant with an initial source concentration of 1500  $\mu$ g/L, which is assumed to remain constant with time over the time period being examined in this example. The leachate head on the composite primary liner is assumed to be constant at 0.3 m, the head on the secondary liner is assumed to be 0.3 m, and the groundwater level relative to the top of the aquifer is assumed to be 3 m (i.e., at the top of the aquitard).

The flow in the aquifer must be established based on hydrogeologic data and is represented in terms of the horizontal Darcy velocity (the "Base Outflow Velocity") in the aquifer at the down-gradient edge of the landfill (see Example 3 for more discussion of Base Outflow Velocity and Aquifer thickness). The parameters used for this example are listed below:

<b><u>Property</u></b>		<u>Value</u>	<u>Units</u>
Geomembrane Contact		Good	-
Geomembrane Holes		Circles	-
Hole Area		0.1	cm <sup>2</sup>
Hole Frequency		1	/acre
Geomembrane Thickness		60	mil
Geomembrane Diffusion Coef.		3.0x10 <sup>-5</sup>	m <sup>2</sup> /a
Source Concentration	c <sub>o</sub>	1500	μg/L
Source Type		Constant	-
Landfill Length	L	200	m
Leachate Head on Primary Liner		0.3	m
Leachate Head on Secondary Liner		0.3	m
Groundwater level in Aquifer		3.0	m
Clay Thickness	Н	0.9	m
Clay Diffusion Coef.	D	0.02	m <sup>2</sup> /a

<u>Property</u>		<u>Value</u>	<u>Units</u>
Clay Distribution Coef.	К <sub>d</sub>	0.5	mL/g
Clay Hydraulic Conductivity	k	1.0x10 <sup>-9</sup>	m/s
Clay Porosity	n	0.35	-
Clay Dry Density		1.9	g/cm <sup>3</sup>
Collection System Thickness	Н	0.3	m
Collection System Dispersion Coef.		100	m <sup>2</sup> /a
Collection System Density		1.9	g/cm <sup>3</sup>
Collection System Distr. Coef.	К <sub>d</sub>	0.0	mL/g
Collection System Porosity	n	0.3	-
Aquitard Thickness	Н	3.0	m
Aquitard Hydraulic Conductivity	k	1.0x10 <sup>-5</sup>	m/s
Aquitard Diffusion Coef.	D	0.02	m <sup>2</sup> /a
Aquitard Dry Density		1.9	g/cm <sup>3</sup>
Aquitard Distribution Coef.	К <sub>d</sub>	0.0	mL/g
Aquitard Porosity	n	0.35	-
Aquifer Thickness	h	3.0	m
Aquifer Porosity	nb	0.3	-
Base Outflow Velocity	vb	10	m/a

# **Data Entry**

Start the POLLUTEv7 program and open the Examples project. Select Case 17 and open the model by double clicking on it in the model list. After the model is displayed, the data for the model can be displayed and edited using the Data Entry menu or by clicking on that part of the model. The data for this type of model is entered differently than the previous models, since it was created using the Primary and Secondary Liner Landfill quick model. The Data Entry menu has two items, model parameters and run parameters.

## **Model Parameters**

To specify the model parameters either click on the model or select the Model Parameters menu item from the Data Entry menu. The Primary and Secondary Liner form on the next page will be displayed.

### **General Tab**

On the General tab shown on the next page, the layers present in the model can be specified. In this example, the model consists of a primary geomembrane, primary liner, secondary liner, aquitard, and aquifer.

1

🗖 Primary and Secondary Liner	- D×
S.Clay Liner Aquitard General Source Heads P.Geomembrane Title Case 17. Landfill with composite primary liner.	Aquifer   O.Velocity P. Leakage   P. Clay Liner   S.Collection
Waste Primary Collection System	Primary Geomembrane C No C Yes Primary Liner
Primary Geomembrane Primary Clay Liner	C No
Secondary Collection System	Secondary Liner C No
Secondary Clay Liner	C No C Yes Aquifer C No C Yes
Aquitard	Units Metric C Imperial
V OK X Cancel	? Help

### Source Tab

The Source tab shown below is used to specify the source information. In this example the source has a constant concentration  $1500 \,\mu$ g/L and a landfill length of 200 m.

🛱 Primary and Secondary Liner	
S.Clay Liner Aquitard Aquifer	0.Velocity
General Source Heads P.Geomembrane P. Leakage P. Clay	Liner S.Collection
Concentration 1500 µg/L Landfill Length 200 m Source Type © Constant Concentration C Finite Mass	
V OK X Cancel ? Help	

### **Heads Tab**

The Heads tab shown on the next page is used to specify the heads on the liners and the groundwater level relative to the aquifer.

Primary and Seco	ndary Liner	、 、			
S.Clay Liner	Aguitard	3	Aguifer	<u>ر ا</u>	√elocity
General Source	Heads P.Geome	embrane	P. Leakage	P. Clay Liner	S.Collection
Leacha	te Head on Primary Liner	0.3	m	<b>.</b>	
Leachate H	lead on Secondary Liner	0.3	m	-	
Groundwater leve	relative to top of Aquifer	3	m	T	
	🖌 ОК	🗙 Cancel	? Help		

### **Primary Geomembrane Tab**

The Primary Geomembrane tab shown below is used to specify the parameters for the geomembrane and the method to calculate the leakage through the geomembrane. In this example, the leakage through the geomembrane will use the method proposed by Giroud & Bonaparte.

🛱 Primary and Secondary Liner	
S.Clay Liner Aquitard	Aquifer 0.Velocity
General Source Heads P.Geomembrane F	P. Leakage P. Clay Liner S.Collection
Name: Geomembrane	Change Symbol
Thickness 60 mil 💌	Leakage Method
Diffusion Coef 3E-5 m2/a 💌	C LEAK, Rowe et al 2004
	Giroud & Bonaparte 1992
Phase Parameter 1	C Equivalent K
V OK X Cancel	? Help

### **Primary Leakage Tab**

The Primary Leakage tab below is used to specify the parameters for the leakage through the primary geomembrane. After the all of the parameters have been specified the Calculate Leakage button can be pressed to calculate the Darcy velocity through the primary composite liner.

🗖 Primary	y and Seco	ondary Liner				- DX
S.C	lay Liner	[ /	Aquitard	Aquifer	0.	Velocity
General	Source	Heads	P.Geomembrane	P. Leakage	P. Clay Liner	S.Collection
		1	Giroud & Bonapa	rte, 1992		
			R			
	ontact		Hole Frequ	ency 2.5	hectare	•
(	Good	O Poor				-
			- Hole 4	rea 0.1	cm2	<b>न</b>
H	ole Type		]		1	- 1
	Circle	C Long				
			_			
⊢P <sup>,</sup>	ermeation		7			
0	Yes	No				
			_			
	ſ	Calculate Leaka	ge Darcy Velo	ity 3.975E-5 m/a	3	
	<u>.</u>			- ,		
		<i>2</i> or		1 200	1	
		V UK	Lance	Help		

### **Primary Clay Liner Tab**

The parameters for the primary clay liner are specified on the Primary Clay Liner tab shown on the next page.

Primary and Secondary Lir	er				
S.Clay Liner	Aquitard	l ubuuu	Aquifer	P Clau Line	0.Velocity
General   Source   Heads	P.Geomei	morane	P. Leakage	T. Cidy Line	™   S.Collection
Name: Clay Liner				////	Change Symbol
Thickness	0.9	m	•		
Density	1.9	kg/m3	•		
Conductivity K	1E-7	cm/s	•		
Diffusion Coef	0.02	m2/a	•		
Distr. Coef	0.5	m3/kg	•		
Porosity	0.35				
✓	ок	Cancel	? Help		

### Secondary Collection Tab

The parameters for the secondary leachate collection system are specified on the Secondary Collection tab shown below.

🗖 Primary and Secondar	y Liner 💦				- D ×
S.Clay Liner	Aquitard	<u>}</u>	Aquifer	. 1	0.Velocity
General Source He	eads P.Geor	membrane	P. Leakage	P. Clay Line	er S.Collection
Name: Collection System					Change Symbol
				- negae -	
Thickr	ness 0.3	m	•		
Der	nsitu 1.9	kg/m3	-		
Diffusion (	Coef  100	m2/a	<b>_</b>		
Distr. (	Coef 0	m3/kg	-		
Por	osity 0.3	[			
Phase Param	eter 1	[			
	🗸 ОК	🗙 Cancel	? Help	<b>b</b>	

### Secondary Liner Tab

🗖 Primary and Secondary Li	ner				- OX
General Source Heads S.Clay Liner	P.Geome Aquitard	emprane	P. Leakage Aquifer	P. Clay Liner	S.Collection
Name: Clay Liner		_	////	Change Symbol	
Thicknes	\$ 0.9	m	•		
Densit	, 1.9	kg/m3	•		
Conductivity I	(  1E-9	m/s	•		
Diffusion Coe	f 0.02	m2/a	•		
Distr. Coe	f 0.5	m3/kg	•		
Porosit	0.35				
1	OK .	🗙 Cancel	? Hel	Þ	

The parameters for the secondary clay liner are specified on the Secondary Liner tab shown below.

### **Aquitard Tab**

The parameters for the aquitard are specified on the Aquitard tab shown below.

🗖 Primary and Secor	ndary Liner	
General Source	Heads P.Geomembrane P.Leal	kage P. Clay Liner S.Collection
S.Clay Liner		juifer 0.Velocity
Name: Aquitard		Change Symbol
	Thickness 3 m	•
	Density 1.9 kg/m3	•
	Conductivity K 1E-5 m/s	•
	Diffusion Coef 0.02 m2/a	•
	Distr. Coef 0.5 m3/kg	•
	Porosity 0.3	
	V OK X Cancel	? Help

### **Aquifer Tab**

👎 Primary and Secondary Liner		
General   Source   Heads   P.Geomembrane	P. Leakage   P. Clay Lin	er S.Collection
S.Clay Liner Aquitard	Aquiter	0.Velocity
Name: Aquifer	Change Sym	bol
	Perijan -	
Thickness 3 m	-	
Porosity 0.3		
1		
V OK X Cancel	? Help	

The parameters for the aquifer are specified on the Aquifer tab shown below.

### **Outflow Velocity Tab**

The outflow velocity in the aquifer can be specified on the Outflow Velocity tab shown below. The minimum outflow velocity for the model will be calculated and shown by the program.

Primary -	and Seconda	ry Liner				- O X
General S.Cla	Source Ì H yLiner	leads P.Geo Aquitar	membrane   d	P. Leakage Aquifer 📐	P. Clay Liner	S.Collection Velocity
-Outflow'	Dutflow Velocity The minimum outflow velocity in the Aquifer that will fulfill the conditions of continuity of flow is: 2.803 m/a					
	Outflow V	elocity 10	m/a	<b>•</b>		
		🖌 ОК	🗙 Cancel	? Help		

## **Run Parameters**

The times and depths to calculate the concentrations can be specified using the Run Parameters menu item on the Data Entry menu. On the Run Parameters form below the times for this model can be specified.

Run Parameters			
Туре	Concentrations at Specified Times		
Tir	nes		
	Number of Times: 5		
	Number: 1 🛛 🖌 🖌 🕨		
	Time: 10 year 💌		
Al	Depths		
•	Yes		
c	No		
	Cancel ? Help		

# **Model Execution**

To run the model and calculate the concentrations either select the Run menu item from the Execute menu or press the Run button on the toolbar.

# **Model Output**

After the model has been executed, the output for the model will be displayed. The initial display will depend on your settings in the program's preferences.

# **Concentration vs Depth**

The Concentration vs. Depth chart below can be displayed by pressing the Concentration vs Depth button on the Output toolbar or selecting the Concentration vs Depth menu item from the Output menu.



# **Output Listing**

To display the output as a text listing that will show the calculated concentrations as numbers, select the List Output menu item from the Output menu or press the Output Listing button on the Output toolbar.

#### THE PASSIVE SINK OPTION HAS BEEN USED NOTE : THE USER IS RESPONSIBLE FOR ENSURING THAT VELOCITY CHANGES ARE CONSISTENT WITH THE PASSIVE SINK

#### Layer Properties

Layer	Thickness	Number of	Coefficient of	Matrix Porosity	Distributon	Dry Density
		µg/∟				
		]				
Fixed Outflow Bottom Boundary						
Landfill Length = 200 m						
Landfill Width = 1 m						
Base Thickness = 3 m						
Base Porosity = 0.3						
Base Outflo	w √Velocity = 10 r	n/a				

#### VELOCITY AND SINK PROFILE:

.

Time Period	Minimum Depth	Maximum Depth	Vertical Velocity	Horizontal Outflow	Phase Parameter
1	0 m 0.001524 m 0.9 m 1.2 m 2.1 m	0.001524 m 0.9 m 1.2 m 2.1 m 5.1 m	3.975E-5 m/a 3.975E-5 m/a 3.975E-5 m/a 3.975E-5 m/a 3.975E-5 m/a	0 m/a 0 m/a 0 m/a 0 m/a 0 m/a	1 1 1 1

Ι

Laplace Transform Parameters

**TAU** = 7 **N** = 20 **SIG** = 0 **RNU** = 2

### Calculated Concentrations at Selected Times and Depths

Time	Depth	Concentration
yr	m	μg/L
10	0.000E+00	1.500E+03
	1.524E-03	6.823E+02
	9.152E-02	4.917E+02
	1.815E-01	3.370E+02
	2.715E-01	2.190E+02
	3.615E-01	1.345E+02
	4.515E-01	7.798E+01
	5.415E-01	4.256E+01
	6.315E-01	2.181E+01
	7.215E-01	1.044E+01

0.315E-01         7.215E-01         9.015E-01         9.015E-01         1.292E+00         1.382E+00         1.472E+00         1.652E+00         1.652E+00         1.742E+00         1.832E+00         2.012E+00         2.012E+00         2.012E+00         2.012E+00         3.002E+00         3.602E+00         3.602E+00         3.902E+00         4.602E+00         4.802E+00         5.102E+00	2.101E+01 1.044E+01 4.532E+00 1.485E+00 5.762E-01 2.090E-01 7.081E-02 2.239E-02 6.608E-03 1.819E-03 4.665E-04 1.115E-04 2.487E-05 5.395E-06 1.203E-08 6.039E-11 6.877E-12 7.519E-13 6.479E-14 4.344E-15 2.236E-16 8.703E-18 2.517E-19 8.435E-22
0.000E+00 1.524E-03 9.152E-02 1.815E-01 2.715E-01 3.615E-01 4.515E-01 5.415E-01 7.215E-01 8.115E-01 9.015E-01 1.202E+00 1.292E+00 1.382E+00 1.652E+00 1.652E+00 1.652E+00 1.652E+00 2.012E+00 2.012E+00 2.012E+00 2.012E+00 3.302E+00 3.302E+00 3.502E+00 4.202E+00 4.202E+00 4.502E+00 5.102E+00	1.500E+03 8.260E+02 6.636E+02 3.968E+02 2.946E+02 2.126E+02 1.488E+02 1.488E+02 1.007E+02 6.553E+01 4.031E+01 2.239E+01 2.238E+01 1.332E+01 7.670E+00 4.275E+00 2.305E+00 1.202E+00 6.060E-01 2.954E-01 1.393E-01 6.381E-02 2.913E-02 1.208E-03 3.221E-05 5.508E-07 6.278E-09 1.246E-10 2.172E-11 4.988E-12 1.028E-12 1.848E-13 6.496E-15
1.524E-03	9.088E+02

	9.152E-02 1.815E-01 2.715E-01 3.615E-01 4.515E-01 5.415E-01 6.315E-01 9.015E-01 9.015E-01 1.202E+00 1.292E+00 1.382E+00 1.472E+00 1.652E+00 1.652E+00 1.832E+00 1.832E+00 2.012E+00 2.012E+00 2.012E+00 2.012E+00 3.002E+00 3.002E+00 3.602E+00 3.902E+00 4.502E+00 1.4502E+	7.644E+02 6.322E+02 5.137E+02 4.098E+02 3.205E+02 2.456E+02 1.837E+02 1.837E+02 9.389E+01 6.252E+01 6.250E+01 4.317E+01 1.932E+01 1.932E+01 1.932E+00 2.986E+00 1.776E+00 1.776E+00 1.040E+00 6.088E-01 6.824E-02 5.728E-03 3.587E-04 1.671E-05 5.782E-07 1.516E-08 4.244E-10 6.379E-11 9.861E-13
50	0.000E+00 1.524E-03 9.152E-02 1.816E-01 2.715E-01 3.615E-01 4.515E-01 5.415E-01 8.115E-01 8.115E-01 9.015E-01 1.202E+00 1.382E+00 1.382E+00 1.652E+00 1.652E+00 1.652E+00 1.652E+00 1.832E+00 2.012E+00 2.012E+00 2.102E+00 2.02E+00 3.002E+00 3.002E+00 3.002E+00 3.002E+00 3.902E+00 3	1.500E+03 1.007E+03 8.850E+02 7.698E+02 6.623E+02 5.634E+02 4.734E+02 3.927E+02 3.210E+02 2.583E+02 2.583E+02 1.573E+02 1.573E+02 1.573E+02 1.573E+01 5.486E+01 4.087E+01 3.008E+01 1.576E+01 1.576E+01 1.576E+01 1.576E+01 1.576E+00 2.028E+00 4.309E-01 7.706E-02 1.459E-03 1.539E-04 1.358E-05

	4.202E+00 4.502E+00 4.802E+00 5.102E+00	1.358E-05 1.003E-06 6.204E-08 6.335E-10
100	0.000E+00 1.524E-03 9.152E-02 1.815E-01 2.715E-01 3.615E-01 4.515E-01 6.315E-01 6.315E-01 7.215E-01 9.015E-01 1.202E+00 1.292E+00 1.382E+00 1.472E+00 1.652E+00 1.652E+00 1.832E+00 1.922E+00 2.012E+00 2.012E+00 2.012E+00 2.02E+00 3.002E+00 3.002E+00 3.002E+00 3.902E+00 4.502E+00 4	1.500E+03 1.124E+03 1.030E+03 9.383E+02 8.503E+02 7.662E+02 6.862E+02 6.106E+02 5.398E+02 4.738E+02 4.738E+02 3.567E+02 3.566E+02 2.265E+02 1.948E+02 1.948E+02 1.948E+02 1.933E+02 1.393E+02 1.393E+02 1.393E+01 8.154E+01 6.789E+01 3.397E+01 1.387E+01 5.537E+00 2.031E+00 6.839E-01 2.112E-01 5.978E-02 1.548E-02 3.554E-03 4.700E 04

#### NOTICE

Although this program has been tested and experience would indicate that it is accurate within the limits given by the assumptions of the theory used, we make no warranty as to workability of this software or any other licensed material. No warranties either expressed or implied (including warranties of fitness) shall apply. No responsibility is assumed for any errors, mistakes or misrepresentations that may occur from the use of this computer program. The user accepts full responsibility for assessing the validity and applicability of the results obtained with this program for any specific case.]

# Case 18: Phase Change

# Description

In this example a phase change in the secondary leachate collection system is modelled using the Phase Change special feature. The landfill has a secondary leachate collection system and liner which overlies a 1 metre thick aquifer. A phase change occurs in the secondary leachate collection system at the interface between the unsaturated and saturated zones, assumed to be .2 and .1 metres thick respectively.

The landfill contains a constant concentration of DCM, which experiences biological decay in the landfill, primary and secondary liners, and the aquifer. A half-life of 10 years in the landfill and 40 years everywhere else is assumed. No biological decay is assumed to occur in the secondary leachate collection system.

The diffusion coefficient of the DCM in the unsaturated zone of the secondary leachate collection system is assumed to be 300 m<sup>2</sup>/a, and in the saturated zone to be 100 m<sup>2</sup>/a (to represent a high degree of mixing in the saturated zone). The phase change parameter for the DCM in the unsaturated zone is Henry's Constant which is assumed to be 0.1 for DCM in this example.

Two layers are used to model the unsaturated and saturated zones of the .3 metre thick secondary leachate collection system. The first layer represents the unsaturated zone and is .2 metres thick. And the second layer represents the saturated zone and is .1 metre thick.

A Darcy velocity of 0.003 m/a is assumed through the primary liner, and 0 m/a through the secondary liner. Thus, for a 500 metre long landfill the outflow rate in the saturated portion of the secondary leachate collection system would be:

Outflow Rate = (500 \* 0.003) / 0.1 = 15 m/a

This example is for a hypothetical landfill and is used to illustrate how to prepare an input file and run an analysis using the Phase Change option. The example is not a prescription for modelling contaminant migration during operation of a landfill. Each landfill has its own unique characteristics and no general prescription can be made. The Phase Change option should only by used by someone with the hydrogeologic background necessary to appreciate the subtleties associated with the physical situation and the steps necessary for appropriate modelling of this physical situation.

# Data Entry

Start the POLLUTEv7 program and open the Examples project. Select Case 18 and open the model by double clicking on it in the model list. After the model is displayed, the data for the model can be displayed and edited using the Data Entry menu or by clicking on that part of the model.

## **General Data**

The general data for this example can be specified by either clicking on the model title or selecting the General Data menu item from the Data Entry menu. On the form below, the Darcy velocity will not show up if the Passive Sink option has already been selected. If the Passive Sink option has not been selected yet, the Darcy velocity will be displayed but will be ignored when the Passive Sink option is selected.

General Data	
Title: Case 18: Phase Change	
Number of Layers: 4	Maximum Depth: 2.65 m
Laplace Transform Parameters	A
TAU: 7 N: 20	SIG: 0 RNU: 2
ОК	X Cancel ? Help

# Layer Data

The layer data for this example consists of four layers: a primary liner, a unsaturated collection system, a saturated collection system, and a secondary liner. The data for these layers can be specified on the forms on the next page, by clicking on the model layer or be selecting the Layer Data menu item from the Data Entry menu.

l
### Layer 1 Primary Liner

Layer Data	
Layer Number 1	
Layer Data Layer Symbol	
Name: Primary Liner	
Number of Sub Layers 4	Fractures
Thickness 0.6 m 💌	None
Dry Density 1.9 g/cm3 💌	C 1 Dimensional
Porosit	C 2 Dimensional
Coef of Hydro Disp 0.02 m2/a 💌	C 3 Dimensional
Distribution Coef 1.5 cm3/g 🗨	· · · · · · · · · · · · · · · · · · ·
V OK X Cancel	<u>? H</u> elp

### Layer 2 Unsaturated Collection System

Layer Data				
Layer Number 2   ( ( ) )				
Layer Data Layer Symbol				
Name: Ufisaturated (	Collection System			
Number of Sub Layers	4		Fractures	
Thickness	0.2 m	•	None	
Dry Density	1.9 g/cm3	- c	1 Dimensional	
Porosity	0.45	С	2 Dimensional	
Coef of Hydro Disp	300 m2/a	• C	3 Dimensional	
Distribution Coef	0 cm3/g	•		
	ОК 🗙 Са	ncel ?	Help	

### Case 18: Phase Change

Layer 3 Saturated Collection System

Layer Data		
	Layer Number 3	
Layer Data   Layer Symbol		
Name: Saturated Col	llection System	
Number of Sub Layers	4	Fractures
Thickness	0.1 m 💌	None
Dry Density	1.9 g/cm3 💌	C 1 Dimensional
Porosity	0.45	C 2 Dimensional
Coef of Hydro Disp	100 m2/a 💌	C 3 Dimensional
Distribution Coef	0 cm3/g 💌	
<b>~</b> (	OK 🗙 Cancel	? Help

### Layer 4 Secondary Liner

Layer Data	
Layer	Number 4   4 + >
Layer Data Layer Symbol	
Name: Secondary Liner	<u>t</u>
Number of Sub Layers 4	Fractures
Thickness 0.75	m 💌 📀 None
Dry Density 1.9	g/cm3  C 1 Dimensional
Porosity 0.4	C 2 Dimensional
Coef of Hydro Disp 0.02	m2/a 💌 C 3 Dimensional
Distribution Coef 1.5	cm3/g 🔻
<b>√</b> 0K	X Cancel ? Help

### **Boundary Conditions**

The boundary conditions for this example are a constant concentration top boundary and a fixed outflow bottom boundary. These boundaries can be specified on the forms below, either by clicking on the boundary or by selecting the Boundary Conditions menu item from the Data Entry menu.

Boundary Conditions	
Bottom - Fixed Outflow	Fixed Outflow Symbol
Boundary Cond ons	Top - Constant Conc.
Constant Top Concentration: 0.	04 mol/m3 🔽
<u>✓ 0</u> K X 9	Cancel ? Help

Boundary Conditions	
Boundary Conditions	Top - Constant Conc.
Bottom - Fixed Duttiow	Fixed Outflow Symbol
Landfill Length: 500	m
Landfill Width: 500	m
Base Thickness: 1	m
Base Porosity: 0.3	_
Base Outflow Velocity: 3	m/a 💌
<u>✓ </u> <u>Ω</u> K	Cancel ? Help

### **Run Parameters**

The run parameters for this example can be specified by selecting the Run Parameters menu item from the Data Entry menu. On the form below the times t o calculate the concentration can be specified as 80, 85, 90, 95, and 100 years.

Run Parameters
Type Concentrations at Specified Times
Times
Number of Times: 5
Number: 1 (
Time: 80 yr 💌
• Yes
Cancel ? Help

# **Special Features**

The biological decay and passive sink data for this model can be entered using the Special Features menu.

### **Radioactive/Biological Decay**

The data for the biological decay of the DCM can be specified by selecting the Radioactive/Biological Decay menu item from the Special Features menu. In this example there are three decay intervals: one for the primary liner, one for the unsaturated and saturated collection system, and one for the secondary liner. This data is entered on the forms shown below.

Radioactive/I	Biological Decay
Decay Range	15
	Number of Depth Rangers:
Source Dec Yes No	say Source Half-Life 10 yr 💌
Base Deca G Yes C No	y Base Half-Life 40 yr 💌
<ul> <li>✓</li> </ul>	OK 🗙 Cancel 🧖 Help

Radioactive/Biological Decay	
Decay Ranges	
Range Number 1	
Top Depth 🚺	m
Bottom Depth 0.6	m
Half Life 40	yr 💌
🗸 ОК 🛛 🗶 С.	ancel <b>?</b> Help

Radioactive/Biological I)eo	cay	
Decay Ranges		
Range Number	2	
Top Depth	0.6	m
Bottom Depth	0.9	m
Half Life	0	yı 💌
🗸 ок	🗙 Cancel	? Help

Radioa	ctive/Bio	ological De	cay		
Decay	Ranges				
	Rang	je Number	3		• •
		Top Depth	0.9	m	•
	В	ottom Depth	1.65	m	•
		Half Life	40	yı	•
[	🗸 0k		🗙 Cancel	?	Help

### **Passive Sink**

The passive sink data is used to specify the Phase parameter and the horizontal and vertical Darcy velocities. In this example there are four depth intervals for the passive sink as shown in the forms below.

Passive Sink
Data Interval Data
Number of Intervals 4
Phase Change
C No C Yes
Inflow Rate
• No C Yes
V OK X Cancel ? Help

Passive Sink	
R	
Data Interval Data	
Depth Interval: 1  4 •	• • •
Top Depth D	•
Bottom Depth 0.6	•
Darcy Velocity 0.003 m	/a 💌
Rate of Removal 0 m	/a 💌
Phase Parameter 1	
V OK X Cancel	<b>?</b> Help

Passive Sink
Data Interval Data Depth Interval: 2   4 4 > >
Top Depth     D.6     m       Bottom Depth     0.8     m       Darcy Velocity     0.003     m/a       Rate of Removal     0     m/a
Phase Parameter 0.1
V OK X Cancel ? Help

Passive Sink			
Data Interval Data	R		
Depth Interval: 3		<b>+                                    </b>	H
Top Depth 🚺	3	m	•
Bottom Depth 0.	3	m	•
Darcy Velocity 0.	003	m/a	•
Rate of Removal 15		m/a	•
Phase Parameter 1			
🗸 ОК 🗙	Cancel	<b>?</b> He	lp

Passive Sink	
Data Interval Data	N
Depth Interval: 4	
Top Depth 0.9	m
Bottom Depth 1.65	m
Darcy Velocity 0	m/a 💌
Rate of Removal 0	m/a 💌
Phase Parameter 1	
🗸 OK 🗙 Car	ncel 🦻 🥐 Help

# **Model Execution**

To run the model and calculate the concentrations either select the Run menu item from the Execute menu or press the Run button on the toolbar.

# **Model Output**

After the model has been executed, the output for the model will be displayed. The initial display will depend on your settings in the program's preferences.

### Case 18: Phase Change

### **Concentration vs Depth**

The Concentration vs. Depth chart below can be displayed by pressing the Concentration vs Depth button on the Output toolbar or selecting the Concentration vs Depth menu item from the Output menu.



### **Output Listing**

To display the output as a text listing that will show the calculated concentrations as numbers, select the List Output menu item from the Output menu or press the Output Listing button on the Output toolbar.

### Case 18: Phase Change

#### THE PASSIVE SINK OPTION HAS BEEN USED NOTE : THE USER IS RESPONSIBLE FOR ENSURING THAT VELOCITY CHANGES ARE CONSISTENT WITH THE PASSIVE SINK

#### Layer Properties

Layer	Thickness	Number of Sublayers	Coefficient of Hydrodynamic Dispersion	Matrix Porosity	Distributon Coefficient	Dry Density
Primary Liner	0.6 m	4	0.02 m2/a	0.4	1.5 cm3/g	1.9 g/cm3
Unsaturated Collection System	0.2 m	4	300 m2/a	0.45	0 cm3/g	1.9 g/cm3 )
Saturated Collection System	0.1 m	4	100 m2/a	0.45	0 cm3/g	] 1.9 g/cm3
Secondary Liner	0.75 m	4	0.02 m2/a	0.4	1.5 cm3/g	ງ 1.9 g/cm3 1

#### **Boundary Conditions**

#### Contant Concentration

Source Concentration = 0.04 mol/m3

#### **Fixed Outflow Bottom Boundary**

Landfill Length = 500 m Landfill Width = 500 m Base Thickness = 1 m Base Porosity = 0.3 Base Outflow Velocity = 3 m/a

#### RADIOACTIVE OR BIOLOGICAL DECAY

#### First Order Radioactive or Biological Decay Depth Ranges

Minimum Depth	Maximum Depth	Half Life
0 m	0.6 m	40 yr
0.6 m	0.9 m	O yr
0.9 m	1.65 m	40 yr

T

Radioactive or Biological Decay Source Half Life = 10 yr

Radioactive or Biological Decay Base Half Life = 40 yr

### VELOCITY AND SINK PROFILE:

Time Period	Minimum Depth	Maximum Depth	Vertical Velocity	Horizontal Outflow	Phase Parameter
1	0 m	0.6 m	0.003 m/a	0 m/a	1
	0.6 m	0.8 m	0.003 m/a	0 m/a	0.1
	0.8 m	0.9 m	0.003 m/a	15 m/a	. 1
	0.9 m	1.65 m	0 m/a	0 m/a	1

### Laplace Transform Parameters

**TAU** = 7 **N** = 20 **SIG** = 0 **RNU** = 2

### Calculated Concentrations at Selected Times and Depths

Time	Depth	Concentration
yr yr	m	mol/m3
80	0.000E+00 1.500E-01 3.000E-01 4.500E-01 6.000E-01 6.500E-01 7.000E-01 7.500E-01 8.000E-01 8.250E-01 8.500E-01 8.750E-01 9.000E-01 1.088E+00 1.275E+00 1.453E+00 1.650E+00	1.563E-04 4.912E-04 7.185E-04 8.173E-04 8.009E-04 8.009E-04 8.009E-04 8.009E-04 8.009E-04 8.009E-04 8.009E-04 8.008E-04 8.008E-04 8.008E-04 6.483E-04 4.620E-04 3.048E-04
85	0.000E+00 1.500E-01 3.000E-01 4.500E-01 6.000E-01 6.500E-01 7.000E-01 7.500E-01 8.250E-01 8.500E-01 8.750E-01 8.750E-01 9.000E-01 1.088E+00 1.275E+00 1.463E+00 1.650E+00	1.105E-04 3.922E-04 5.930E-04 6.923E-04 6.960E-04 6.960E-04 6.960E-04 6.960E-04 6.960E-04 6.960E-04 6.960E-04 6.960E-04 6.960E-04 6.969E-04 5.830E-04 4.321E-04 2.982E-04 2.118E-04
90	0.000E+00	7.816E-05

I	1.500E-01 3.000E-01 4.500E-01 6.000E-01 6.500E-01 7.000E-01 8.000E-01 8.250E-01 8.500E-01 8.750E-01 8.750E-01 1.088E+00 1.275E+00 1.463E+00 1.650E+00	3.151E-04 4.912E-04 5.870E-04 6.040E-04 6.040E-04 6.040E-04 6.040E-04 6.040E-04 6.040E-04 6.040E-04 6.040E-04 6.040E-04 5.220E-04 4.010E-04 2.881E-04 2.118E-04
95	0.000E+00 1.500E-01 3.000E-01 4.500E-01 6.000E-01 6.500E-01 7.000E-01 8.000E-01 8.250E-01 8.500E-01 8.750E-01 8.750E-01 1.088E+00 1.275E+00 1.463E+00 1.650E+00	5.527E-05 2.547E-04 4.083E-04 4.985E-04 5.239E-04 5.239E-04 5.239E-04 5.239E-04 5.239E-04 5.239E-04 5.239E-04 5.239E-04 5.239E-04 5.239E-04 3.698E-04 3.698E-04 2.754E-04 2.087E-04
100	0.000E+00 1.500E-01 3.000E-01 4.500E-01 6.000E-01 6.500E-01 7.000E-01 7.500E-01 8.000E-01 8.250E-01 8.500E-01 8.750E-01 9.000E-01 1.088E+00 1.275E+00 1.463E+00 1.650E+00	3.908E-05 2.072E-04 3.408E-04 4.242E-04 4.544E-04 4.544E-04 4.544E-04 4.544E-04 4.544E-04 4.544E-04 4.544E-04 4.544E-04 4.544E-04 4.544E-04 3.392E-04 2.609E-04 2.029E-04

# Case 19: Multiphase Diffusion Test

# Description

In this example a multiphase diffusion test performed by Buss et al. (1995) is modelled. This test involved the migration of toluene from a 'constant' source through a 0.1 cm thick HDPE geomembrane, a 18.2 cm thick airspace and into a 12.3 cm water reservoir (assumed to be well mixed). Based on Buss et al. the geomembrane diffusion coefficient was 6 x  $10^{-8}$  cm<sup>2</sup>/s and the phase coefficient was 43.8. From Schwarzenbach et al. (1993), the diffusion coefficient and phase coefficient for toluene in air are 0.088 cm<sup>2</sup>/s and 0.27 respectively. Based on these parameters the test is modelled for 600 hours and the calculated and observed concentrations in the receptor are provided at the end of this example.

# **Data Entry**

Start the POLLUTEv7 program and open the Examples project. Select Case 19 and open the model by double clicking on it in the model list. After the model is displayed, the data for the model can be displayed and edited using the Data Entry menu or by clicking on that part of the model.

## **General Data**

The general data for this example can be specified by either clicking on the model title or selecting the General Data menu item from the Data Entry menu. On the form on the next page, the Darcy velocity will not show up if the Passive Sink option has already been selected. If the Passive Sink option has not been selected yet, the Darcy velocity will be displayed but will be ignored when the Passive Sink option is selected.



### **Case 19: Multiphase Diffusion Test**

General Data	4
Title: Case 19: Multiphase Diffusion Test	
Number of Layers: 2	Maximum Depth: 30.6 cm 💌
Laplace Transform Parameters	
TAU: 7 N: 20	SIG: 0 RNU: 2
🖌 ОК	X Cancel ? Help

### Layer Data

The layer data for this example consists of two layers: a geomembrane and an air space. The data for these layers can be specified on the forms below, by clicking on the model layer or be selecting the Layer Data menu item from the Data Entry menu.

### Layer 1 Geomembrane

Layer Data		
	Layer Number 1	
Layer Data Layer Symbol		
Name: Geomembrane		
Number of Sub Layers 1		Fractures
Thickness 0.1	cm 💌	None
Dry Density 2.7	kg/m3 👻	C 1 Dimensional
Porosity 1		C 2 Dimensional
Coef of Hydro Disp 0.00	00216 cm2/hr 💌	C 3 Dimensional
Distribution Coef	m3/kg 💌	
ОК	X Cancel	? Help

### Layer 2 Air Space

Layer Data		
l	ay Number 2	
Layer Data Layer Symbol		
Name: Air Space		
Number of Sub Layers 4		Fractures
Thickness 18.2	cm 💌	None
Dry Density 2.7	kg/m3 💌	C 1 Dimensional
Porosity 1		C 2 Dimensional
Coef of Hydro Disp 316.8	3 cm2/hr 💌	C 3 Dimensional
Distribution Coef	m3/kg 💌	
🗸 ОК	🗶 Cancel	? Help

### **Boundary Conditions**

The boundary conditions for this example are a constant concentration top boundary and a fixed outflow bottom boundary. These boundaries can be specified on the forms below, either by clicking on the boundary or by selecting the Boundary Conditions menu item from the Data Entry menu.

Boundary Conditions	
Bottom - Fixed Outow	Fixed Outflow Symbol
Boundary Conditions	Top - Constant Conc.
Constant Top Concentration: 5	00 mg/L 💌
<u>✓ 0</u> K	Cancel ? Help

Boundary Conditions	
Boundary Conditions	Top - Constant Conc.
Bottom - Fixed Outriow	Fixed Outflow Symbol
Landfill Length: 1	cm 💌
Landfill Width: 1	cm 💌
Base Thickness: 12.3	cm 💌
Base Porosity: 1	Ī
Base Outflow Velocity:	m/a 💌
<u>✓ 0</u> K X Can	cel ? Help

### **Run Parameters**

The run parameters for this example can be specified by selecting the Run Parameters menu item from the Data Entry menu. On the form below the times t o calculate the concentration can be specified as 1, 20, 40, 70, 100, 150, 200, 250, 300, 350, 400. 450, 500, 550, and 600 hours.

Run Parameters
Type Concentrations at Specified Times
Times
Number of Times. 113
Number: 1 🛛 🛛 🖌 🕨
Time: 1 hr
All Depths
C No
✓ OK X Cancel ? Help

# **Special Features**

The passive sink data for this model can be entered using the Special Features menu.

### **Passive Sink**

The passive sink data is used to specify the Phase parameter and the horizontal and vertical Darcy velocities. In this example there are two depth intervals for the passive sink as shown in the forms below.

Passive Sink	Passive Sink
Data Interval Data	Data Interval Data
Depth Interval: 1 🛛 🛛 🖌 🕨	Depth Interval: 2   ( ( )
Top Depth 0 cm 💌	Top Depth 0.1
Bottom Depth 0.1	Bottom Depth 18.3 cm 💌
Darcy Velocity 0 m/a 💌	Darcy Velocity 0 m/a 💌
Rate of Removal 0 m/a 💌	Rate of Removal 0 m/a 💌
Phase Parameter 43.8	Phase Parameter 0.27
V OK X Cancel ? Help	VOK X Cancel ? Help

# **Model Execution**

To run the model and calculate the concentrations either select the Run menu item from the Execute menu or press the Run button on the toolbar.

# **Model Output**

After the model has been executed, the output for the model will be displayed. The initial display will depend on your settings in the program's preferences.

### **Concentration vs Time**

The Concentration vs. Time chart below can be displayed by pressing the Concentration vs Time button on the Output toolbar or selecting the Concentration vs Time menu item from the Output menu.



### **Output Listing**

To display the output as a text listing that will show the calculated concentrations as numbers, select the List Output menu item from the Output menu or press the Output Listing button on the Output toolbar.

### Case 19: Multiphase Diffusion Test

#### THE PASSIVE SINK OPTION HAS BEEN USED NOTE : THE USER IS RESPONSIBLE FOR ENSURING THAT VELOCITY CHANGES ARE CONSISTENT WITH THE PASSIVE SINK

#### Layer Properties

Layer	Thickness	Number of Sublayers	Coefficient of Hydrodynamic Dispersion	Matrix Porosity	, Distributon Coefficient	Dry Density
Geomembrane	0.1 cm	1	0.000216 cm2/hr	1	0 m3/kg	2.7 kg/m3
Air Space	18.2 cm	4	316.8 cm2/hr	1	0 m3/kg	2.7 kg/m3

### **Boundary Conditions**

#### Contant Concentration

Source Concentration = 500 mg/L

#### Fixed Outflow Bottom Boundary

Landfill Length = 1 cm Landfill Width = 1 cm Base Thickness = 12.3 cm Base Porosity = 1 Base Outflow Velocity = 0 m/a

### VELOCITY AND SINK PROFILE:

Time Period	Minimum Depth	Maximum Depth	Vertical Velocity	Horizontal Outflow	Phase Parameter
1	0 cm	0.1 cm	0 m/a	0 m/a	43.8
	0.1 cm	18.3 cm	0 m/a	Om/a	0.27

#### Laplace Transform Parameters

**TAU =** 7 **N =** 20 **SIG =** 0 **RNU =** 2

Calculated Concentrations at Selected Times and Depths

hr         cm         mg/L           1         0.000E400         5.000E402         1.771E04           4.650E400         7.045E05         9.2667E05         9.2667E05           9.200E400         2.667E05         9.110E06         6.398E07           20         0.000E400         5.000E402         3.420E401           1.830E401         3.622E401         3.420E401         3.622E401           1.920E400         3.234E401         3.652E401         3.652E401           1.830E401         2.906E401         9.200E400         3.622E401           40         0.000E400         7.660E401         9.200E401           1.375E401         7.500E401         7.660E401         7.354E401           1.375E401         7.354E401         7.354E401         1.337E402           1.830E401         1.337E402         1.337E402         1.337E402           1.830E401         1.337E402         1.337E402<	Time	Depth	Concentration
1         0.000E+00 1 000E+01 4 650E+02 9 200E+02 1 375E+01         500E+02 7 045E+05 9 110E+06 9 110E+06 9 110E+01           20         0.000E+00 1 000E+01         5.000E+02 3 322E+01           20         0.000E+00 1 000E+01         3.622E+01           40         0.000E+00 1 000E+01         3.622E+01           40         0.000E+00 1 000E+01         6.002E+02           70         0.000E+00 1 000E+01         6.002E+02           70         0.000E+00 1 000E+01         7.660E+01           70         0.000E+00 1 000E+01         1.375E+01           70         0.000E+00 1 0.000E+01         1.375E+02           70         0.000E+00 1 0.000E+01         1.375E+02           100         0.000E+00 1 0.000E+01         1.375E+02           1.375E+01         1.328E+02           1.00E+01         1.328E+02           1.00E+01         1.830E+01           1.375E+01         1.328E+02           1.00E+01         1.830E+01           1.00E+01         1.832E+02           1.00E+01         1.832E+02           1.00E+01         1.832E+02           1.00E+01         1.832E+02           1.00E+01         1.832E+02           1.00E+01         1.832E+02           1.00E+01 <th>hr</th> <th>cm</th> <th>mg/L</th>	hr	cm	mg/L
1000E-01         1.771E-04           9200E+00         2.887E-05           9200E+00         2.887E-05           1.830E+01         8.398E-07           20         0.000E+00         3.622E+01           4.650E+00         3.234E+01           9.200E+00         3.234E+01           9.200E+00         3.234E+01           9.200E+00         3.234E+01           9.200E+00         3.234E+01           9.200E+00         7.660E+01           1.830E+01         2.906E+01           40         0.000E+00         7.660E+01           1.830E+01         7.660E+01           9.200E+00         7.660E+01           1.375E+01         7.660E+01           1.375E+01         7.354E+01           1.375E+01         1.375E+02           1.375E+01         1.372E+02           1.375E+01         1.325E+02           1.375E+01         1.325E+02           1.375E+01         1.325E+02           1.375E+01         1.325E+02           1.375E+01         1.325E+02           1.375E+01         1.325E+02           1.375E+01         1.830E+01           1.830E+01         1.830E+02           1.830E+01	1	0.000E+00	5.000E+02
4 660 E40 9 200E40 1 375 E401         7 045 -05 9 110E-06 9 110E-06 9 110E-06 1 830E401           20         0.000E400 1 000E401         5 000E402 3 420E401           20         0.000E400 1 000E401         3 420E401           9 200E400 9 200E400         3 234E401           9 200E400         3 234E401           9 200E400         3 022E401           1 375E401         3 022E401           1 375E401         3 022E401           1 375E401         2 005E401           1 375E401         7 000E400           1 000E400         7 034E401           70         0 0000E400           1 375E401         7 356E401           1 375E401         1 375E401           1 375E401         1 322E402           1 375E401         1 322E402           1 375E401         1 322E402           1 300E401         1 322E402           1 300E401         1 322E402           1 300E401         1 322E402           1 300E401         1 337E401           1 337E401         1 840E402           1 300E401         1 337E402           1 300E401         1 337E402           1 300E401         2 567E402           1 300E401         2 366E402		1.000E-01	1.771E-04
9,000=400 1,830E+01         2,000=400 8,309E+07           20         0,000E+00 1,000E+01         3,630E+07           20         0,000E+00 4,650E+00         3,622E+01           4,650E+00         3,234E+01           9,200E+00         3,232E+01           1,375E+01         3,062E+01           1,375E+01         3,062E+01           1,000E+01         8,022E+01           40         0,000E+00           1,000E+01         7,034E+01           1,000E+01         7,034E+01           1,000E+01         7,034E+01           1,000E+01         1,375E+01           1,000E+01         1,375E+01           1,000E+01         1,375E+01           1,000E+01         1,375E+02           1,000E+01         1,322E+02           1,000E+01         1,322E+02           1,000E+01         1,322E+02           1,000E+01         1,322E+02           1,375E+01         1,832E+02           1,375E+01         1,832E+02           1,375E+01         1,832E+02           1,375E+01         1,832E+02           1,375E+01         1,832E+02           1,375E+01         1,832E+02           1,375E+01         2,595E+02		4.650E+00	7.045E-05
1.375-401         9.112-66           20         0.000E+00         3.639E-07           20         1.000E-01         3.622E+01           4.650E+00         3.234E+01         3.622E+01           9.200E+00         3.234E+01         3.622E+01           1.375E+01         3.662E+01         3.622E+01           40         0.000E+00         5.000E+02           40         0.000E+01         8.022E+01           41         1.375E+01         7.660E+01           1.375E+01         7.560E+01         7.564E+01           70         0.000E+00         1.387E+02           1.375E+01         1.387E+02         1.387E+02           1.375E+01         1.890E+02         1.387E+02           1.375E+01         1.890E+02         1.387E+02           1.375E+01         1.840E+02         2.566E+02		9.200E+0J	2.687E-05
1.830E-00         6.399E-07           20         0.000E+00         5.000E+02           1.000E-01         3.420E+01         3.420E+01           4.650E+00         3.420E+01         3.052E+01           1.375E+01         3.052E+01         3.052E+01           40         0.000E+00         5.000E+02           9.200E+00         7.834E+01         9.20E+00           9.200E+00         7.660E+01         7.500E+01           9.200E+00         7.660E+01         1.375E+01           70         0.000E+00         5.000E+02           1.375E+01         7.354E+01         7.354E+01           70         0.000E+00         1.375E+02           1.375E+01         1.375E+01         1.375E+02           1.375E+01         1.332E+02         1.375E+02           1.375E+01         1.332E+02         1.375E+01           1.375E+01         1.830E+01         1.836E+02           1.375E+01         1.836E+02         1.375E+01           1.375E+01         1.836E+02         2.567E+02           1.375E+01         1.836E+02         2.567E+02           1.30E+01         2.567E+02         2.568E+02           200         0.000E+00         5.000E+02 <t< th=""><th></th><th>1.375E+U1</th><th>9.110E-06</th></t<>		1.375E+U1	9.110E-06
20         0.000E+00 1.000E+01 9.200E+00 9.200E+00 1.375E+01 1.830E+01         5.000E+02 3.622E+01 3.234E+01 9.200E+00           40         0.000E+01 1.830E+01         5.000E+02 9.206E+01           40         0.000E+01 1.830E+01         5.000E+02 9.206E+01           70         0.000E+01 9.200E+00         7.834E+01 7.500E+01           70         0.000E+01 1.830E+01         1.337E+02 1.337E+02           1.000E-01 1.830E+01         1.337E+02 1.337E+02         1.337E+02 1.337E+02           1.000E-01 1.830E+01         1.337E+02 1.337E+02         1.332E+02           100         0.000E+00 1.337E+01         1.332E+02           100         0.000E+00 1.337E+01         1.332E+02           100         0.000E+00 1.837E+01         1.830E+01           100         0.000E+00 1.837E+01         1.832E+02           100         0.000E+00 1.837E+01         1.832E+02           150         0.000E+00 1.000E+01         2.567E+02 2.565E+02           200         0.000E+01 1.830E+01         3.038E+02           250         0.000E+01 1.830E+01         3.038E+02           250         0.000E+01 1.830E+01         3.038E+02           250         0.000E+01 1.830E+01         3.038E+02           1.830E+01         3.038E+02         3.532E+02 <t< th=""><th></th><th>[ 1.830E+01</th><th>6.369E-07</th></t<>		[ 1.830E+01	6.369E-07
100         000000000000000000000000000000000000	20		5.000E+02
4 650 ± 00 9 200 ± 00 1 .375 ± 01 1 .830 ± 01         3 202 ± 01 3 234 ± 01 3 .062 ± 01           40         0.000 ± 00 1 .000 ± 01 4 .650 ± 00         5 .000 ± 402 7 .650 ± 01           40         0.000 ± 01 1 .830 ± 01         7 .650 ± 01 7 .650 ± 01           70         0.000 ± 00 1 .830 ± 01         7 .650 ± 01 7 .550 ± 01           70         0.000 ± 00 1 .830 ± 01         1 .337 ± 02 1 .337 ± 02 1 .337 ± 01           100         0.000 ± 00 1 .336 ± 02         1 .337 ± 02 1 .337 ± 02           100         0.000 ± 00 1 .337 ± 01         1 .332 ± 02           100         0.000 ± 00 1 .337 ± 02         1 .332 ± 02           100         0.000 ± 00 1 .337 ± 01         1 .332 ± 02           100         0.000 ± 00 1 .337 ± 01         1 .332 ± 02           100         0.000 ± 00 1 .337 ± 01         1 .332 ± 02           100         0.000 ± 00 1 .337 ± 01         1 .830 ± 02           100         0.000 ± 01 1 .830 ± 02         1 .830 ± 02           150         0.000 ± 01 2 .567 ± 02         2 .566 ± 02 2 .566 ± 02 2 .539 ± 02           200         0.000 ± 01 1 .830 ± 01         3 .037 ± 02 2 .539 ± 02           200         0.000 ± 01 1 .308 ± 02         3 .038 ± 02 1 .830 ± 01           250         0.000 ± 01 1 .308 ± 02 1 .830 ± 01         3 .037 ± 02 1 .830 ± 02 1 .830 ± 01	20	1.000E-01	3.622E+01
9 200E +00 1 375E +01 3 35E +01 2 200E +01         3 234E +01 2 200E +01 2 200E +01           40         0.000E +00 1 0.00E +01 9 200E +00 1 375E +01 1 375E +01 2 250         5000E +02 1 375E +01 1 375E +01 2 257E +02 2 250           200         0.000E +00 0 000E +00 1 830E +02 1 375E +01 1 375E +01 1 375E +01 1 313E +02 1 375E +01 1 313E +02 1 375E +01 1 313E +02 1 375E +01 3 3098E +02 1 375E +01 3 3098E +02 1 375E +01 3 3098E +02 1 375E +01 3 3098E +02 1 3098E +02 1 3098E +02 1 3098E +02 1 3098E +02 1 375E +01 3 3098E +02 1 3098E +02 1 3098E +02 1 3098E +02 1 3098E +02 1 375E +01 3 3098E +02 1 3098E +02 1 375E +01 3 3098E +02 1 30		4 650E+00	3 420E+01
1375E+01 1830E+01         3.0622+01 2.996E+01           40         0.000E+00         5.000E+02           40         0.000E+00         7.600E+01           40         1.000E-01         8.1022E+01           4.650E+00         7.634E+01         7.500E+01           9.200E+00         7.660E+01         7.334E+01           70         0.000E+00         1.337E+02           4.650E+00         1.337E+02         4.650E+00           1.375E+01         1.337E+02         4.650E+00           1.375E+01         1.337E+02         4.650E+00           1.375E+01         1.332E+02         4.650E+00           1.375E+01         1.332E+02         4.650E+00           1.000E+01         1.332E+02         4.650E+00           1.000E+01         1.830E+01         1.830E+01           1.000E+01         1.830E+01         1.830E+02           1.000E+01         2.567E+02         2.566E+02           1.375E+01         1.365E+02         2.566E+02           1.375E+01         2.566E+02         2.566E+02           1.375E+01         2.566E+02         3.104E+02           4.650E+00         3.104E+02         4.650E+00           250         0.000E+01         3.104E+02 </th <th></th> <th>9 200E+00</th> <th>3.234E+01</th>		9 200E+00	3.234E+01
1         1         2.906E+01           40         0.000E+00         5.000E+02           1.000E+01         8.022E+01         7.832E+01           9.200E+00         7.832E+01         7.802E+01           1.375E+01         7.500E+01         7.500E+01           1.375E+01         7.500E+01         7.500E+01           70         0.000E+00         5.000E+02           9.200E+00         1.375E+01         1.375E+02           1.375E+01         1.375E+01         1.332F+02           1.375E+01         1.332F+02         1.375E+01           1.375E+01         1.332F+02         1.332F+02           1.330E+01         1.332F+02         1.339E+02           1.330E+01         1.332F+02         1.339E+02           1.000E+01         1.830E+01         1.830E+02           1.000E+01         1.830E+01         1.830E+02           1.000E+01         2.557E+02         4.650E+00           1.000E+01         2.557E+02         4.650E+00           1.000E+01         2.555E+02         2.538E+02           200         0.000E+00         3.104E+02           1.375E+01         3.0389E+02         3.0389E+02           200         0.000E+00         3.532E+02		1.375E+01	3.062E+01
40         0.000E+00 1.000E-01 4.650E+00         5.000E+02 8.022E+01 7.634E+01           40         0.000E-01 1.375E+01         8.022E+01 7.634E+01           9.200E+00 1.375E+01         7.630E+01           70         0.000E+00 1.000E+01         1.375E+02           70         0.000E+00 1.375E+01         1.375E+02           1.375E+01         1.375E+02           1.375E+01         1.355E+02           1.375E+01         1.355E+02           1.375E+01         1.355E+02           1.375E+01         1.355E+02           1.375E+01         1.355E+02           1.375E+01         1.863E+02           1.375E+01         1.863E+02           1.375E+01         1.863E+02           1.375E+01         1.863E+02           1.375E+01         1.863E+02           1.375E+01         2.567E+02           2.00E+00         2.567E+02           1.830E+01         2.568E+02           2.00E+00         3.048E+02           1.375E+01         2.547E+02           2.568E+02         3.048E+02           1.375E+01         3.039E+02           1.333E+01         3.039E+02           1.333E+01         3.039E+02           1.330E+01         3.0		1.830E+01	2.906E+01
40         0.000E+00 1000E+01 4 650E+00         5.000E+02 7 834E+01           9.200E+00         7.660E+01           1.375E+01         7.500E+01           1.375E+01         7.500E+01           70         0.000E+00         5.000E+02           1.376E+01         1.377E+02           4.650E+00         1.377E+02           9.200E+00         1.357E+02           1.376E+01         1.328E+02           1.376E+01         1.328E+02           1.376E+01         1.328E+02           1.376E+01         1.328E+02           1.376E+01         1.328E+02           1.000E-01         5.000E+02           1.830E+01         1.890E+02           1.830E+01         1.890E+02           1.830E+01         1.890E+02           1.830E+01         1.863E+02           1.830E+01         1.863E+02           1.830E+01         2.577E+02           1.830E+01         2.566E+02           1.375E+01         2.566E+02           1.375E+01         2.566E+02           1.375E+01         3.612E+02           1.830E+01         3.039E+02           200         0.000E+00         5.000E+02           1.830E+01         3.038E+0		-	-
1.000-01         61.022-01         7.834-01           9.2002+00         7.6602+01           9.2002+00         7.6602+01           1.3752+01         7.5602+01           1.8302+01         7.3542+01           70         0.0002+00         5.0002+02           1.8302+01         1.3372+02           4.6502+00         1.3372+02           9.2002+00         1.3525+02           1.3752+01         1.3225+02           1.3752+01         1.3225+02           1.3752+01         1.3225+02           1.000         0.0002+00         5.0002+02           1.8302+01         1.8762+02           9.2002+00         1.8762+02           9.2002+00         1.8762+02           9.2002+00         1.8902+02           1.8302+01         1.8402+02           1.8302+01         1.8402+02           1.8302+01         2.5672+02           9.2002+00         2.5672+02           9.2002+00         2.5682+02           9.2002+00         3.1132+02           4.6502+01         3.1328+02           200         0.0002+00         5.0002+02           1.3752+01         3.0832+02           1.3002+02         3.6322+02	40	0.000E+00	5.000E+02
4.650±400         7.630±401           1.375±401         7.600±401           1.375±401         7.500±401           70         0.000±400         5.000±402           1.000±01         1.387±402           4.650±400         1.375±401           9.200±400         1.365±402           1.375±401         1.342±402           1.375±401         1.342±402           1.339±402         1.339±402           1.000±01         1.890±402           1.830±401         1.329±402           1.000±01         1.890±402           4.650±400         1.890±402           4.650±400         1.890±402           4.650±400         1.890±402           4.650±400         1.863±402           1.375±401         1.861±402           1.830±401         1.840±402           1.000±01         2.566±402           9.200±400         2.566±402           9.200±400         3.03±402           1.337±401         2.539±402           200         0.000±400         3.008±402           1.337±401         3.03±402           200         0.000±400         3.03±402           200         0.000±400         3.03±402 <th></th> <th></th> <th>8.022E+01</th>			8.022E+01
9.200E401         7.600E401           1.375E401         7.600E401           1.830E401         7.354E401           70         0.000E400         5.000E402           1.000E01         1.337E402           4.650E400         1.337E402           9.200E400         1.337E402           1.375E401         1.342E402           1.375E401         1.342E402           1.339E401         1.342E402           1.339E401         1.342E402           1.339E401         1.342E402           1.339E401         1.342E402           1.339E401         1.342E402           1.800E401         1.840E402           100         0.000E400         5.000E402           1.830E401         1.863E402           1.337E401         1.863E402           1.337E401         1.840E402           150         0.000E400         2.566E402           9.200E400         2.566E402           1.375E401         2.537E402           1.830E401         2.539E402           200         0.000E400         3.008E402           200         0.000E400         3.037E402           1.3375E401         3.038E402           1.3375E401		4.650E+00	7.834E+01
1.335EH01         7.50EH01         7.50EH01           70         0.000E+00         5.000E+02           4.650E+00         1.337E+02           9.200E+00         1.335E+01           1.375E+01         1.342E+02           1.000E-01         1.355E+02           1.375E+01         1.342E+02           1.000E-01         1.342E+02           1.000E-01         1.890E+02           1.000E-01         1.890E+02           1.000E-01         1.890E+02           1.830E+01         1.835E+02           1.375E+01         1.835E+02           1.375E+01         1.835E+02           1.375E+01         1.835E+02           1.375E+01         1.835E+02           1.830E+01         2.577E+02           4.650E+00         2.577E+02           4.650E+00         2.566E+02           9.200E+00         2.566E+02           9.200E+00         2.566E+02           9.200E+00         3.103E+02           200         0.000E+00         5.000E+02           1.375E+01         3.083E+02           200         0.000E+00         3.03Fe+02           1.375E+01         3.083E+02           1.375E+01         3.083E+02 </th <th></th> <th></th> <th></th>			
1.000E-01         7.000E+01           70         0.000E+00         5.000E+02           1.000E-01         1.376E+02           9.200E+00         1.376E+02           1.375E+01         1.342E+02           1.375E+01         1.342E+02           1.375E+01         1.342E+02           1.830E+01         1.322E+02           100         0.000E+00         5.000E+02           1.830E+01         1.332E+02           100         0.000E+00         1.385E+02           100         0.000E+00         1.890E+02           100         0.000E+00         1.885E+02           9.200E+00         1.851E+02           1.830E+01         1.851E+02           1.830E+01         1.865E+02           9.200E+00         2.566E+02           1.375E+01         2.566E+02           1.375E+01         2.539E+02           200         0.000E+00         3.000E+02           1.300E+01         3.039E+02           250         0.000E+00         3.632E+02           1.330E+01         3.039E+02         3.532E+02           250         0.000E+00         3.532E+02           250         0.000E+00         3.632E+02			/ .000⊑+01 7.354⊑±04
70         0.000E+00         5.000E+02           1.000E-01         1.377E+02         1.377E+02           4.650E+000         1.375E+01         1.375E+02           9.200E+000         1.355E+01         1.342E+02           1.300E+01         1.322E+02         1.332E+02           1.00         0.000E+00         5.000E+02           1.00         0.000E+00         1.376E+01           1.000E-01         1.890E+02         1.876E+02           1.375E+01         1.876E+02         1.876E+02           1.375E+01         1.876E+02         1.830E+02           1.375E+01         1.851E+02         1.830E+02           1.50         0.000E+00         5.000E+02           1.375E+01         2.577E+02         2.566E+02           2.000         0.000E+00         2.556E+02           1.375E+01         2.539E+02         2.539E+02           200         0.000E+00         3.113E+02           1.375E+01         3.132E+01         3.097E+02           1.375E+01         3.507E+01         3.507E+02           250         0.000E+00         3.601E+02           250         0.000E+00         3.602E+02           250         0.000E+01         3.507E+02		1.0302401	7.354E#01
1000E-01         1.387E+02           4.650E+00         1.375E+01           1.375E+01         1.342E+02           1.375E+01         1.342E+02           100         0.000E+00         5.000E+02           1.000E-01         1.890E+02           4.650E+00         1.876E+02           9.200E+00         1.876E+02           1.000E-01         1.890E+02           4.650E+00         1.876E+02           1.375E+01         1.861E+02           1.330E+01         1.861E+02           1.830E+01         2.567E+02           1.830E+01         2.567E+02           1.000E-01         2.566E+02           1.375E+01         2.568E+02           1.375E+01         2.568E+02           1.375E+01         2.537E+02           1.830E+01         2.538E+02           200         0.000E+00         5.000E+02           1.830E+01         3.113E+02           200         1.000E-01         3.113E+02           200         0.000E+00         3.087E+02           1.375E+01         3.083E+02         3.083E+02           1.375E+01         3.083E+02         3.083E+02           1.375E+01         3.532E+02         3.532E+	70	0.000E+00	5.000E+02
4 650E+00         1 370E+02           9 200E+00         1.375E+01           1.375E+01         1.342E+02           1.000         0.000E+00           1.000E-01         1.830E+01           1.000E-01         1.870E+02           4.650E+00         1.875E+02           9.200E+00         1.875E+01           1.830E+01         1.865E+02           1.375E+01         1.865E+02           1.830E+01         1.865E+02           1.830E+01         1.865E+02           1.830E+01         2.567E+02           1.830E+01         2.566E+02           2.566E+02         2.566E+02           9.200E+00         3.104E+02           1.330E+01         2.539E+02           200         0.000E+00         5.000E+02           1.375E+01         2.547E+02           1.375E+01         2.539E+02           200         0.000E+00         3.103E+02           250         0.000E+00         3.0397E+02           1.375E+01         3.083E+02         3.532E+02           250         0.000E+00         3.532E+02           250         0.000E+00         3.532E+02           250         0.000E+00         3.532E+02 </th <th></th> <th>1.000E-01</th> <th>1.387E+02</th>		1.000E-01	1.387E+02
9.200E+00         1.355E+02           1.375E+01         1.342E+02           100         0.000E+00         1.329E+02           100         0.000E+00         1.890E+02           4.650E+00         1.875E+02         9.200E+00           9.200E+00         1.863E+02         1.863E+02           1.375E+01         1.863E+02         1.863E+02           1.375E+01         1.863E+02         1.863E+02           1.375E+01         1.863E+02         2.565E+02           1.375E+01         2.565E+02         2.565E+02           1.375E+01         2.565E+02         2.565E+02           1.375E+01         2.547E+02         2.565E+02           1.375E+01         2.547E+02         2.539E+02           200         0.000E+00         5.000E+02           1.000E-01         3.113E+02         3.087E+02           200         0.000E+00         3.097E+02           250         0.000E+00         3.038E+02           250         0.000E+00         3.533E+02           250         0.000E+00         3.532E+02           250         0.000E+00         3.537E+02           250         0.000E+00         3.517E+02           1.330E+01         3.50		4.650E+00	1.370E+02
1.375E+01         1.342E+02           100         0.000E+00         5.000E+02           1.00         1.000E-01         1.890E+02           1.00         1.000E-01         1.890E+02           1.01         1.830E+01         1.863E+02           1.01         1.830E+01         1.863E+02           1.01         1.830E+01         1.863E+02           1.1375E+01         1.863E+02         1.863E+02           1.1300E+01         2.577E+02         4.650E+00           1.000E-01         2.566E+02         2.566E+02           1.375E+01         2.566E+02         2.539E+02           200         0.000E+00         5.000E+02           1.830E+01         3.104E+02         2.539E+02           200         0.000E+00         3.104E+02           200         0.000E+00         3.089E+02           1.375E+01         3.089E+02         3.089E+02           1.380E+01         3.083E+02         3.083E+02           250         0.000E+00         3.530E+02           1.830E+01         3.532E+02         3.532E+02           3.00         0.000E+00         3.532E+02           3.00         0.000E+00         3.532E+02           3.000E+00 <th></th> <th>9.200E+00</th> <th>1.355E+02</th>		9.200E+00	1.355E+02
1830E+01         1.329E+02]           100         0.000E+00         5.000E+02           1.000E-01         1.890E+02         1.890E+02           4.650E+00         1.876E+02         9.200E+00           1.375E+01         1.851E+02         1.830E+01           150         0.000E+00         2.507E+02           150         0.000E+00         2.567E+02           9.200E+00         2.566E+02           9.200E+00         2.566E+02           9.200E+00         2.566E+02           9.200E+00         2.567E+02           1.330E+01         2.539E+02           1.830E+01         2.539E+02           1.830E+01         3.113E+02           1.830E+01         3.097E+02           1.830E+01         3.097E+02           1.830E+01         3.083E+02           250         0.000E+00         5.000E+02           1.330E+01         3.083E+02           250         0.000E+00         3.530E+02           1.830E+01         3.530E+02           1.330E+01         3.530E+02           1.330E+01         3.530E+02           1.330E+01         3.532E+02           1.330E+01         3.507E+02           1.330E+01 <th></th> <th>1.375E+01</th> <th>1.342E+02</th>		1.375E+01	1.342E+02
100         0.000E+00         5.000E+02           1.000E-01         1.890E+02         1.890E+02           4.650E+00         1.876E+02         1.876E+02           9.200E+00         1.863E+02         1.863E+02           1.375E+01         1.851E+02         1.851E+02           1.50         0.000E+00         5.000E+02           150         0.000E+00         2.656E+02           9.200E+00         2.656E+02           1.375E+01         2.658E+02           1.375E+01         2.639E+02           200         0.000E+00         5.000E+02           9.200E+00         2.656E+02           1.375E+01         2.639E+02           1.375E+01         3.113E+02           4.650E+00         3.113E+02           9.200E+00         3.097E+02           1.375E+01         3.083E+02           1.330E+01         3.0382E+02           250         0.000E+00         5.000E+02           1.330E+01         3.632E+02           9.200E+00         3.533E+02           9.200E+00         3.533E+02           9.200E+00         3.517E+02           1.375E+01         3.523E+02           9.200E+00         3.517E+02		1.830E+01	1.329E+02
1.000E-01         1.800E+02           4.650E+00         1.876E+02           9.200E+00         1.863E+02           1.375E+01         1.863E+02           1.830E+01         1.863E+02           1.830E+01         1.863E+02           1.830E+01         1.863E+02           1.830E+01         1.863E+02           1.830E+01         1.863E+02           1.830E+01         2.577E+02           4.650E+00         2.556E+02           9.200E+00         2.556E+02           1.375E+01         2.539E+02           1.830E+01         2.539E+02           1.830E+01         3.113E+02           200         0.000E+00         5.000E+02           1.375E+01         3.192+02           1.375E+01         3.089E+02           1.375E+01         3.089E+02           1.375E+01         3.083E+02           1.300E+00         3.530E+02           1.300E+01         3.530E+02           1.300E+01         3.530E+02           1.375E+01         3.512E+02           1.375E+01         3.512E+02           1.300E+01         3.512E+02           1.300E+01         3.512E+02           1.300E+01         3.551	100		5 000E+02
4.650E+00         1.876E+02           9.200E+00         1.837E+02           1.375E+01         1.831E+02           1.830E+01         1.863E+02           150         0.000E+00         5.000E+02           1.800E+00         2.565E+02           9.200E+00         2.565E+02           9.200E+00         2.565E+02           9.200E+00         2.565E+02           1.830E+01         2.539E+02           1.830E+01         2.539E+02           200         0.000E+00         5.000E+02           1.830E+01         3.113E+02           4.650E+00         3.104E+02           9.200E+00         3.097E+02           1.375E+01         3.083E+02           1.830E+01         3.083E+02           1.830E+01         3.083E+02           1.830E+01         3.032E+02           250         0.000E+00         5.000E+02           1.830E+01         3.532E+02           9.200E+00         3.517E+02           1.375E+01         3.507E+02           1.375E+01         3.507E+02           1.375E+01         3.507E+02           1.380E+01         3.507E+02           3.507E+02         3.856E+02	100	1.000E-01	1.890E+02
9.200E+00         1.863E+02           1.375E+01         1.851E+02           1.800E+01         1.81E+02           150         0.000E+00         5.000E+02           1.000E-01         2.577E+02           4.650E+00         2.566E+02           9.200E+00         2.566E+02           9.200E+00         2.539E+02           1.830E+01         2.539E+02           200         0.000E+00         5.000E+02           1.830E+01         2.539E+02           200         0.000E+00         3.113E+02           4.650E+00         3.104E+02           9.200E+00         3.097E+02           1.830E+01         3.089E+02           1.375E+01         3.089E+02           1.375E+01         3.089E+02           1.375E+01         3.089E+02           1.375E+01         3.089E+02           1.375E+01         3.502E+02           250         0.000E+00         5.000E+02           1.830E+01         3.532E+02           250         0.000E+00         3.532E+02           250         0.000E+00         3.517E+02           1.830E+01         3.507E+02         3.507E+02           300         0.000E+00 <t< th=""><th></th><th>4.650E+00</th><th>1.876E+02</th></t<>		4.650E+00	1.876E+02
1.375E+01         1.851E+02           150         0.000E+00         5.000E+02           150         1.000E-01         2.577E+02           4.650E+00         2.566E+02         2.566E+02           9.200E+00         2.556E+02         2.539E+02           1.375E+01         2.539E+02         2.539E+02           200         0.000E+00         5.000E+02           1.830E+01         2.539E+02         2.539E+02           200         0.000E+00         3.113E+02           4.650E+00         3.104E+02         9.200E+00           1.830E+01         3.089E+02         3.089E+02           1.830E+01         3.083E+02         3.083E+02           250         0.000E+00         3.530E+02           1.830E+01         3.083E+02         3.530E+02           250         0.000E+00         3.532E+02           9.200E+00         3.512E+02         3.512E+02           1.375E+01         3.507E+02         3.512E+02           300         0.000E+00         1         5.000E+02           1.830E+01         3.507E+02         3.855E+02           300         0.000E+00         1         3.855E+02           300         0.000E+00         3.855E+02 <th></th> <th>9.200E+00</th> <th>1.863E+02</th>		9.200E+00	1.863E+02
1.830E+01         1.840E+02           150         0.000E+00         5.000E+02           150         1.00E-01         2.577E+02           4.650E+00         2.566E+02         2.566E+02           9.200E+00         2.565E+02         2.539E+02           1.375E+01         2.539E+02         2.539E+02           200         0.000E+00         5.000E+02           1.830E+01         2.539E+02         3.113E+02           200         0.000E+00         3.113E+02           200         0.000E+00         3.097E+02           1.375E+01         3.089E+02         3.089E+02           1.375E+01         3.089E+02         3.083E+02           250         0.000E+00         3.530E+02           250         0.000E+00         3.532E+02           9.200E+00         3.532E+02           9.200E+00         3.512E+02           1.375E+01         3.507E+02           1.830E+01         3.507E+02           300         0.000E+00         1           300         0.000E+00         3.855E+02           300         0.000E+00         3.855E+02           300         0.000E+00         3.855E+02           3.855E+00         3.855E		1.375E+01	1.851E+02
150         0.000E+00         5.000E+02           150         1.000E-01         2.577E+02           4.650E+00         2.566E+02         2.566E+02           9.200E+00         2.565E+02         2.539E+02           1.830E+01         2.539E+02         2.539E+02           200         0.000E+00         5.000E+02           1.830E+01         3.113E+02         4.650E+00           9.200E+00         3.104E+02         9.200E+00           9.200E+00         3.097E+02         3.097E+02           1.375E+01         3.089E+02         3.083E+02           250         0.000E+00         5.000E+02           1.000E-01         3.533E+02         3.533E+02           250         0.000E+00         3.532E+02           1.375E+01         3.532E+02         3.532E+02           250         0.000E+00         3.512E+02           1.830E+01         3.512E+02         3.512E+02           1.830E+01         3.507E+02         3.856E+02           300         0.000E+00         1.385E+02           300         0.000E+00         1.385E+02           300         0.000E+00         3.856E+02		1.830E+01	1.840E+02
130         0.000E+00 1.000E+00         3.000E+02 2.556E+02           9.200E+00         2.556E+02           1.375E+01         2.539E+02           1.830E+01         2.539E+02           200         0.000E+00         5.000E+02           1.000E-01         3.113E+02           4.650E+00         3.104E+02           9.200E+00         3.097E+02           1.375E+01         3.089E+02           1.375E+01         3.089E+02           1.375E+01         3.083E+02           1.375E+01         3.083E+02           1.375E+01         3.083E+02           1.375E+01         3.083E+02           250         0.000E+00         5.000E+02           1.000E-01         3.532E+02           1.375E+01         3.532E+02           9.200E+00         3.517E+02           1.375E+01         3.512E+02           1.375E+01         3.517E+02           1.375E+01         3.507E+02           1.375E+01         3.507E+02           1.000E-01         3.5507E+02           1.000E+00         1.000E+00           1.000E+01         3.850E+02           3.00         0.000E+00         3.850E+02           3.850E+02	150	0.0005.00	E 000E ±00
1.660E+00         2.576E+02           9.200E+00         2.56E+02           1.375E+01         2.539E+02           1.830E+01         2.539E+02           200         0.000E+00         5.000E+02           1.830E+01         3.113E+02           4.650E+00         3.104E+02           9.200E+00         3.097E+02           1.375E+01         3.089E+02           1.375E+01         3.089E+02           1.375E+01         3.089E+02           1.375E+01         3.083E+02           1.830E+01         3.083E+02           250         0.000E+00           1.830E+01         3.530E+02           1.830E+01         3.532E+02           250         0.000E+00           1.375E+01         3.512E+02           1.375E+01         3.512E+02           1.375E+01         3.512E+02           1.375E+01         3.512E+02           1.830E+01         3.507E+02           300         0.000E+00         1           1.830E+01         3.507E+02           3.850E+02         3.850E+02           4.650E+00         3.855E+02           4.650E+00         3.850E+02	150	1.000E-01	2 577E±02
9.200E+00 1.375E+01 1.830E+01         2.556E+02 2.539E+02           200         0.000E+00 1.000E-01 4.650E+00 9.200E+00         5.000E+02 3.113E+02 3.097E+02           200         0.000E+00 1.375E+01 3.083E+01         3.008E+02 3.083E+02           250         0.000E+00 1.000E-01 4.650E+00 9.200E+00 1.000E-01 4.650E+00 9.200E+00 1.830E+01         5.000E+02 3.532E+02 3.512E+02 1.375E+01 1.830E+01           300         0.000E+00 1.000E-01 4.650E+00 3.650E+02         3.650E+02 3.855E+02 3.855E+02		4.650E+00	2.577E+02
1.375E+01 1.830E+01         2.547E+02 2.539E+02           200         0.000E+00 1.000E-01         5.000E+02 3.113E+02           4.650E+00         3.104E+02           9.200E+00         3.097E+02           1.375E+01         3.089E+02           1.375E+01         3.089E+02           1.375E+01         3.083E+02           250         0.000E+00           250         5.000E+02           1.00E-01         3.530E+02           3.032         0.000E+00           300         0.000E+00           1.375E+01         3.507E+02           300         0.000E+00           1.000E-01         3.507E+02           3.507E+02         3.855E+02           300         0.000E+00         3.855E+02           3.855E+01         3.855E+02           3.855E+02         3.855E+02		9 200 E +00	2.556E+02
1.830E+01         2.539E+02           200         0.000E+00         5.000E+02           1.000E-01         3.113E+02           4.650E+00         3.104E+02           9.200E+00         3.097E+02           1.375E+01         3.089E+02           1.330E+01         3.083E+02           250         0.000E+00         5.000E+02           1.830E+01         3.0382E+02           250         0.000E+00         3.530E+02           1.830E+01         3.503E+02           250         0.000E+00         3.530E+02           1.830E+01         3.532E+02           9.200E+00         3.517E+02           1.375E+01         3.512E+02           1.830E+01         3.507E+02           300         0.000E+00         1           300         0.000E+00         3.856E+02           300         0.000E+00         3.856E+02           300         0.000E+00         3.856E+02           300         0.000E+00         3.856E+02           3.850E+01         3.856E+02		1.375E+01	2.547E+02
200         0.000E+00         5.000E+02           1.000E-01         3.113E+02         4.650E+00         3.104E+02           9.200E+00         3.097E+02         1.375E+01         3.089E+02           1.375E+01         3.083E+02         3.083E+02           250         0.000E+00         3.530E+02           1.830E+01         3.532E+02           250         0.000E+00         3.512E+02           1.375E+01         3.512E+02           1.375E+01         3.512E+02           1.375E+01         3.512E+02           1.330E+01         3.507E+02           300         0.000E+00         1           300         0.000E+00         3.865E+02           300         0.000E+00         3.865E+02           300         0.000E+00         3.850E+01		1.830E+01	2.539E+02
200         0.000E+00         5.000E+02           1.000E-01         3.113E+02           4.650E+00         3.104E+02           9.200E+00         3.097E+02           1.375E+01         3.089E+02           1.830E+01         3.083E+02           250         0.000E+00         5.000E+02           1.830E+01         3.530E+02           250         0.000E+00         3.530E+02           1.830E+01         3.530E+02           3.512E+02         3.512E+02           1.830E+01         3.512E+02           1.830E+01         3.507E+02           300         0.000E+00         1           300         0.000E+00         3.855E+02           4.650E+00         3.855E+02           3.855E+02         3.855E+02			
1.000E-01         3.113E+02           4.650E+00         3.104E+02           9.200E+00         3.097E+02           1.375E+01         3.089E+02           1.375E+01         3.083E+02           250         0.000E+00           1.000E-01         3.530E+02           4.650E+00         3.523E+02           9.200E+00         3.517E+02           1.375E+01         3.512E+02           9.200E+00         3.517E+02           1.375E+01         3.512E+02           1.830E+01         3.507E+02           300         0.000E+00         1           300         0.000E+00         3.865E+02           4.650E+00         3.850E+02           3.850E+01         3.850E+02	200	0.000E+00	5.000E+02
4.650E+00         3.104E+02           9.200E+00         3.097E+02           1.375E+01         3.089E+02           1.830E+01         3.083E+02           250         0.000E+00         5.000E+02           1.000E-01         3.530E+02           4.650E+00         3.512E+02           9.200E+00         3.512E+02           1.375E+01         3.512E+02           1.830E+01         3.507E+02           1.830E+01         3.507E+02           300         0.000E+00         1.3856E+02           4.650E+00         3.850E+02           300         0.000E+00         3.850E+02           300         0.000E+00         3.850E+02			3.113E+02
3.200E+00         3.097E+02           1.375E+01         3.089E+02           1.830E+01         3.083E+02           250         0.000E+00         5.000E+02           1.000E-01         3.530E+02           4.650E+00         3.512E+02           9.200E+00         3.512E+02           1.375E+01         3.512E+02           1.330E+01         3.507E+02           300         0.000E+00         1           300         0.000E+00         3.850E+02           300         0.000E+00         3.850E+02           300         0.000E+00         3.850E+02           3.850E+01         3.850E+02		4.650E+00	3.104E+02
1.375E+01         3.089E+02           1.830E+01         3.083E+02           250         0.000E+00         5.000E+02           1.000E-01         3.530E+02           4.650E+00         3.523E+02           9.200E+00         3.512E+02           1.375E+01         3.512E+02           1.375E+01         3.512E+02           1.375E+01         3.507E+02           300         0.000E+00         1           300         0.000E+00         3.850E+02           4.650E+00         3.850E+02		9.200E+00 1.275E (01	3.09/E+02
250         0.000E+00         5.003E+02           250         0.000E+00         3.530E+02           4.650E+00         3.523E+02           9.200E+00         3.517E+02           1.375E+01         3.512E+02           1.830E+01         3.507E+02           300         0.000E+00         1           4.650E+00         3.507E+02           300         0.000E+00         1           3.855E+02         3.855E+02           4.650E+00         3.855E+02			3.009000
250 0.000E+00 5.000E+02 1.000E-01 3.530E+02 4.650E+00 3.523E+02 9.200E+00 3.517E+02 1.375E+01 3.512E+02 1.830E+01 3.507E+02 300 0.000E+00 1 5.000E+02 1.000E-01 3.855E+02 3.855E+02 3.850E+02		1.0300+01	3.003E+02
1.000E-01         3.530E+02           4.650E+00         3.523E+02           9.200E+00         3.517E+02           1.375E+01         3.512E+02           1.830E+01         3.507E+02           300         0.000E+00         1           1.000E-01         1         3.855E+02           4.650E+00         3.855E+02         3.855E+02	250	0.000E+00	5.000E+02
4.650E+00         3.523E+02           9.200E+00         3.517E+02           1.375E+01         3.512E+02           1.830E+01         3.507E+02           300         0.000E+00         1           1.000E-01         3.855E+02           4.650E+00         3.855E+02           4.650E+00         3.850E+02		1.000E-01	3.530E+02
9.200E+00         3.517E+02           1.375E+01         3.512E+02           1.830E+01         3.507E+02           300         0.000E+00         1           1.000E-01         3.855E+02           4.650E+00         3.850E+012		4.650E+00	3.523E+02
1.375E+01         3.512E+02           1.830E+01         3.507E+02           300         0.000E+00         1           1.000E-01         3.855E+02           4.650E+00         3.850E+02		9.200E+00	3.517E+02
1.830E+01         3.507E+02           300         0.000E+00         I           1.000E-01         3.855E+02           4.650E+00         3.850E+02		1.375E+01	3.512E+02
300 0.000E+00 1 5.000E+02 1.000E-01 3.855E+02 4.650E+00 3.850E+02		1.830E+01	3.507E+02
1.000E-01 - 3.855E+02 4.650E+00 - 3.855E+02	300		 τ τ 5,000Ε+02
4 650E+00 3 850E+02		1 000E-00	38555+02
		4.650E+00	3.850E+02

Т	9.200E+00 1.375E+01 1.830E+01	3.845E+02 <sup>1</sup> 3.841E+02 3.837E+02
350	0.000E+00 1.000E-01 4.650E+00 9.200E+00 1.375E+01 1.830E+01	5.000E+02 4.108E+02 4.104E+02 4.100E+02 4.007E+02 4.097E+02 4.094E+02
400	0.000E+00 1.000E-01 4.650E+00 9.200E+00 1.375E+01 1.830E+01	5.000E+02 4.305E+02 4.302E+02 4.299E+02 4.299E+02 4.297E+02 - 4.294E+02
450	0.000E+00 1.000E-01 4.650E+00 9.200E+00 1.375E+01 1.830E+01	5.000E+02 4.459E+02 - 4.456E+02 4.454E+02 4.454E+02 4.452E+02 4.452E+02 4.450E+02
500	0.000E+00 1.000E-01 4.650E+00 9.200E+00 1.375E+01 1.830E+01	5.000E+02 4.578E+02 4.577E+02 4.575E+02 4.575E+02 4.573E+02 4.572E+02
550	0.000E+00 1.000E-01 4.650E+00 9.200E+00 1.375E+01 1.830E+01	5.000E+02 4.672E+02 4.670E+02 4.669E+02 4.668E+02 4.668E+02 4.666E+02
600 T	0.000E+00 1.UUUE-U1 4.650E+00 9.200E+00 1.375E+01 1.830E+01	5.000E+02 4.744E+02 4.743E+02 4.742E+02 4.741E+02 4.740E+02

#### NOTICE

Although this program has been tested and experience would indicate that it is accurate within the limits given by the assumptions of the theory used, we make no warranty as to workability of this software or any other licensed material. No warranties either expressed or implied (including warranties of fitness) shall apply. No responsibility is assumed for any errors, mistakes or misrepresentations that may occur from the use of this computer program. The user accepts full responsibility for assessing the validity and applicability of the results obtained with this program for any specific case.

# Case 20: Sensitivity Analysis

# Description

In this example, Sensitivity Analysis will be used to examine the effect of uncertainty in the service life of a Primary Leachate Collection system. The landfill from Cases 15 and 16 will be used, except the time that the Primary Leachate Collection system begins to fail will range from 15 to 50 years. Cases 15 and 16 should be reviewed prior to reading this example, where the implementation of the Variable Properties and Passive Sink special features are described in detail.

The parameters for this example are the same as in Case 15, except for the addition of the Sensitivity Analysis parameters.

<b>Property</b>		<u>Value</u>	<u>Units</u>
Darcy Velocity	v <sub>a</sub>	variable	m/a
Sink Outflow Velocity	v <sub>s</sub>	variable	m/a
Diffusion Coefficient Dispersivity	D	0.02 0.4	m <sup>2</sup> /a m
Distribution Coefficient Soil Porosity Granular Layer Porosity	K n n	0.0 0.4 0.3	cm <sup>3</sup> /g
Dry Density Layer 1 Thickness Layer 2 Thickness Layer 3 Thickness Source Concentration Ref. Height of Leachate	H H C <sub>O</sub> H <sub>r</sub>	1.5 1.0 0.3 2.0 1000 7.5	g/cm <sup>3</sup> m m mg/L cm
Vol. of Leachate Collected	Q <sub>c</sub>	variable	m/a
Landfill Length Landfill Width Aquifer Thickness Aquifer Porosity	L W h n <sub>b</sub>	200.0 1.0 1.0 0.3	m m -
Aquifer Outflow Velocity	v <sub>b</sub>	4.0	m/a
Minimum Failure Start Time Maximum Failure Start Time		15 50	a a

This example is for a hypothetical landfill and is used to illustrate how to prepare an input file and run an analysis using the Variable Properties and Passive Sink option. The example is not a prescription for modelling contaminant migration during operation of a landfill. Each landfill has its own unique characteristics and no general prescription can be made. These options should only by used by someone with the hydrogeologic and engineering background necessary to appreciate the subtleties associated with the physical situation and the steps necessary for appropriate modelling of this physical situation. This option should not be used for an actual project of importance without the guidance of the program developers.

# **Data Entry**

l

Start the POLLUTEv7 program and open the Examples project. Select Case 20 and open the model by double clicking on it in the model list. After the model is displayed, the data for the model can be displayed and edited using the Data Entry menu or by clicking on that part of the model.

# General Data

The general data for this example is the same as for Case 15, except that the title is different.

# Layer Data

The layer data for this example is the same as for Case 15.

# **Boundary Conditions**

The boundary conditions for this example is the same as for Case 15.

### **Run Parameters**

The run parameters for this example are the same as for Case 15, except that the concentrations will be only be calculated at a depth off 3.3 m as shown on the next page. This depth corresponds to the base of the aquitard.

Run Pa	arameters
Туре	Concentrations at Specified Times
	b <sub>g</sub>
All C	Depths Number of Depths: 1 Yes Number: 1   ↓ ↓ ↓ No Depth: 3.3 m ↓
	✓ OK X Cancel ? Help

# **Special Features**

The time-varying data, passive sink, and sensitivity analysis data for this model can be entered using the Time-varying Data and Passive Sink menu items in the Special Features menu.

## **Time-Varying Properties**

The time-varying properties for this example is the same as for Case 15.

### **Passive Sink**

The passive sink data for this example is the same as for Case 15.

### **Sensitivity Analysis**

The sensitivity analysis data can be specified by selecting the Sensitivity Analysis menu item from the Special Features menu, the form on the next page will be displayed. The number of simulations and data ranges can be specified on the General tab. The number of simulations is usually between 1000 and 10000. However, the time to compute this many simulations may be quite large. It is suggested as a trial to use less than 50 simulations.

Sensitivity Analysis
General Variable Entry
▶
Number of Simulations 2000
Number of Data Ranges 50
List All Results
No C Yes
V DK K Cancel ? Help

On the Variable Entry tab below, the type and distribution for the variable can be specified. To vary the failure time of the Primary Leachate Collection system, the Variable Properties end time that corresponds to the time of failure in the input data set is used.

Sensitivity Analysis	
General Variable Entry	
Variable Type C Initial Source Concentration	R
C Darcy Velocity	
C Layer Thickness	
C Diffusion Coefficient	Time Group: 1
C Distribution Coefficient	
Variable Properties End Time	
	1
	Minimum: 15
	Maximum: 50
🖌 ОК	X Cancel ? Help

# **Model Execution**

To run the model and calculate the concentrations either select the Run menu item from the Execute menu or press the Run button on the toolbar.

# **Model Output**

After the model has been executed, the output for the model will be displayed. The initial display will depend on your settings in the program's preferences.

### **Distribution of Peak Concentration**

The Distribution of Peak Concentration chart below can be displayed by pressing the Distribution of Peak Concentration button on the Output toolbar or selecting the Distribution of Peak Concentration menu item from the Output menu.



Using the chart of the probability of peak chloride concentration predictions can be made about the concentration in the aquifer. For example, in this case, the expected maximum concentration is 23.6 mg/L.

### **Distribution of the Time of Peak Concentration**

The Distribution of the Time Peak Concentration chart below can be displayed by pressing the Distribution of Time of Peak Concentration button on the Output toolbar or selecting the Distribution of Time of Peak Concentration menu item from the Output menu. Using this chart the expected time of the maximum concentration can be predicted. In this example, the expected time is 68.9 years.



## **Output Listing**

To display the output as a text listing that will show the calculated concentrations as numbers, select the List Output menu item from the Output menu or press the Output Listing button on the Output toolbar.

### Case 20: Sensitivity Analysis

#### THE VARIABLE VELOCITY AND/OR CONCENTRATION OPTION HAS BEEN USED NOTE THAT THE ACCURACY OF THE CALCULATIONS WITH THIS OPTION WILL DEPEND ON THE NUMBER OF SUBLAYERS USED

#### THE PASSIVE SINK OPTION HAS BEEN USED NOTE : THE USER IS RESPONSIBLE FOR ENSURING THAT VELOCITY CHANGES ARE CONSISTENT WITH THE PASSIVE SINK

### Layer Properties

Layer	Thickness	Number of Sublayers	Coefficient of Hydrodynamic	Matrix Porosity	Distributon Coefficient	Dry Density
			Dispersion	{		
Clay	1 m	4	0.02 m2/a	0.4	0 cm3/g	1.5 g/cm3
Collection System	0.3 m	4	10 m2/a	0.3	0 cm3/g	1.5 g/cm3
Aquitard	2 m	4	0.02 m2/a	0.4	0 cm3/g	1.5 g/cm3

#### **Boundary Conditions**

#### Finite Mass Top Boundary

#### Fixed Outflow Bottom Boundary

Landfill Length = 200 m Landfill Width = 1 m Base Thickness = 1 m Base Porosity = 0.3

#### VARIATION IN PROPERTIES WITH TIME:

#### TIME PERIODS WITH THE SAME SOURCE AND VELOCITY

Period	Start Time	No. of	Time Step	Source Conc	Rate of	Height of	Volume
		Steps			Change	Leachate	Collected
1	0 yr	1	20 yr	1000 mg/L	0	7.5 m	0.29 m/a
2	20 yr	5	2 yr	-1 mg/L	0	7.5 m	0.2 m/a
3	30 ýr	2	10 yr	-1 mg/L	0	7.5 m	0.2 m/a
4	50 yr	5	10 yr	-1 mg/L	0	7.5 m	0.2 m/a
5	100 yr	5	20 ýr	-1 mg/L	Q	7.5 m	0.2 m/a
	ŕ			Ŭ	L		

Period	Start Time	End Time	Darcy Velocity	Dispersivity	Base Velocity
1	0 yr	20 yr	1 m/a	0.4 m	4 m/a
2	20 yr	30 yr	1 m/a	0.4 m	4 m/a
3	30 ýr	50 ýr	1 m/a	0.4 m	4 m/a

4	50 yr	100 yr	1 m/a	U.4 m	4 m/a
5	100 yr	200 yr	1 m/a	0.4 m	4 m/a
	I				

### VELOCITY AND SINK PROFILE:

Time Period	Minimum Depth	Maximum Depth	Vertical Velocity	Horizontal Outflow
1	. Om	. <u>1</u> m	. 0.01 m/a	O_m/a
	1 m	1.3 m	0.01 m/a	_ 6.67 m/a
	. 1.3 m	3.3 M	Ľ Um/a ₽	_ Um/a
2	0 m	) 1 m	₹ 0.028 m/a	0 m/a
	1 m	[ 1.3 m	₹ 0.028 m/a	18.7 m/a
	1.3 m	l 3.3 m r	₽ Om/a	0 m/a
3	0 m	1 m	0.046 m/a	0 m/a
	1 m	1.3 m	0.046 m/a	30.7 m/a
	1.3 m	3.3 m	Um/a	Um/a
4	0 m	1 m	0.064 m/a	O m/a
	1 m	1.3 m	0.064 m/a	42.7 m/a
	1.3 m	3.3 m	Um/a	, Um/a
5	- 0 m	- 1 m	- 0.082 m/a	- Om/a
	1 m	1.3 m	0.082 m/a	54.7 m/a
	1.3 m	3.3 m	U m/a	U m/a
6	0 m	1 m	0.1 m/a	0 m/a
	1 m	1.3 m	0.1 m/a	66.7 m/a
	1.3 m	3.3 m	Um/a	Um/a
7	0 m	1 m	0.1 m/a	0 m/a
	1 m	1.3 m	0.1 m/a	66.7 m/a
	1.3 m	3.3 m	0 m/a	U m/a
8	0 m	1 m	0.1 m/a	0 m/a
	; 1 m	1.3 m	0.1 m/a	66.7 m/a
	1.3 m	( 3.3 m	[ Om/a	0 m/a
9	0 m	1 m	0.1 m/a	- Om/a
	1 m	1.3 m	0.1 m/a	66.7 m/a
	1.3 m	3.3 m	Um/a	Um/a
10	0 m	1 m	0.1 m/a	0 m/a
	1 m	1.3 m	0.1 m/a	66.7 m/a
	. 1.3 m	3.3 m 🔸	l Um/a I≯	Um/a
11	0 m	1_m	0.1 m/a	O_m/a
	1 m	1.3 m	t 0.1 m/a	t 66.7 m/a
	- 1.3 m	5 3.3 m	E Um/a	r Um/a
12	0 m	1 m	[0.1 m/a	0 m/a
	1 m	( 1.3 m	[ 0.1 m/a	66.7 m/a
	1.3 m	( <sup>3.3</sup> m	[ Om/a	0 m/a
13		1 m	0.1 m/a	- Om/a
	1 m	1.3 m	0.1 m/a	66.7 m/a
	1.3 m	3.3 m	Um/a	Um/a
I	I	I	1	ı I

14	0 m	. 1 m	- 0.1 m/a	0 m/a
	1 m	[ 1.3 m	₹ 0.1 m/a	66.7 m/a
	. 1.3 m	. 3.3 m	. 0 m/a	. 0 m/a
15	0 m	1 m	0.1 m/a	0 m/a
	1 m	1.3 m I	0.1 m/a	66.7 m/a
	1.3 m	3.3 m	0 m/a	0 m/a
16	0 m	1 m	0.1 m/a	0 m/a
	: 1 m	1.3 m	0.1 m/a	66.7 m/a
	- 1.3 m	- 3.3 m	. 0 m/a	0 m/a
17	. 0 m	1 m	0.1 m/a	. 0 m/a
	1 m	1.3 m	0.1 m/a	66.7 m/a
	1.3 m	3.3 m	0 m/a	0 m/a
18	0 m	l 1 m	5 0.1 m/a	0 m/a
	1 m	l 1.3 m	5 0.1 m/a	66.7 m/a
	. 1.3 m	. 3.3 m	. 0 m/a	. 0 m/a

### Laplace Transform Parameters

**TAU** = 7 **N** = 20 **SIG** = 0 **RNU** = 2

### Sensitivity Analysis Results

 Number of Simulations = 2000

 Number of Data Ranges = 50
 Variable Properties End Time

 Time Period = 1
 Uniform Distribution
 (Minimum = 15
 Maximum = 50)

Depth = 3.3

#### DISTRIBUTION OF PEAK CONCENTRATION

Minimum	Maximum	Number	Probability	Cumulative	Expected
Value	Value	Occur.	_	Probability	Value
2.285E+01	2.289E+01	68	0.03	0.03	7.775E-01
2.289E+01	2.293E+01	53	0.03	0.06	6.070E-01
2.293E+01	2.296E+01	47	0.02	0.08	5.392E-01
2.296E+01	2.300E+01	43	0.02	0.11	4.941E-01
2.300E+01	2.304E+01	41	0.02	0.13	4.719E-01
2.304E+01	2.308E+01	39	0.02	0.15	4.497E-01
2.308E+01	2.312E+01	38	0.02	0.16	4.389E-01
2.312E+01	2.315E+01	38	0.02	0.18	4.396E-01
2.315E+01	2.319E+01	38	0.02	Τ 0.20	4.403E-01
2.319E+01	2.323E+01	37	0.02	0.22	4.294E-01
2.323E+01	2.327E+01	38	0.02	0.24	4.418E-01
2.327E+01	2.331E+01	39	0.02	0.26	4.541E-01
2.331E+01	2.335E+01	40	0.02	0.28	4.665E-01
2.335E+01	2.338E+01	42	0.02	0.30	4.907E-01
2.338E+01	2.342E+01	44	0.02	0.32	5.149E-01
2.342E+01	2.346E+01	47	0.02	0.35	5.509E-01
2.346E+01	2.350E+01	52	0.03	0.37	6.105E-01
2.350E+01	2.354E+01	83	0.04	0.41	9.760E-01
2.354E+01	2.358E+01	153	0.08	0.49	1.802E+00

2.358E+01 2.365E+01 2.365E+01 2.373E+01 2.373E+01 2.377E+01 2.381E+01 2.388E+01 2.398E+01 2.398E+01 2.396E+01 2.400E+01 2.400E+01 2.415E+01 2.415E+01 2.415E+01 2.423E+01 2.426E+01 2.434E+01 2.434E+01 2.434E+01 2.438E+01 2.448E	2.361E+01 2.365E+01 2.365E+01 2.377E+01 2.377E+01 2.381E+01 2.384E+01 2.384E+01 2.396E+01 2.396E+01 2.400E+01 2.400E+01 2.407E+01 2.415E+01 2.415E+01 2.426E+01 2.426E+01 2.434E+01 2.438E+01 2.438E+01 2.442E+01 2.442E+01 2.442E+01 2.445E+01 2.445E+01 2.445E+01 2.445E+01 2.445E+01	244 176 14 15 15 15 16 17 17 18 20 20 20 22 22 26 30 32 38 46 65 21 9	0.12 0.09 0.01 0.01 0.01 0.01 0.01 0.01 0.01	0.61 0.70 0.71 0.71 0.72 0.73 0.74 0.74 0.75 0.76 0.76 0.77 0.78 0.79 0.80 0.81 0.81 0.82 0.83 0.84 0.83 0.84 0.85 0.87 0.88 0.87 0.88 0.87 0.88 0.90 0.93 0.96 0.97	2.879E+00 2.080E+00 1.657E-01 1.662E-01 1.784E-01 1.787E-01 1.790E-01 1.790E-01 2.035E-01 2.038E-01 2.038E-01 2.161E-01 2.409E-01 2.409E-01 2.659E-01 3.031E-01 3.031E-01 3.648E-01 3.648E-01 3.648E-01 3.648E-01 5.620E-01 7.954E-01 2.574E-01 1.105E-01
2.442E+01 2.446E+01	2.446E+01 2.449E+01	46 65	0.02 0.03	0.93	5.620E-01 7.954E-01
2.449E+01 2.453E+01	2.453E+01 2.457E+01	21 9	0.01	0.97	2.574E-01 1.105E-01
2.457E+01	2.461E+01	10	0.01	0.98	1.229E-01
2.461E+01 2.465E+01	2.465E+01 2.469E+01	10 10	0.01 0.01	U.98 0.99	1.231E-01 1.233E-01
2.469E+01	2.472E+01	10	0.01	0.99	1.235E-01
2.472E+01	2.476E+01	11	0.01	1.00	1.361E-01

Expected Maximum Concentration = 2.362E+01

#### DISTRIBUTION OF TIME OF PEAK CONCENTRATION

Minimum	Maximum	Number	Probability	Cumulative	Expected
Value	Value	Occur.	_	Probability	Value
5.500E+01	5.548E+01	28	0.01	0.01	7.733E-01
5.548E+01	5.595E+01	27	0.01	0.03	7.521E-01
5.595E+01	5.643E+01	27	0.01	0.04	7.586E-01
5.643E+01	5.690E+01	27	0.01	0.05	7.650E-01
5.690E+01	5.738E+01	27	0.01	0.07 📢	7.714E-01
5.738E+01	5.786E+01	28	0.01	0.08	8.067E-01
5.786E+01	5.833E+01	27	0.01	0.10	7.843E-01
5.833E+01	5.881E+01	27	0.01	0.11	7.907E-01
5.881E+01	5.929E+01	27	0.01	0.12	7.971E-01
5.929E+01	5.976E+01	27	0.01	0.14	8.036E-01
5.976E+01	6.024E+01	28	0.01	0.15	8.400E-01
6.024E+01	6.071E+01	27	0.01	0.16	8.164E-01
6.071E+01	6.119E+01	27	0.01	0.18	8.229E-01
6.119E+01	6.167E+01	27	0.01	0.19	8.293E-01
6.167E+01	6.214E+01	27	0.01	0.20	8.357E-01
6.214E+01	6.262E+01	28	0.01	0.22	8.733E-01
6.262E+01	6.310E+01	27	0.01	0.23	8.486E-01
6.310E+01	6.357E+01	27	0.01	0.25	8.550E-01
6.357E+01	6.405E+01	27	0.01	0.26	8.614E-01
6.405E+01	6.452E+01	27	0.01	0.27	8.679E-01
6.452E+01	6.500E+01	28	0.01	0.29	9.067E-01
6.500E+01	6.548E+01	27	0.01	0.30	8.807E-01
L 6 548E+01	L 6 595E+01	I 27	L 0.01	0.31	8 871E-01

6.595E+01 6.643E+01 6.738E+01 6.738E+01 6.738E+01 6.833E+01 6.831E+01 6.929E+01 6.929E+01 7.071E+01 7.071E+01 7.119E+01 7.167E+01 7.367E+01 7.367E+01 7.367E+01 7.367E+01 7.500E+01 7.595E+01 7.643E+01 7.690E+01 7.786E+01 7.833E+01	6.643E+01 6.690E+01 6.738E+01 6.738E+01 6.833E+01 6.831E+01 6.929E+01 6.976E+01 7.024E+01 7.071E+01 7.119E+01 7.119E+01 7.214E+01 7.214E+01 7.357E+01 7.405E+01 7.405E+01 7.590E+01 7.595E+01 7.643E+01 7.633E+01 7.738E+01 7.738E+01 7.833E+01 7.881E+01	27 27 28 27 30 82 82 68 54 54 55 54 55 54 55 54 55 54 55 55 54 55 55	0.01 0.01 0.01 0.01 0.04 0.03	0.33 0.34 0.35 0.37 0.38 0.40 0.44 0.44 0.51 0.54 0.57 0.62 0.65 0.68 0.68 0.68 0.70 0.73 0.76 0.73 0.76 0.73 0.76 0.78 0.81 0.81 0.81 0.82 0.89 0.92 0.97 1.00	8.936E-01 9.000E-01 9.129E-01 9.129E-01 1.029E+00 2.831E+00 2.850E+00 2.380E+00 1.903E+00 1.916E+00 1.964E+00 1.964E+00 1.964E+00 2.030E+00 2.030E+00 2.030E+00 2.034E+00 2.044E+00 2.044E+00 2.095E+00 2.095E+00 2.095E+00 2.095E+00 2.095E+00 2.095E+00 2.095E+00 2.095E+00 2.095E+00 2.095E+00 2.095E+00 2.095E+00 2.095E+00
---	---	--	--	--	--

Expected Time of Maximum Concentration = 68.9456445222611

#### VARIABLE NUMBER: 1

Minimum	Maximum	Number	Probability	Cumulative	Expected
Value	Value	Occur.	-	Probability	⊺ Value
1.500E+01	1.570E+01	40	0.02	0.02	3.070E-01
1.570E+01	1.640E+01	40	0.02	0.04	3.210E-01
1.640E+01	1.710E+01	40	0.02	0.06	3.350E-01
1.710E+01	1.780E+01	40	0.02	0.08	3.490E-01
1.780E+01	1.850E+01	40	0.02	0.10	3.630E-01
1.850E+01	1.920E+01	40	0.02	0.12	3.770E-01
1.920E+01	1.990E+01	40	0.02	0.14	3.910E-01
1.990E+01	2.060E+01	40	0.02	0.16	4.050E-01
2.060E+01	2.130E+01	40	0.02	0.18	4.190E-01
2.130E+01	2.200E+01	40	0.02	0.20	4.330E-01
2.200E+01	2.270E+01	40	0.02	0.22	4.470E-01
2.270E+01	2.340E+01	40	0.02	0.24	4.610E-01
2.340E+01	2.410E+01	40	0.02	0.26	4.750E-01
2.410E+01	2.480E+01	40	0.02	0.28	4.890E-01
2.480E+01	2.550E+01	40	0.02	0.30	5.030E-01
2.550E+01	2.620E+01	40	0.02	0.32	5.170E-01
2.620E+01	2.690E+01	40	0.02	0.34	5.310E-01
2.690E+01	2.760E+01	40	0.02	0.36	5.450E-01
2.760E+01	2.830E+01	40	0.02	0.38	5.590E-01
2.830E+01	2.900E+01	40	0.02	0.40	5.730E-01
2.900E+01	2.970E+01	40	0.02	0.42	5.870E-01
2.970E+01	3.040E+01	40	0.02	0.44	6.010E-01
3.040E+01	3.110E+01	40	0.02	0.46	6.150E-01
3.110E+01	3.180E+01	40	0.02	0.48	6.290E-01
3.180E+01	3.250E+01	40	0.02	0.50	6.430E-01

2.900E+01 2.970E+01 3.140E+01 3.110E+01 3.260E+01 3.260E+01 3.320E+01 3.460E+01 3.460E+01 3.670E+01 3.670E+01 3.670E+01 3.880E+01 4.020E+01 4.020E+01 4.020E+01 4.300E+01 4.370E+01 4.540E+01 4.540E+01 4.540E+01 4.560E+01 4.720E+01 4.720E+01 4.930E+01 4.930E+01 4.930E+01 4.930E+01	2.970E+01 3.040E+01 3.110E+01 3.120E+01 3.250E+01 3.320E+01 3.320E+01 3.460E+01 3.600E+01 3.670E+01 3.670E+01 3.870E+01 3.880E+01 3.950E+01 4.020E+01 4.020E+01 4.300E+01 4.370E+01 4.370E+01 4.370E+01 4.510E+01 4.510E+01 4.510E+01 4.520E+01	40 40 40 40 40 40 40 40 40 40 40 40 40 4	0.02 0.02 0.02 0.02 0.02 0.02 0.02 0.02	0.42 0.44 0.46 0.48 0.50 0.52 0.54 0.56 0.58 0.60 0.62 0.64 0.62 0.64 0.62 0.64 0.70 0.72 0.74 0.76 0.74 0.76 0.78 0.80 0.82 0.80 0.82 0.84 0.88 0.80 0.82 0.84 0.88 0.90 0.92 0.94 0.92 0.94 0.98 1.00	5.870E-01 6.010E-01 6.150E-01 6.430E-01 6.570E-01 6.710E-01 6.710E-01 6.990E-01 7.130E-01 7.270E-01 7.410E-01 7.690E-01 7.830E-01 8.250E-01 8.530E-01 8.530E-01 8.530E-01 8.530E-01 8.530E-01 8.530E-01 9.230E-01 9.230E-01 9.230E-01 9.510E-01 9.790E-01 9.790E-01 9.790E-01
--	--	---	--	--	---

Expected Value = 3.250E+01

#### NOTICE

Although this program has been tested and experience would indicate that it is accurate within the limits given by the assumptions of the theory used, we make no warranty as to workability of this software or any other linearead material. No warranty as its accurate within the limits given licensed material. No warranties either expressed or implied (including warranties of fitness) shall apply. No responsibility is assumed for any errors, mistakes or misrepresentations that may occur from the use of this computer program. The user accepts full responsibility for assessing the validity and applicability of the results obtained with this program for any specific case.

Name of Section